

Photoelectron imaging spectroscopy of Ag_3^- in the S_0 and S_1 states

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1 **Photoelectron imaging spectroscopy of Ag_3^- in the S_0 and S_1 states**2 Yuta Suzuki, Tasuku Nishizato, Kazuaki Matsumoto, Yuta Ushiki, Yuma Aoki,
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7 We explore laboratory-frame photoelectron angular distributions (LF-PADs) originating from the
8 outermost two orbitals, σ_u (the highest occupied molecular orbital: HOMO) and σ_g (HOMO-1), of the
9 silver trimer anion (Ag_3^-) in the $S_0(^1\Sigma_g^+)$ state. The experiment was performed by our novel
10 photoelectron imaging technique using a high-repetition-rate tunable laser [T. Horio *et al.*, J. Chem.
11 Phys. **162**, 026101 (2025)]. The LF-PAD for σ_u is found to be highly energy-dependent in a
12 photoelectron kinetic energy (PKE) range from 0 to 1.57 eV; an isotropic LF-PAD with an anisotropy
13 parameter $\beta \sim 0$ is observed at the detachment threshold, exemplifying the Wigner threshold law,
14 whereas β value decreases down to $\beta = -0.4$ at 0.46 eV, followed by an increase up to $\beta = 0.6$ at 1.57 eV,
15 as PKE increases. A small dip discernible in the PKE range of 1.2 – 1.3 eV suggests an influence of the
16 autodetachment process on the β value, which is via bound electronic state(s) embedded in the $D_0(^2\Sigma_u^+)$
17 + e^- continuum. On the other hand, the LF-PAD for σ_g exhibits a strong anisotropy parallel to the laser
18 polarization with β of ~ 1 in 0 – 0.39 eV. These contrasted trends are qualitatively reproduced by
19 theoretical modeling of LF-PAD that accounts for photoelectron partial waves allowed for each
20 photodetachment process. Furthermore, two-photon detachment spectra via the excited $S_1(^1\Sigma_u^+)$ state are
21 presented, where the relative band intensities for the two detachment channels, $D_0(^2\Sigma_u^+) + e^- \leftarrow S_1(^1\Sigma_u^+)$
22 and $D_1(^2\Sigma_g^+) + e^- \leftarrow S_1(^1\Sigma_u^+)$, are discussed in terms of their leading electronic configurations.

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27 **I. INTRODUCTION**

28 The silver trimer anion, Ag_3^- , has been receiving continuous attention over the past decades. A
29 simple Hückel model¹⁻³ and *ab initio* calculations⁴ predicted that the equilibrium geometry of Ag_3^- in
30 the ground electronic state is linear, i.e., $S_0(^1\Sigma_g^+)$, where four valence electrons including the excess
31 charge occupy the outermost molecular orbitals (MOs), σ_u (the highest occupied MO: HOMO) and σ_g
32 (HOMO-1), created mainly by Ag 5s orbitals. The high-resolution photodetachment spectroscopy by
33 Lineberger and coworkers⁵ found that the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transition (i.e., the detachment of an
34 electron from HOMO) occurs at 2.43 ± 0.01 eV, which corresponds to the vertical detachment energy
35 (VDE). At the same time, Ganteför et al.⁶ reported a VDE value of 2.452 eV using zero-kinetic-energy-
36 electron (ZEKE) spectroscopy of jet-cooled Ag_3^- ; the authors pointed out that the slightly larger VDE is
37 likely due to the internal temperature of the samples lower than that in ref.⁵. A theoretical estimate of
38 2.455 eV by Bonačić-Koutecký et al.⁴ is in excellent agreement with these experimental VDEs. The
39 electron binding energy for the $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transition (i.e., the detachment of an electron
40 from HOMO-1) has been reported to be 3.62 eV by Handschuh et al.⁷ This anion also served as a
41 precursor for demonstrating negative-to-neutral-to-positive (NeNePo) spectroscopy that explores time-
42 resolved dynamics in the neutral state.^{8,9}

43 Recently, we conducted photodestruction action spectroscopy of Ag_3^- in the photon energy range of
44 2 – 5 eV using an ion trap to investigate its excited electronic states,¹⁰ where photodestruction signals
45 (i.e., depletion in the number of Ag_3^- anions in the trap) were obtained through detachment of the excess
46 electron and/or fragmentation of Ag_3^- upon photoirradiation. It was found that the spectrum exhibits a
47 relatively sharp resonance due to the $S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ transition at 2.39 eV, i.e., just below VDE,
48 which is followed by a broad hump around 3.8 eV.

49 These studies have motivated us to further advance the continuous investigations on Ag_3^- . The
50 objective of the present study is twofold. First, we attempt to characterize HOMO (σ_u) and HOMO-1
51 (σ_g) of Ag_3^- in $S_0(^1\Sigma_g^+)$ from energy-dependent laboratory-frame photoelectron angular distributions

52 (LF-PADs). To this end, we employ our novel photoelectron velocity-map imaging (VMI) setup that
53 utilizes a tunable femtosecond (fs) laser at a 100 kHz repetition rate. The technique was demonstrated
54 very recently by measuring two-dimensional (2D) projections of photoelectrons detached from Ag_3^- at
55 various photon energies.¹¹ Here, we provide a full account of the observed images along with a
56 theoretical modeling of LF-PAD using the ezDyson program.^{12,13} Second, taking advantage of tunable
57 and short pulses from the 100-kHz laser system, we attempt to obtain one-color, two-photon detachment
58 spectra via the $S_1(^1\Sigma_u^+)$ state of Ag_3^- to gain insight into the electronic configuration of this transient
59 state.

60

61 II. EXPERIMENTAL AND COMPUTATIONAL METHODS

62 The whole experimental setup including the photodetachment light source has been described in our
63 recent reports.^{11,14} A continuous beam of Ag_3^- was produced by combination of a magnetron-sputtering
64 ion source and a quadrupole mass filter (QMF). The Ag_3^- anions were delivered from the exit lens of
65 QMF to a potential switch (PS) with octopole ion guides driven by radio-frequency (rf) generators
66 operated at a frequency of ~ 1 MHz. At the PS, the continuous beam of Ag_3^- was chopped into 100-kHz
67 anion bunches by +0.4-kV pulses synchronized with laser pulses from an Yb:KGW (ytterbium-doped
68 potassium gadolinium tungstate) regenerative amplifier. The light source produced ~ 210 fs, 100 μJ , and
69 1030 nm pulses with linear polarization at a 100 kHz repetition rate; 80% of its output (i.e., 80 μJ /pulse)
70 was used to pump an optical parametric amplifier that generated fs pulses tunable from near infrared
71 (NIR) to visible (VIS) (620 – 2600 nm). For generating wavelengths shorter than 620 nm, we used an
72 additional beta-barium borate (β -BBO) crystal for frequency doubling the NIR and VIS pulses.

73 The bunched Ag_3^- beam focused with an einzel lens was admitted to an assembly of photoelectron
74 extraction lenses optimized at low extraction fields¹⁵ for achieving the VMI condition.¹⁶ For examining
75 LF-PADs, we measured two-dimensional (2D) projections of photoelectrons ejected by the fs pulses into

76 three dimension. The photon energy was varied from 2.43 to 4.00 eV to observe one-photon detachment
77 from HOMO (σ_u) and HOMO-1 (σ_g) of Ag_3^- in $S_0(^1\Sigma_g^+)$, whereas it was tuned at the resonance to the
78 $S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ transition in one-color, two-photon detachment experiments. The peak laser power
79 at the laser-anion interaction region was estimated to be $10^8 - 10^9$ W/cm².

80 A dual microchannel plate ($\phi 40$ mm) coupled with a phosphor screen (P43) was used to visualize
81 photoelectron 2D projections. In our previous studies,^{11,14,17,18} we used a frame-based (i.e., conventional)
82 digital camera for obtaining photoelectron images, where intensities of bright spots on the phosphor
83 screen were recorded for 500 ms and the measurements were repeated until an accumulated image
84 reached an acceptable signal to noise ratio. In the present study, we have installed a new digital camera
85 (SilkyEvCam HD, 1280×720 pixels, CenturyArks Co., Ltd.) equipped with an event-based vision sensor,
86 which enables us to perform event counting of bright spots on the phosphor screen (see Supplementary
87 Information for further details). Since some of the bunched Ag_3^- anions emitted low energy electrons
88 upon collision with the VMI electrodes, an image of such background electrons was recorded with the
89 photodetachment laser turned off (a laser-off image), which was subtracted from a laser-on image to
90 remove the backgrounds. The 2D projection thus obtained was analyzed by the polar onion-peeling
91 (POP) method¹⁹ to reconstruct the original 3D distribution of the detached photoelectrons, which yielded
92 photoelectron-kinetic-energy (PKE) distributions (i.e., photoelectron spectra) and LF-PADs.

93 The electronic-structure calculations were performed with the Q-chem 5.4 package²⁰ to simulate
94 energy dependence of LF-PADs using ezDyson 5.0.^{12,13} The equilibrium geometry of Ag_3^- in the
95 $S_0(^1\Sigma_g^+)$ state was optimized by the coupled-cluster single and double (CCSD) theory with the aug-cc-
96 pVDZ-PP^{21,22} basis set, which has found that the most stable structure is linear with the Ag-Ag bond
97 lengths of 2.67 Å. The equation-of-motion ionization potential CCSD (EOM-IP-CCSD) methodology
98 with the same basis set was further performed to calculate Dyson orbitals, which were used for ezDyson
99 to simulate LF-PADs. For comparison, we also calculated LF-PAD using Kohn-Sham orbitals with
100 BP86^{23,24} functional and LanL2DZ²⁵ basis set with the corresponding effective core potential. EOM-EE-

101 CCSD theory calculations were also used to estimate vertical electron excitation energies (VEEs) of
102 optically allowed transitions from the gerade state of $S_0(^1\Sigma_g^+)$ to ungerade states.

103

104 III. RESULTS AND DISCUSSION

105 A. Energy dependence of LF-PADs from σ_u and σ_g orbitals

106 Figure 1 shows 2D slice images of photoelectrons detached from Ag_3^- in the $S_0(^1\Sigma_g^+)$ state, obtained
107 for the photon energies of (a) 2.43, (b) 2.53, (c) 2.64, (d) 2.76, (e) 2.89, (f) 3.02, (g) 3.18, (h) 3.35, (i)
108 3.45, (j) 3.65, (k) 3.77, and (l) 3.88 eV; the original projected images before transformed to these 2D
109 slices are shown in Fig. S3 in Supplementary Material. Isotropic distributions are observed at (a) 2.43
110 and (b) 2.53 eV. The images gradually become anisotropic with more photoelectrons emitted
111 perpendicular to the laser polarization direction (ε in Fig. 1(a)) with increasing the photon energy from
112 (c) 2.64 to (e) 2.89 eV; the ring diameter increases accordingly, which is proportional to the
113 photoelectron velocity. The perpendicular anisotropy turns to be less prominent at (f) 3.02 eV. Then the
114 LF-PADs return to be nearly isotropic at (g) 3.18, (h) 3.35, and (i) 3.45 eV. These photoelectrons

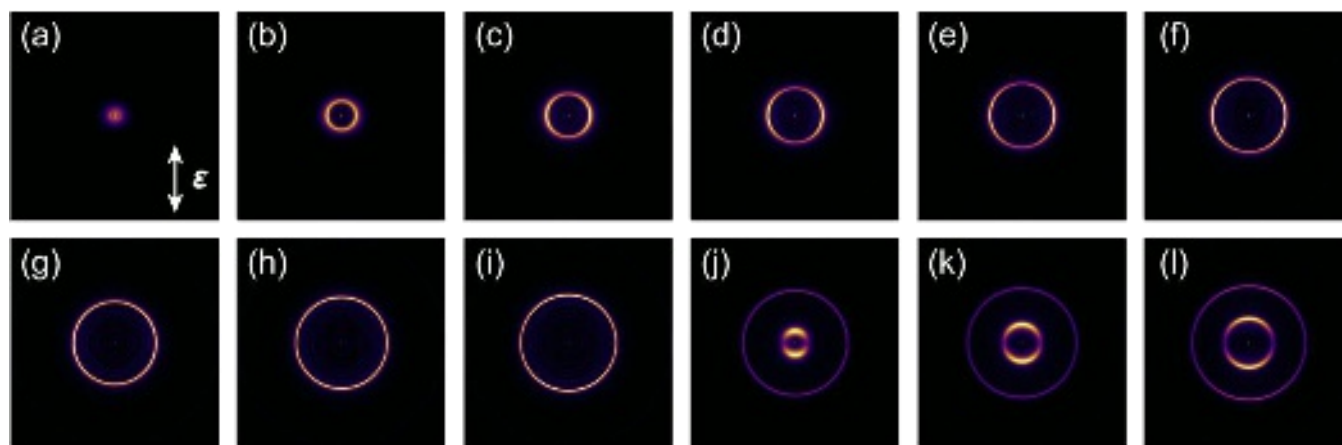


Figure 1. 2D slices of photoelectron distributions for Ag_3^- obtained at (a) 2.43, (b) 2.53, (c) 2.64, (d) 2.76, (e) 2.89, (f) 3.02, (g) 3.18, (h) 3.35, (i) 3.45, (j) 3.65, (k) 3.77, and (l) 3.88 eV. The direction of the polarization vector, ε , of the photodetachment laser is indicated by a double arrow in (a). The original projected images before transformation to these 2D slices can be found in Fig. S3 in Supplementary Information.

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115 originate from the lowest-energy detachment channel, $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$. The image indicates a
 116 significant change at (j) 3.65 eV, showing an additional component at the center. The inner component
 117 is assignable to the second detachment channel, $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$. As manifested in Figs. 1(j),
 118 1(k), and 1(l), the photoelectrons for this channel exhibit a strong anisotropy parallel to ε .

119 In single-photon detachment from randomly oriented samples with a linearly-polarized light, LF-
 120 PAD is proportional to $1 + \beta P_2(\cos\theta)$,²⁶ where θ , β , and $P_2(x)$ are the polar angle with respect to the
 121 laser polarization vector (ε), the photoelectron anisotropy parameter ranging from -1 to $+2$, and the 2nd
 122 order Legendre polynomial, respectively. The β parameters obtained by POP are plotted in Fig. 2(a) as a
 123 function of PKE for the photoelectrons both in the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ (circles) and in the $D_1(^2\Sigma_g^+)$
 124 $+ e^- \leftarrow S_0(^1\Sigma_g^+)$ transitions (squares). The β values for the former transition vary significantly from
 125 negative through positive as a function of PKE, whereas those for the latter transition are less energy-
 126 dependent, although the data points are limited; the estimation of errors in the β parameters is described
 127 in Supplementary Material.

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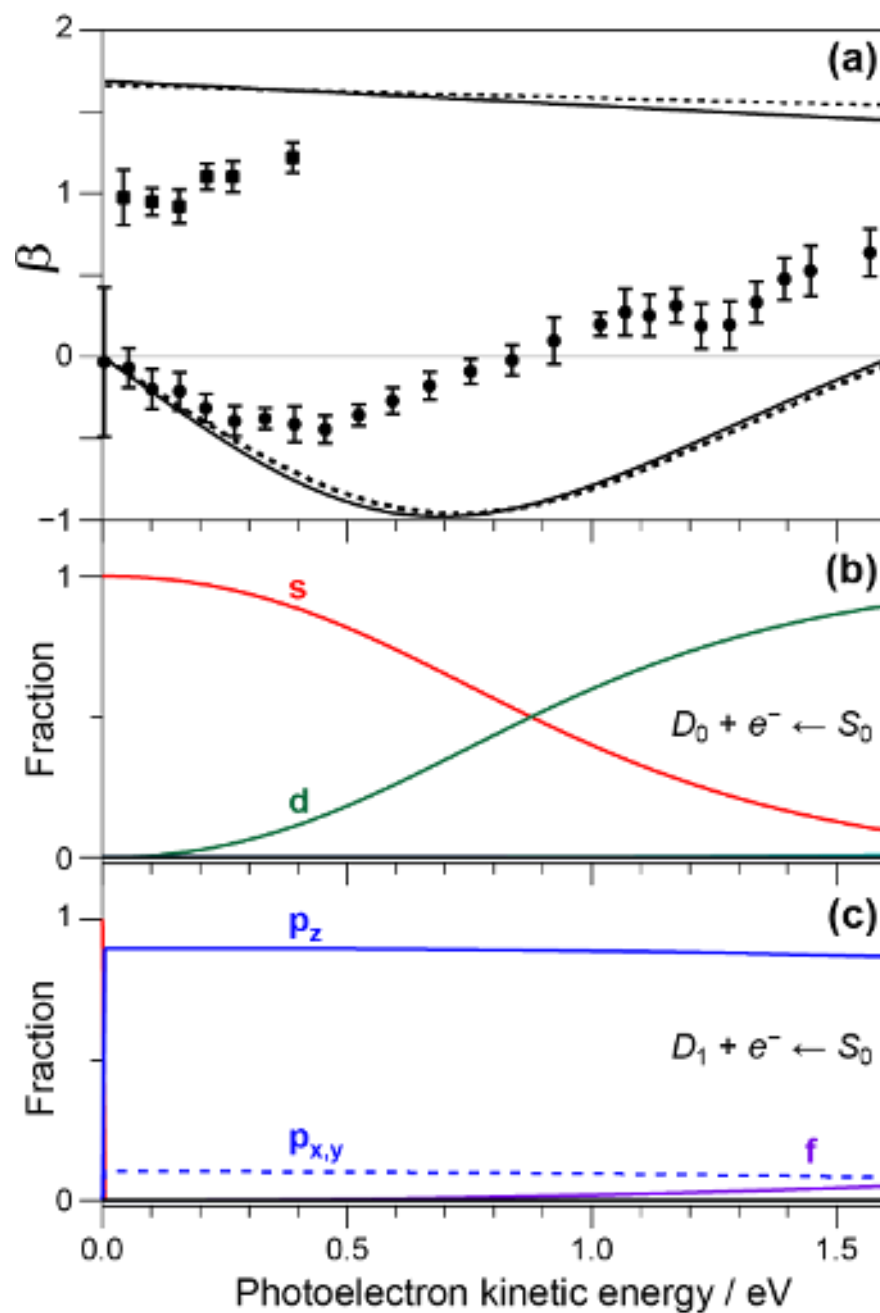


Figure 2. (a) Photoelectron anisotropy parameters, β , evaluated from the photoelectron images for the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ (circles) and $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transitions (squares) of Ag_3^- as a function of photoelectron kinetic energy. The results of simulation are superimposed by the solid and dashed curves, which are obtained by ezDyson 5.0 using EOM-IP-CCSD/aug-cc-pVDZ-PP and BP86/LanL2DZ level of calculations, respectively (see the text). (b) and (c): Partial wave analyses for photoelectrons ejected via the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ and the $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transitions, respectively, obtained by the EOM-IP-CCSD/aug-cc-pVDZ-PP level of calculations.

133 The EOM-IP-CCSD theory calculation with aug-cc-pVDZ-PP basis sets performed in the present
 134 study has found that the former and the latter transitions can be well described by detachment of an
 135 electron from the outermost two MOs, σ_u and σ_g , respectively. The corresponding valence electron
 136 configurations of $D_0(^2\Sigma_u^+)$ and $D_1(^2\Sigma_g^+)$ are therefore approximated as $(\sigma_g)^2(\sigma_u)^1$ and $(\sigma_g)^1(\sigma_u)^2$, as
 137 illustrated in Fig. 3. The calculation also evaluated the VDE and the second electron binding energy to
 138 be 2.33 and 3.59 eV, respectively, which reasonably reproduce the experimental values of 2.43 (ref. ⁵) /
 139 2.452 (ref. ⁶) and 3.62 eV.⁷

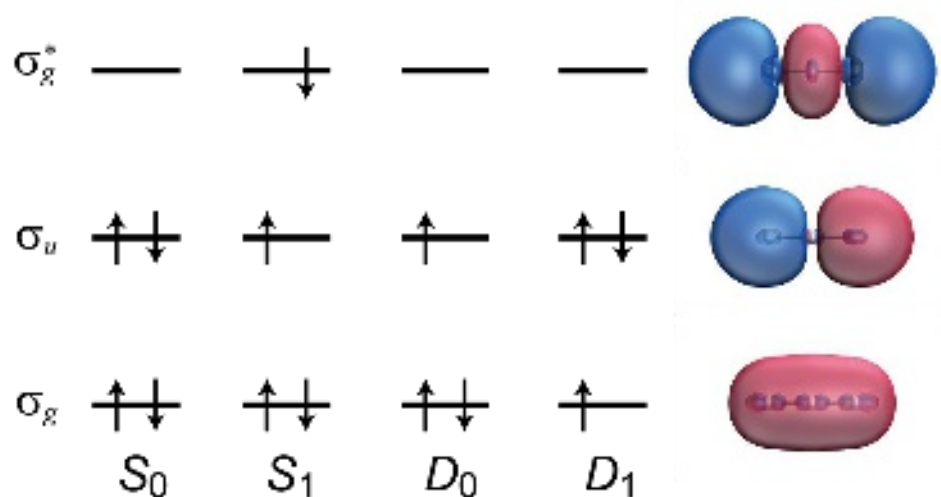


Figure 3. The leading electronic configurations of S_0 , S_1 , D_0 , and D_1 states for anionic and neutral silver trimers along with the iso-surface plots of σ_g , σ_u , and σ_g^* MOs formed mainly with 5s atomic orbitals of silver atoms. The plots were obtained by the BP86/LanL2DZ level of calculation.

140 Due to its ungerade symmetry, single-photon detachment from the σ_u orbital results in emission of
 141 photoelectron partial waves only with gerade symmetries (i.e., s, d, g, ...). According to the Wigner
 142 threshold law,²⁷ the photodetachment cross section is proportional to $E^{l+1/2}$, where E and l denote PKE
 143 and the angular momentum quantum number of the detached electron, respectively. This indicates that s-
 144 wave ($l = 0$) is dominant when E is close to zero, leading to $\beta = 0$. As manifested in Fig. 2(a), our
 145 experimental result obtained for the photodetachment from the σ_u orbital (i.e., $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$)

146 exemplifies this threshold law. On the other hand, photodetachment from the σ_g orbital gives rise to
147 emission of photoelectron partial waves only with ungerade symmetries, (i.e., p, f, h, ...), indicating that
148 the β value does not fall off to zero even at the threshold, which is consistent with the present
149 observation as far as PKE is greater than ~ 0.04 eV (the first data point for the $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$
150 channel in Fig. 2(a)).

151

152 **B. Theoretical modeling of LF-PADs by ezDyson**

153 The solid and dashed curves in Fig. 2(a) present theoretical β parameters evaluated from LF-PADs
154 obtained with the EOM-IP-CCSD/aug-cc-pVDZ-PP and BP86/LanL2DZ levels of calculations,
155 respectively. As mentioned in Section II, the former level of calculation provided the Dyson orbitals for
156 the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ and $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ photodetachment processes, whereas the latter
157 produced the Kohn–Sham orbitals shown in Fig. 3, which were used as substitutes for the corresponding
158 Dyson orbitals; either Dyson or Kohn–Sham orbitals were used for the evaluation of β parameters. In
159 both cases, we assumed a plane wave for the photoelectron wave function with the maximum angular
160 momentum quantum number of 5 (i.e., h-wave). The trends in the energy dependence of the
161 experimental β parameters are reproduced by both theoretical approaches qualitatively; the simulations
162 either underestimate in the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ channel or overestimate in the $D_1(^2\Sigma_g^+) + e^- \leftarrow$
163 $S_0(^1\Sigma_g^+)$ channel.

164 Figure 2(b) shows partial wave decompositions for photoelectrons ejected from the $D_0(^2\Sigma_u^+) + e^- \leftarrow$
165 $S_0(^1\Sigma_g^+)$ transition, as obtained by the EOM-IP-CCSD/aug-cc-pVDZ-PP level of calculation. It is
166 obvious that s-wave (red curve) is dominant at the threshold, which reconfirms the Wigner threshold law.
167 As PKE increases, the contribution of d-wave (green curve) shows up, which results in interference
168 between s- and d-waves. In the plane-wave approximation, where interaction of an outgoing electron
169 and a residual neutral core is ignored, the s- and d-waves exhibit destructive interference along the laser

170 polarization axis.^{28,29} This leads to negative β values (see the solid line in the lower part of Fig. 2(a))
171 from the threshold to around 0.7 eV with the minimum value of -1 , followed by a monotonic increase,
172 as the contribution of d-wave becomes dominant above 0.9 eV. Although this scenario qualitatively
173 explains the energy dependence observed for the β values, the experimental data exhibit a minimum
174 with $\beta = -0.4$ at 0.46 eV. The underestimation of β values in the ezDyson calculations is ascribed to the
175 assumption that outgoing photoelectrons are described as a plane wave. Figure 2(c), on the other hand,
176 shows similar partial wave decompositions for photoelectrons in the $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transition.
177 The leading contribution of p_z -wave in this channel, which is dominant even just above the threshold,
178 explains the high β values ($\beta > 1$) as presented in the upper part of Fig. 2(a). The partial-wave
179 decomposition analysis is thus qualitatively in line with the symmetry considerations discussed above.

180

181 C. Comparison with LF-PADs for Na_3^-

182 Herein, we compare our experimental results for Ag_3^- with those observed for Na_3^- . The equilibrium
183 geometry of Na_3^- in the S_0 state is also linear with the bond lengths of 3.581 Å.³⁰ Therefore, the valence
184 electron configuration is expected to be $(\sigma_g)^2(\sigma_u)^2$ as well, which are created by the interaction of Na 3s
185 orbitals. Using an excimer-laser-pumped dye laser generating VIS and ultraviolet pulses with 1.64 –
186 4.28 eV photon energies, Bartels et al.³¹ investigated Na_3^- by measuring energy-dependent LF-PADs for
187 photodetachment from σ_u and σ_g orbitals. Due to the tuning range of the detachment laser with respect
188 to the VDE of Na_3^- (1.158 ± 0.010 eV),³² the minimum PKE of the measurement for the σ_u orbital was
189 0.48 eV, where isotropic distribution ($\beta \sim 0$) is observed. As PKE increases, the measured β value rises
190 and reaches ~ 1.8 at PKE = 3.1 eV. Although the absolute values of β are different from those obtained
191 for Ag_3^- , the upward trend in β values above ~ 0.5 eV is common to these two clusters. As for LF-PAD
192 from the σ_g orbital, the β values obtained for Na_3^- are 1.2 – 1.3 in the PKE region of 0.0 – 0.4 eV,³¹

193 which are comparable with those for Ag_3^- . Thus, the present study has shown that Na_3^- and Ag_3^- are
194 valence iso-electronic systems in terms of the photoelectron angular anisotropy.

195

196 **D. Excited states below and above the photodetachment threshold**

197 Closer examination of Fig. 2(a) reveals a small dip in the experimental β values around 1.2 – 1.3 eV
198 for the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ channel (circles). To discuss this point, we refer to the photodestruction
199 action spectrum of Ag_3^- in Fig. 4 (blue triangles) cited from ref.,¹⁰ which was obtained using an ion trap
200 cooled at 100 K. A sharp resonance signal is observed at 2.39 eV, just below VDE (the vertical dashed
201 line in the figure), which is assignable to the $S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ absorption; a tail extending toward a
202 lower energy region is attributed to hot bands that are unresolved in our measurements;¹⁰ the harmonic
203 vibrational frequencies of the symmetric stretching, bending, and anti-symmetric stretching modes were

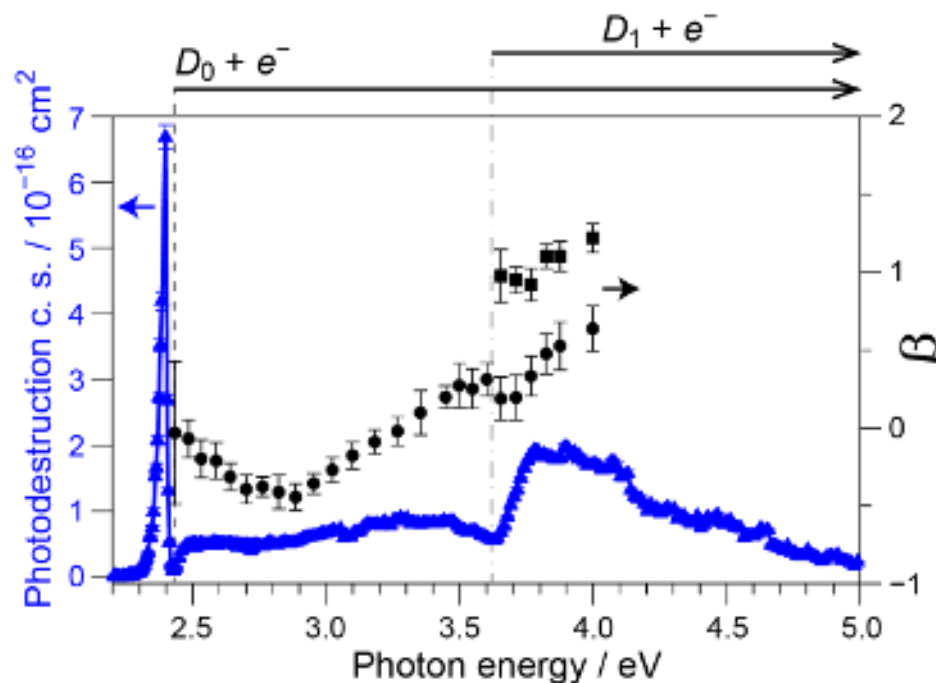


Figure 4. Photodestruction action spectra (blue triangles) of Ag_3^- obtained at an ion trap temperature of 100 K,¹⁰ along with the β values for the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ (circles) and $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transitions (squares) plotted as a function of photon energy. The vertical dashed line shows the VDE, while the dash-dotted line indicates the second detachment threshold.

204 estimated to be 110, 39, and 179 cm^{-1} , respectively, by the CCSD/aug-cc-PVDZ-PP level of calculation.
205 Such an asymmetric profile due to hot bands is seen also in the photodetachment spectra of Ag_3^- in ref. ⁵
206 and in the present study (see Fig. S5 in Supplementary Information).

207 We confirmed that the photodestruction signal corresponding to the $S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ transition is
208 induced by one-photon process. This sharp resonance is followed by nearly structureless absorption with
209 its onset at the VDE. This manifests that the transition from $S_0(^1\Sigma_g^+)$ to the $D_0(^2\Sigma_u^+) + e^-$ continuum
210 indeed starts around this energy, yielding the structureless absorption from the detachment threshold.
211 Another feature discernible in the spectrum is a broad hump observed around 3.8 eV. As summarized in
212 Table S2 in Supplementary Information, the present EOM-EE-CCSD/aug-cc-pVDZ-PP calculation
213 predicts that optically allowed states lie at 2.45 ($^1\Sigma_u^+$), 3.23 ($^1\Pi_u$), 3.42 ($^1\Sigma_u^+$), 3.57 ($^1\Sigma_u^+$), 4.01 ($^1\Pi_u$),
214 and 4.97 ($^1\Pi_u$) eV. The lowest one corresponds reasonably to the $S_1(^1\Sigma_u^+)$ state. The photoabsorption
215 from $S_0(^1\Sigma_g^+)$ to the $^1\Sigma_u^+$ state at 3.57 eV and/or the $^1\Pi_u$ state at 4.01 eV could account for the 3.8-eV
216 hump, which slightly modifies our former assignment proposed in ref. ¹⁰. Another broad band seen in
217 3.1 – 3.5 eV, which is rather unnoticeable most likely due to overlap of the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$
218 continuum absorption, may be a signature of two other states below 3.5 eV.

219 Here, we superimpose the experimental β values on the photodestruction action spectrum, which
220 are already presented in Fig. 2(a) but are replotted as a function of photon energy in Fig. 4. The result
221 reveals that the variation of the β values associated with the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ channel (circles in
222 Fig. 4) is relatively smooth up to ~ 3.6 eV, where the β values turns to a significant drop. Concomitantly,
223 the sharp, intense rise in the photodestruction spectrum due to the aforementioned $^1\Sigma_u^+$ and/or $^1\Pi_u \leftarrow$
224 $S_0(^1\Sigma_g^+)$ absorption shows up. Therefore, the dip in the β values around 3.7 eV is suggestive of
225 autodetachment process(es) via these bound excited states embedded in the $D_0(^2\Sigma_u^+) + e^-$ continuum. It
226 would be highly probable that the β values obtained for the $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ channel (squares in

227 Fig. 4) are also affected by these bound electronic states. The present study has demonstrated that
228 photodestruction action spectroscopy greatly assists the interpretation of energy-dependent LF-PADs.

229

230 E. Two-photon detachment via the $S_1(^1\Sigma_u^+)$ state

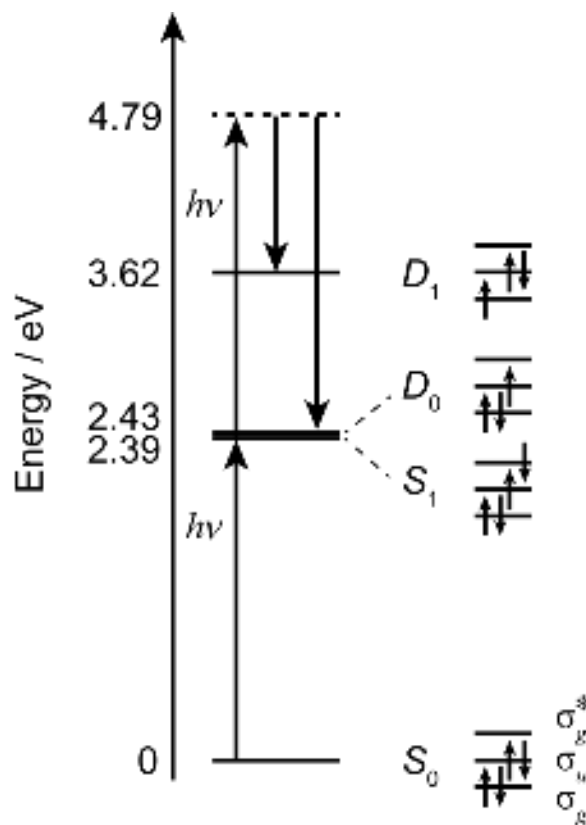


Figure 5. An energy diagram of the two-photon detachment via the $S_1(^1\Sigma_u^+)$ state of Ag_3^- .

231 By tuning the photon energies at the $S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ transition, we carried out single-color, two-
232 photon detachment experiments, as schematically illustrated in Fig. 5. Figure 6(a) shows photoelectron
233 spectra obtained with laser pulses at 2.35, 2.39, and 2.43 eV, where the intensity is normalized to unity
234 at the most intense bands in the vicinity of PKE = 0 eV (the original photoelectron images obtained by
235 2.35- and 2.39-eV irradiation are displayed in Figs. S6(a) and S6(b), respectively, in Supplementary
236 Material). In addition to the intense 0-eV components, the spectrum measured by laser pulses at 2.35
237 (2.39) eV exhibits two other peaks at 2.22 (2.30) and 1.09 (1.18) eV. Table 1 lists these values along
238 with those expected for two-photon detachment leading to the neutral final states of $D_0(^2\Sigma_u^+)$ and

239 $D_1(^2\Sigma_g^+)$. Agreement between the peak PKEs observed and those expected confirms that the final states
 240 for the higher and the lower energy peaks in Fig. 6(a) are assigned as $D_0(^2\Sigma_u^+)$ and $D_1(^2\Sigma_g^+)$, respectively.
 241 As for the 2.43-eV spectrum, the two-photon detachment signals are significantly weaker than the
 242 former two cases because the photon energy exceeds the $S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ resonance energy (see Fig.
 243 4).

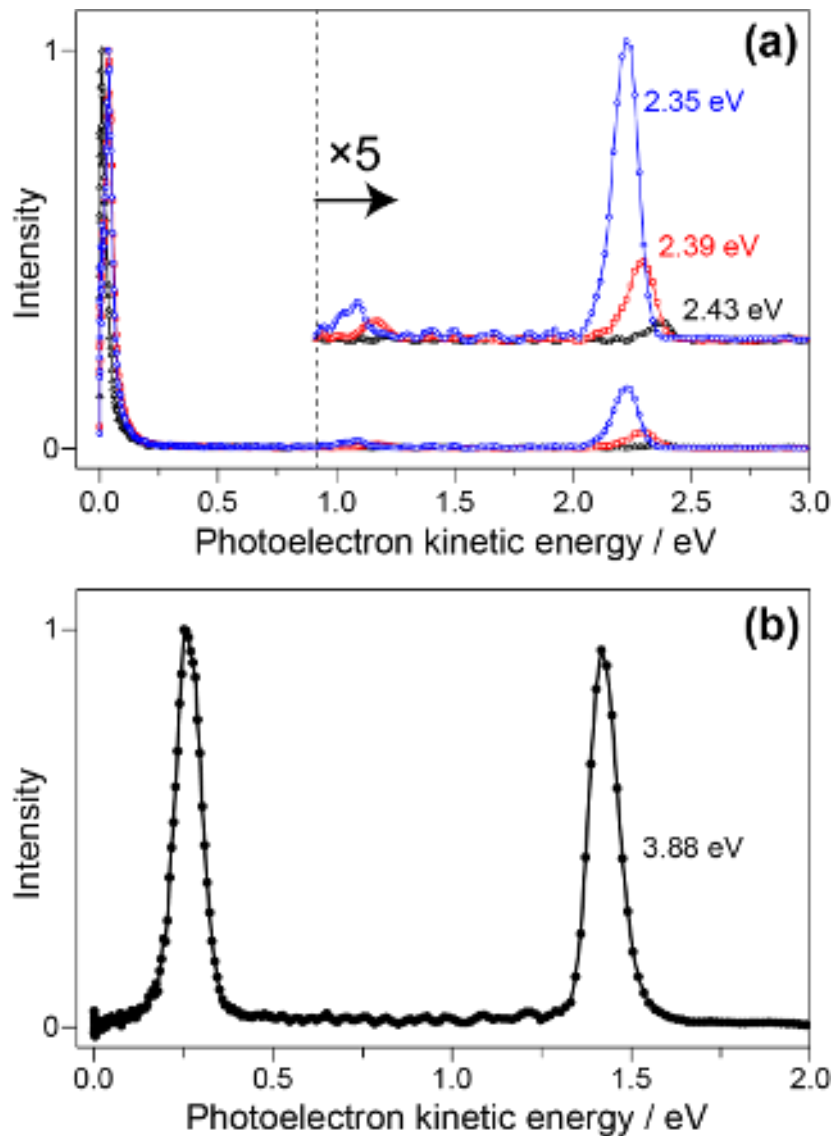


Figure 6. (a) Photoelectron spectra of Ag_3^- obtained by the detachment laser at 2.35 (blue circles), 2.39 (red squares), and 2.43 eV (black triangles). (b) A photoelectron spectrum of Ag_3^- obtained at 3.88 eV. The intensity is in arbitrary units.

245 First, we discuss the origins of the 0-eV bands. One should note that the 0-eV band profiles of the
246 2.35- and 2.39-eV spectra are different from that of the 2.43-eV spectrum, as manifested in Fig. S7 in
247 Supplementary Material magnifying the 0-eV bands of Fig. 6(a). These features in the spectral profiles
248 suggest that the 0-eV photoelectrons upon 2.35- and 2.39-eV irradiation are yielded via detachment
249 processes different from that for the 2.43-eV photodetachment case; the latter allows direct one-photon
250 detachment because the photon energy is just at the VDE. Here, one should further note that the 0-eV
251 signals upon 2.35- and 2.39-eV irradiation are generated in a one-photon process as well, as confirmed
252 by the measurement of the laser-power dependence of their intensities (see the inset of Fig. S7),
253 although the photon energy is slightly below the VDE. This odd behavior may be explained as follows:
254 since vibrationally-hot Ag_3^- anions are prepared in our cluster source, one-photon absorption from
255 vibrationally-hot $S_0(^1\Sigma_g^+)$ state into vibrationally-hot $S_1(^1\Sigma_u^+)$ that is energetically above the VDE
256 become possible. Thus, we suppose that the 0-eV components in the 2.35- and 2.39-eV spectra are due
257 to autodetachment from such vibrationally-hot $S_1(^1\Sigma_u^+)$ states into the $D_0(^2\Sigma_u^+) + e^-$ continuum via one-
258 photon processes.

259 Figure 6(b) shows a photoelectron spectrum obtained by one-photon detachment at 3.88 eV, where
260 two peaks assignable to the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ and $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transitions are
261 observed. The intensities of the two peaks are almost comparable, which is in contrast to Fig. 6(a), i.e.,
262 two-photon processes. In one-photon detachment, both the transitions are allowed in terms of the frozen-
263 orbital approximation, where only one electron is removed upon photodetachment without altering the
264 configuration of the rest of the electrons (see the electron configurations in Figs. 3 and 5). In two-photon
265 detachment, on the other hand, this approximation readily implies that the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_1(^1\Sigma_u^+) \leftarrow$
266 $S_0(^1\Sigma_g^+)$ process corresponding to the removal of σ_g^* electron from $S_1(^1\Sigma_u^+)$ is allowed, whereas the
267 $D_1(^2\Sigma_g^+) + e^- \leftarrow S_1(^1\Sigma_u^+) \leftarrow S_0(^1\Sigma_g^+)$ process is forbidden, which requires rearrangement of two electrons
268 upon photodetachment. This accounts for why the $D_1(^2\Sigma_g^+)$ band around 1 eV appears so weakly

269 compared with the $D_0(^2\Sigma_u^+)$ band in Fig. 6(a). Therefore, our experimental result qualitatively supports
 270 that the leading electronic configuration of the $S_1(^1\Sigma_u^+)$ state is $(\sigma_g)^2(\sigma_u)^1(\sigma_g^*)^1$ as shown in Fig. 3.
 271 Similar arguments were demonstrated in time-resolved photoelectron spectroscopy for isolated
 272 molecules,^{33,34} where resonantly-enhanced multiphoton ionization via their excited electronic states was
 273 employed. Relative intensities of the observed photoelectron signals were discussed by considering the
 274 leading electronic configurations of the transient electronic states.

Table 1. Photoelectron kinetic energies expected for two-photon detachment from $S_0(^1\Sigma_g^+)$ to $D_0(^2\Sigma_u^+)$ and $D_1(^2\Sigma_g^+)$ states with 2.35- and 2.39-eV photons along with the observed peak positions in Fig. 6(a).

Two-photon energy / eV	Expected photoelectron kinetic energies / eV ^a		Obsd. peak position / eV
	$D_0(^2\Sigma_u^+)$	$D_1(^2\Sigma_g^+)$	
4.69	2.26	1.07	2.22 / 1.09
4.79	2.36	1.17	2.30 / 1.18

^a Obtained from the two-photon energies (4.69 or 4.79 eV) and the electron binding energies for the $D_0(^2\Sigma_u^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ and the $D_1(^2\Sigma_g^+) + e^- \leftarrow S_0(^1\Sigma_g^+)$ transitions (2.43 and 3.62 eV, respectively).

275

276 IV. CONCLUSION

277 We have presented photoelectron imaging spectroscopy of Ag_3^- in the $S_0(^1\Sigma_g^+)$ and $S_1(^1\Sigma_u^+)$ states.
 278 Our novel photoelectron imaging apparatus using a 100-kHz tunable fs laser system has enabled fast
 279 data acquisition of energy dependence of LF-PADs from the outermost two orbitals, σ_u (HOMO) and σ_g
 280 (HOMO-1) of Ag_3^- . Highly energy-dependent LF-PAD was obtained for the σ_u orbital in the PKE
 281 range of 0 – 1.57 eV. An isotropic LF-PAD ($\beta \sim 0$) was observed at the photodetachment threshold,
 282 which exemplifies the Wigner threshold law, whereas the LF-PAD gradually became anisotropic with
 283 more photoelectrons perpendicular to the laser polarization (i.e., negative anisotropy) as the PKE
 284 increased. The corresponding β parameter exhibited a minimum (-0.4) at 0.46 eV, and thereafter it

285 increased up to ~ 0.6 at 1.57 eV, with a small dip discernible at 1.2 – 1.3 eV, suggesting autodetachment
286 via bound electronic state(s) embedded in the $D_0(^2\Sigma_u^+) + e^-$ continuum. On the other hand, the
287 photodetachment from the σ_g orbital exhibited a strong positive anisotropy ($\beta \sim 1$) in 0 – 0.39 eV. The
288 simulations of LF-PADs by the ezDyson software qualitatively explained the contrasted trends of the
289 energy-dependent β values, where the photoelectron partial waves with gerade / ungerade symmetries
290 are responsible for the LF-PADs for the σ_u / σ_g orbitals, respectively.

291 Taking advantage of fs pulses from the 100-kHz tunable light source, we also obtained photoelectron
292 images by two-photon detachment via the $S_1(^1\Sigma_u^+)$ state of Ag_3^- . The relative band intensities for the
293 $D_0(^2\Sigma_u^+)$ and $D_1(^2\Sigma_g^+)$ final states reflected the leading electronic configuration of the transient state,
294 which eventually decays into vibrationally hot $S_0(^1\Sigma_g^+)$ state and/or undergoes Ag–Ag bond dissociation
295 in a finite lifetime. We plan to explore such decay dynamics by applying the present photoelectron
296 imaging spectroscopy to time-resolved measurements.

297

298

299 SUPPLEMENTARY MATERIAL

300 See the supplementary material for details on acquisition and analysis of photoelectron images, error
301 estimation of anisotropy parameters, and experimental and calculated results that support the discussion
302 of the main text.

303

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311

312 AUTHOR DECLARATIONS

313 Conflict of Interest

314 The authors have no conflicts to disclose.

315 DATA AVAILABILITY

316 The data that support the findings of the present study are available on request from the corresponding
317 author, T. H.

318

319 AUTHOR CONTRIBUTIONS

320 **Yuta Suzuki:** Formal analysis (lead); Investigation (lead); Methodology (supporting); Writing - original
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322 Investigation (supporting); Methodology (supporting); Writing - review & editing (equal). **Kazuaki**
323 **Matsumoto:** Formal analysis (supporting); Investigation (supporting); Methodology (supporting);
324 Writing - review & editing (equal). **Yuta Ushiki:** Formal analysis (supporting); Investigation
325 (supporting); Methodology (supporting); Writing - review & editing (equal). **Yuma Aoki:** Formal
326 analysis (supporting); Investigation (supporting); Writing - review & editing (equal). **Akira Terasaki:**
327 Funding acquisition (equal); Supervision (lead); Writing - review and editing (equal). **Takuya Horio:**
328 Conceptualization (lead); Formal analysis (supporting); Funding acquisition (equal); Investigation
329 (supporting); Methodology (lead); Project administration (lead); Writing - original draft (equal);
330 Writing - review & editing (equal).

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333 REFERENCES

- 334 ¹ H. Basch, *J. Am. Chem. Soc.* **103**(16), 4657–4663 (1981).
- 335 ² D.M. Lindsay, L. Chu, Y. Wang, and T.F. George, *J. Chem. Phys.* **87**(3), 1685–1689 (1987).
- 336 ³ C.W. Bauschlicher, S.R. Langhoff, and H. Partridge, *J. Chem. Phys.* **91**(4), 2412–2419 (1989).
- 337 ⁴ V. Bonačić-Koutecký, L. Češpiva, P. Fantucci, J. Pittner, and J. Koutecký, *J. Chem. Phys.* **100**(1),
338 490–506 (1994).
- 339 ⁵ J. Ho, K.M. Ervin, and W.C. Lineberger, *J. Chem. Phys.* **93**(10), 6987–7002 (1990).
- 340 ⁶ G.F. Gantefor, D.M. Cox, and A. Kaldor, *J. Chem. Phys.* **93**(11), 8395–8396 (1990).
- 341 ⁷ H. Handschuh, C. Cha, P.S. Bechthold, G. Ganteför, and W. Eberhardt, *J. Chem. Phys.* **102**(16), 6406–
342 6422 (1995).
- 343 ⁸ S. Wolf, G. Sommerer, S. Rutz, E. Schreiber, T. Leisner, L. Wöste, and R.S. Berry, *Phys. Rev. Lett.*
344 **74**(21), 4177–4180 (1995).
- 345 ⁹ D.W. Boo, Y. Ozaki, L.H. Andersen, and W.C. Lineberger, *J. Phys. Chem. A* **101**(36), 6688–6696
346 (1997).
- 347 ¹⁰ S. Kawamura, M. Yamaguchi, S. Kono, M. Arakawa, T. Yasuike, T. Horio, and A. Terasaki, *J. Phys.*
348 *Chem. A* **127**(29), 6063–6070 (2023).
- 349 ¹¹ T. Horio, T. Nishizato, Y. Suzuki, K. Matsumoto, and A. Terasaki, *J. Chem. Phys.* **162**(2), 026101
350 (2025).
- 351 ¹² S. Gozem, A.O. Gunina, T. Ichino, D.L. Osborn, J.F. Stanton, and A.I. Krylov, *J. Phys. Chem. Lett.*
352 **6**(22), 4532–4540 (2015).
- 353 ¹³ S. Gozem, and A.I. Krylov, *WIREs Computational Molecular Science* **12**(2), (2022).
- 354 ¹⁴ T. Horio, K. Minamikawa, T. Nishizato, H. Hashimoto, K. Matsumoto, M. Arakawa, and A. Terasaki,
355 *Rev. Sci. Instrum.* **93**(8), 083302 (2022).
- 356 ¹⁵ D.A. Horke, G.M. Roberts, J. Lecointre, and J.R.R. Verlet, *Rev. Sci. Instrum.* **83**(6), 063101 (2012).
- 357 ¹⁶ A.T.J.B. Eppink, and D.H. Parker, *Rev. Sci. Instrum.* **68**(9), 3477–3484 (1997).
- 358 ¹⁷ K. Minamikawa, T. Nishizato, H. Hashimoto, K. Matsumoto, M. Arakawa, T. Horio, and A. Terasaki,
359 *J. Phys. Chem. Lett.* **14**(17), 4011–4018 (2023).
- 360 ¹⁸ Y. Suzuki, K. Matsumoto, R. Nomi, M. Arakawa, T. Horio, and A. Terasaki, *J. Phys. Chem. Lett.*
361 **15**(16), 4327–4332 (2024).
- 362 ¹⁹ G.M. Roberts, J.L. Nixon, J. Lecointre, E. Wrede, and J.R.R. Verlet, *Rev. Sci. Instrum.* **80**(5), 053104
363 (2009).
- 364 ²⁰ E. Epifanovsky, A.T.B. Gilbert, X. Feng, J. Lee, Y. Mao, N. Mardirossian, P. Pokhilko, A.F. White,
365 M.P. Coons, A.L. Dempwolff, Z. Gan, D. Hait, P.R. Horn, L.D. Jacobson, I. Kaliman, J. Kussmann,
366 A.W. Lange, K.U. Lao, D.S. Levine, J. Liu, S.C. McKenzie, A.F. Morrison, K.D. Nanda, F. Plasser,
367 D.R. Rehn, M.L. Vidal, Z.-Q. You, Y. Zhu, B. Alam, B.J. Albrecht, A. Aldossary, E. Alguire, J.H.
368 Andersen, V. Athavale, D. Barton, K. Begam, A. Behn, N. Bellonzi, Y.A. Bernard, E.J. Berquist,
369 H.G.A. Burton, A. Carreras, K. Carter-Fenk, R. Chakraborty, A.D. Chien, K.D. Closser, V. Cofer-
370 Shabica, S. Dasgupta, M. de Wergifosse, J. Deng, M. Diedenhofen, H. Do, S. Ehlert, P.-T. Fang, S.
371 Fatehi, Q. Feng, T. Friedhoff, J. Gayvert, Q. Ge, G. Gidofalvi, M. Goldey, J. Gomes, C.E. González-
372 Espinoza, S. Gulania, A.O. Gunina, M.W.D. Hanson-Heine, P.H.P. Harbach, A. Hauser, M.F. Herbst,

- 373 M. Hernández Vera, M. Hodecker, Z.C. Holden, S. Houck, X. Huang, K. Hui, B.C. Huynh, M.
374 Ivanov, Á. Jász, H. Ji, H. Jiang, B. Kaduk, S. Kähler, K. Khistyayev, J. Kim, G. Kis, P. Klunzinger, Z.
375 Koczor-Benda, J.H. Koh, D. Kosenkov, L. Koulias, T. Kowalczyk, C.M. Krauter, K. Kue, A. Kunitsa,
376 T. Kus, I. Ladjánszki, A. Landau, K. V. Lawler, D. Lefrancois, S. Lehtola, R.R. Li, Y.-P. Li, J. Liang,
377 M. Lieenthal, H.-H. Lin, Y.-S. Lin, F. Liu, K.-Y. Liu, M. Loipersberger, A. Luenser, A. Manjanath,
378 P. Manohar, E. Mansoor, S.F. Manzer, S.-P. Mao, A. V. Marenich, T. Markovich, S. Mason, S.A.
379 Maurer, P.F. McLaughlin, M.F.S.J. Menger, J.-M. Mewes, S.A. Mewes, P. Morgante, J.W. Mullinax,
380 K.J. Oosterbaan, G. Paran, A.C. Paul, S.K. Paul, F. Pavošević, Z. Pei, S. Prager, E.I. Proynov, Á. Rák,
381 E. Ramos-Cordoba, B. Rana, A.E. Rask, A. Rettig, R.M. Richard, F. Rob, E. Rossomme, T. Scheele,
382 M. Scheurer, M. Schneider, N. Sergueev, S.M. Sharada, W. Skomorowski, D.W. Small, C.J. Stein,
383 Y.-C. Su, E.J. Sundstrom, Z. Tao, J. Thirman, G.J. Tornai, T. Tsuchimochi, N.M. Tubman, S.P.
384 Veccham, O. Vydrov, J. Wenzel, J. Witte, A. Yamada, K. Yao, S. Yeganeh, S.R. Yost, A. Zech, I.Y.
385 Zhang, X. Zhang, Y. Zhang, D. Zuev, A. Aspuru-Guzik, A.T. Bell, N.A. Besley, K.B. Bravaya, B.R.
386 Brooks, D. Casanova, J.-D. Chai, S. Coriani, C.J. Cramer, G. Cserey, A.E. DePrince, R.A. DiStasio,
387 A. Dreuw, B.D. Dunietz, T.R. Furlani, W.A. Goddard, S. Hammes-Schiffer, T. Head-Gordon, W.J.
388 Hehre, C.-P. Hsu, T.-C. Jagau, Y. Jung, A. Klamt, J. Kong, D.S. Lambrecht, W. Liang, N.J. Mayhall,
389 C.W. McCurdy, J.B. Neaton, C. Ochsenfeld, J.A. Parkhill, R. Peverati, V.A. Rassolov, Y. Shao, L. V.
390 Slipchenko, T. Stauch, R.P. Steele, J.E. Subotnik, A.J.W. Thom, A. Tkatchenko, D.G. Truhlar, T. Van
391 Voorhis, T.A. Wesolowski, K.B. Whaley, H.L. Woodcock, P.M. Zimmerman, S. Faraji, P.M.W. Gill,
392 M. Head-Gordon, J.M. Herbert, and A.I. Krylov, *J. Chem. Phys.* **155**(8), 084801 (2021).
- 393 ²¹ K.A. Peterson, and C. Pizzarini, *Theor. Chem. Acc.* **114**(4–5), 283–296 (2005).
- 394 ²² B.P. Pritchard, D. Altarawy, B. Didier, T.D. Gibson, and T.L. Windus, *J. Chem. Inf. Model* **59**(11),
395 4814–4820 (2019).
- 396 ²³ J.P. Perdew, *Phys. Rev. B* **33**(12), 8822–8824 (1986).
- 397 ²⁴ A.D. Becke, *Phys. Rev. A* **38**(6), 3098–3100 (1988).
- 398 ²⁵ P.J. Hay, and W.R. Wadt, *J. Chem. Phys.* **82**(1), 270–283 (1985).
- 399 ²⁶ J. Cooper, and R.N. Zare, *J. Chem. Phys.* **48**(2), 942–943 (1968).
- 400 ²⁷ E.P. Wigner, *Phys. Rev.* **73**(9), 1002–1009 (1948).
- 401 ²⁸ R. Mabbs, E.R. Grumblin, K. Pichugin, and A. Sanov, *Chem. Soc. Rev.* **38**(8), 2169 (2009).
- 402 ²⁹ A. Sanov, *Annu. Rev. Phys. Chem.* **65**(1), 341–363 (2014).
- 403 ³⁰ V. Bonačić-Koutecký, P. Fantucci, and J. Koutecký, *J. Chem. Phys.* **93**(6), 3802–3825 (1990).
- 404 ³¹ C. Bartels, C. Hock, R. Kuhnen, and B. von Issendorff, *J. Phys. Chem. A* **118**(37), 8270–8276 (2014).
- 405 ³² K.M. McHugh, J.G. Eaton, G.H. Lee, H.W. Sarkas, L.H. Kidder, J.T. Snodgrass, M.R. Manaa, and
406 K.H. Bowen, *J. Chem. Phys.* **91**(6), 3792–3793 (1989).
- 407 ³³ M. Schmitt, S. Lochbrunner, J.P. Shaffer, J.J. Larsen, M.Z. Zgierski, and A. Stolow, *J. Chem. Phys.*
408 **114**(3), 1206–1213 (2001).
- 409 ³⁴ T. Horio, R. Spesyvtsev, K. Nagashima, R.A. Ingle, Y. Suzuki, and T. Suzuki, *J. Chem. Phys.* **145**(4),
410 044306 (2016).
- 411