

Photoelectron Imaging Signature for Selective Formation of Icosahedral Anionic Silver Cages Encapsulating Group 5 Elements: $M@Ag_{12}^-$ (M = V, Nb, and Ta)

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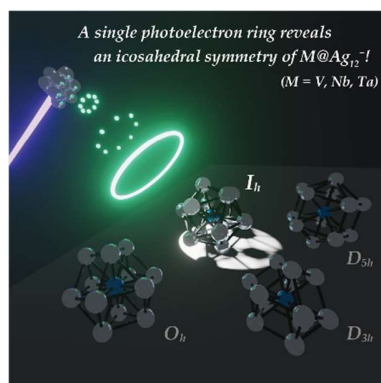
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Abstract

An assembly of thirteen atoms can form highly symmetric architectures like those belonging to D_{3h} , O_h , D_{5h} , and I_h point groups. Here, using photoelectron imaging spectroscopy in combination with density functional theory (DFT) calculations, we present a simple yet convincing experimental signature for selective formation of icosahedral cages of anionic silver clusters encapsulating a dopant atom of group 5 elements: $M@Ag_{12}^-$ ($M = V, Nb, \text{ and } Ta$). Their photoelectron images obtained at 4 eV closely resemble one another: only a single ring is observed, which is assignable to photodetachment signals from a five-fold degenerate superatomic 1D electronic shell in the $1S^21P^61D^{10}$ configuration of valence electrons. The perfect degeneracy represents an unambiguous fingerprint of an icosahedral symmetry, which would otherwise be lifted in all the other structural isomers. DFT calculations confirm that I_h forms are the most stable and that D_{5h} , O_h , and D_{3h} structures are not found even in metastable states.

TOC GRAPHICS



KEYWORDS

Icosahedron, Structural determination, Geometric isomer selectivity, Metal clusters, Superatoms, Group theory, Photoelectron imaging

Twelve atoms can build up highly symmetric cages like those belonging to D_{3h} , O_h , D_{5h} , and I_h point groups, suggesting that an assembly of thirteen atoms, i.e., one at the center with the other twelve in the outer layer, is expected to be a distinctive nanocluster. Especially, an icosahedron is the best known as an iconic structure in the finite size regime,¹ where a magic number of $n = 13$ was observed in the mass spectra of rare gas clusters, R_n ($R = \text{Ar}^2$ and Xe^3), implying that R_{13} is the smallest size of so-called Mackay icosahedra with concentric shell structures.⁴ The aluminum tridecamer anion, Al_{13}^- , is one of the most well-known metal aggregates with I_h symmetry that has been inspiring a considerable body of work on so-called *superatoms*.^{5,6} Icosahedral forms also constitute novel platforms for synthesizing ligand-protected gold and silver superatoms,⁷ leading to a variety of promising applications based on atomically-precise metal nanoclusters.

Such highly symmetric architectures are also formed by an assembly of twelve atoms, A_{12} , encapsulating a foreign atom, X, at the center of the A_{12} cage, i.e., $X@A_{12}$. The diversity of the combinations of A and X has stimulated a bunch of experimental and theoretical explorations for discovering $X@A_{12}$, which are summarized in a part of a recent comprehensive review by Zhao et al.⁸ Among them, X-doped coinage metal clusters (i.e., $A = \text{Cu}$, Ag , and Au) have been attracting much attention.

Pyykkö and Runeberg⁹ explored the most stable structure of $\text{W}@Au_{12}$ using density functional theory (DFT), where they predicted that $\text{W}@Au_{12}$ is in I_h symmetry with eighteen valence electrons ($12 \times \text{Au } 6s^1 + \text{W } 6s^2 5d^4$) delocalized over the metal framework with the spin multiplicity of singlet. This suggests that the jellium model,¹⁰ which is known to well describe valence electrons in clusters of monovalent metals (Na_n , Au_n , etc.), can also be applied to this bimetallic cluster; the valence electrons occupy atomic-like electronic shells of 1S, 1P, 1D, 2S, etc.

so that electronic-shell closure with $1S^21P^61D^{10}$ configuration is realized in $W@Au_{12}$. Photoelectron spectroscopy (PES) of its anion, $Au_{12}W^-$, performed by Li et al.¹¹ observed a sharp peak at the vertical detachment energy (VDE) as low as 2.08 eV, implying that the structural deformation upon photodetachment is minimal. Although the experiment did not directly probe the neutral species, the observation strongly suggests that the excess electron is weakly attached on a rigid icosahedral core of $W@Au_{12}$.

Here, we focus on $Ag_{12}M^-$ ($M = V, Nb, \text{ and } Ta$), which are all expected to be valence isoelectronic to $W@Au_{12}$; $Ag_{12}M^-$ ($M = V, Nb, \text{ and } Ta$) have commonly 18 valence electrons including the excess charge since the valence electron configurations of Ag, V, Nb and Ta atoms are $5s^1$, $4s^23d^3$, $5s^14d^4$ and $6s^25d^3$, respectively. The present study was inspired by our recent experiment on reactivities of Ag_nV^- with molecular oxygen,¹² where the size-dependent pseudo first-order reaction rate constant was revealed to exhibit a local minimum at $n = 12$, indicating that $Ag_{12}V^-$ is highly stable against O_2 exposure. This readily implies that the closed electronic shell structure of $1S^21P^61D^{10}$ is realized in $Ag_{12}V^-$ as well. Although information on the symmetry of the cluster's geometry was not obtained through the reactivity experiment, our DFT calculations have predicted that the doped cluster has I_h symmetry, which motivated us to apply anion PES by using our novel photoelectron imaging apparatus that enables fast acquisition of photoelectron images under space-charge free conditions.¹³ As explained later, photodetachment signals from a five-fold degenerate 1D electronic shell can be an unambiguous fingerprint for I_h symmetry of $V@Ag_{12}^-$. This point has not been examined before. The study is extended also to $Ag_{12}Nb^-$ and $Ag_{12}Ta^-$ to explore if they are in icosahedral symmetry. After presenting our results, comparison to the anion PES studies for $Au_{12}M^-$ ($M = V, Nb, \text{ and } Ta$) by Zhai et al.,¹⁴ which also have 18 valence electrons, will be made by addressing possible geometric isomers in both systems.

Experimental results are presented in Figs. 1(a) – (c), which show two-dimensional (2D) projections of three-dimensional (3D) distributions for photoelectrons detached from Ag_{12}M^- ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$), respectively, by linearly-polarized, ultraviolet (UV) femtosecond (fs) laser pulses at 310 nm (4.00 eV). From these images, we have obtained 2D slices of the original 3D photoelectron distributions, which are presented in Figs. 1(d) – (f) correspondingly. These 2D-slice images closely resemble one another, indicating that they are indeed valence iso-electronic systems. Most importantly, the 2D slice images all exhibit a *single* ring.

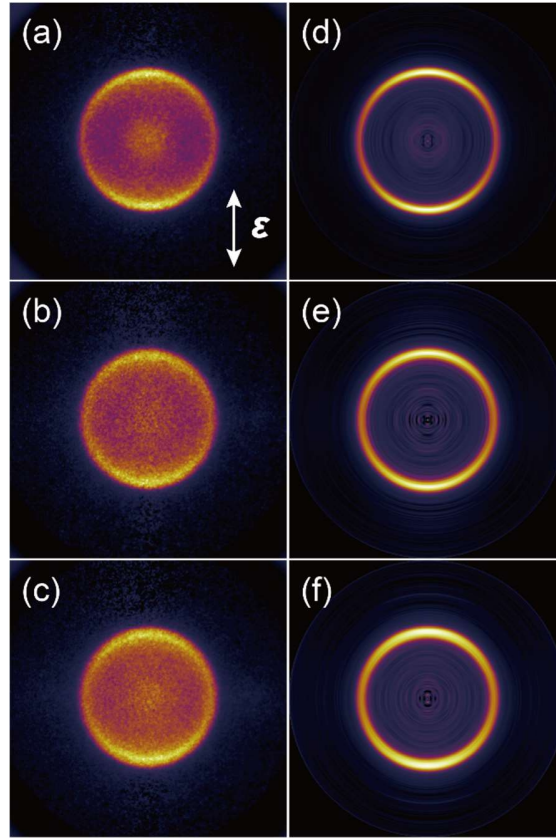
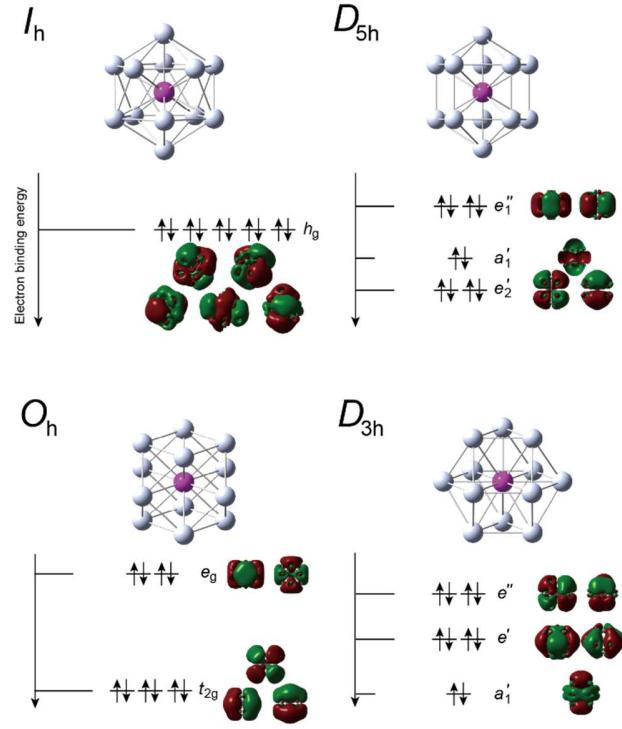


Figure 1. 2D projections (left panels) and 2D slices (right panels) of the 3D photoelectron distributions obtained for Ag_{12}V^- ((a) and (d)), $\text{Ag}_{12}\text{Nb}^-$ ((b) and (e)), and $\text{Ag}_{12}\text{Ta}^-$ ((c) and (f)). The direction of the polarization vector, ϵ , of the 310-nm fs UV pulses is indicated by a double arrow in (a).

According to the jellium model, the valence electron configurations of Ag_{12}M^- ($\text{M} = \text{V}$, Nb, and Ta) are predicted to be $1\text{S}^21\text{P}^61\text{D}^{10}$, where photodetachment from the outermost 1D electronic shell yields photoelectron signals with the lowest electron binding energy. Herein, we discuss how the 1D electronic shell, i.e., the highest occupied molecular orbital (HOMO), behaves under I_h , D_{5h} , O_h , and D_{3h} structures. As shown in Fig. 2, under I_h point group, the 1D electronic shell has five-fold degeneracy with h_g symmetry, whereas it splits into $e''_1 + a'_1 + e'_2$, $e_g + t_{2g}$, and $e'' + e' + a'_1$ orbitals under D_{5h} , O_h , and D_{3h} point groups, respectively. In the zeroth order approximation, where Jahn–Teller distortion and spin–orbit coupling in the neutral states are both ignored, the photodetachment signal from h_g , $e''_1 + a'_1 + e'_2$, $e_g + t_{2g}$, and $e'' + e' + a'_1$ orbitals should yield one, three, two, and three bands, respectively. Turning to the top panels of Figs. 3(a) – (c) that present experimental photodetachment spectra for Ag_{12}M^- ($\text{M} = \text{V}$, Nb, and Ta), a *single* band is observed; it corresponds to the single ring in each image of Figs. 1(a) – (c). Thus, our results indicate the first case. This point is further discussed in spectral simulation shown later.

It should be noted that the observation of the single band for each spectrum is rather surprising, as photodetachment spectra for metal cluster anions composed of more than ten atoms are generally congested in the electron binding energy range from 0 to 4 eV; see refs.^{14–16}, for example. Least-squares fitting to the observed photodetachment spectra was performed to characterize their overall spectral profiles. The dashed lines in the top panels of Figs. 3(a) – (c) are the best-fit curves using Lorentzian functions. Notably, tails in both the lower and higher energy regions of the single bands are likely due to the instrumental response of our setup, because such tails are also discernible in the photodetachment spectrum of Ag^- (see Fig. S1 in Supporting Information). In addition to these tails, minor components are observed around 4 eV in the experimental data. These are presumably due to residuals in the background subtraction, which

114 corresponds to weak signals in the central part of the images in Figs. 1(a) – (c) (see
 115 EXPERIMENTAL METHODS). The analysis indicates that the observed photodetachment
 116 spectra for Ag_{12}M^- ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$) are almost symmetric to the peak energy.



117

118 **Figure 2.** Possible highly-symmetric structures of Ag_{12}M^- ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$) with their splitting
 119 schemes of the 1D electronic shells. The isosurface plots are of $\text{Ag}_{12}\text{Ta}^-$, where Kohn–Sham
 120 orbitals are shown with the isovalue of 0.01. Photodetachment signals expected for the
 121 corresponding structures are also shown schematically.

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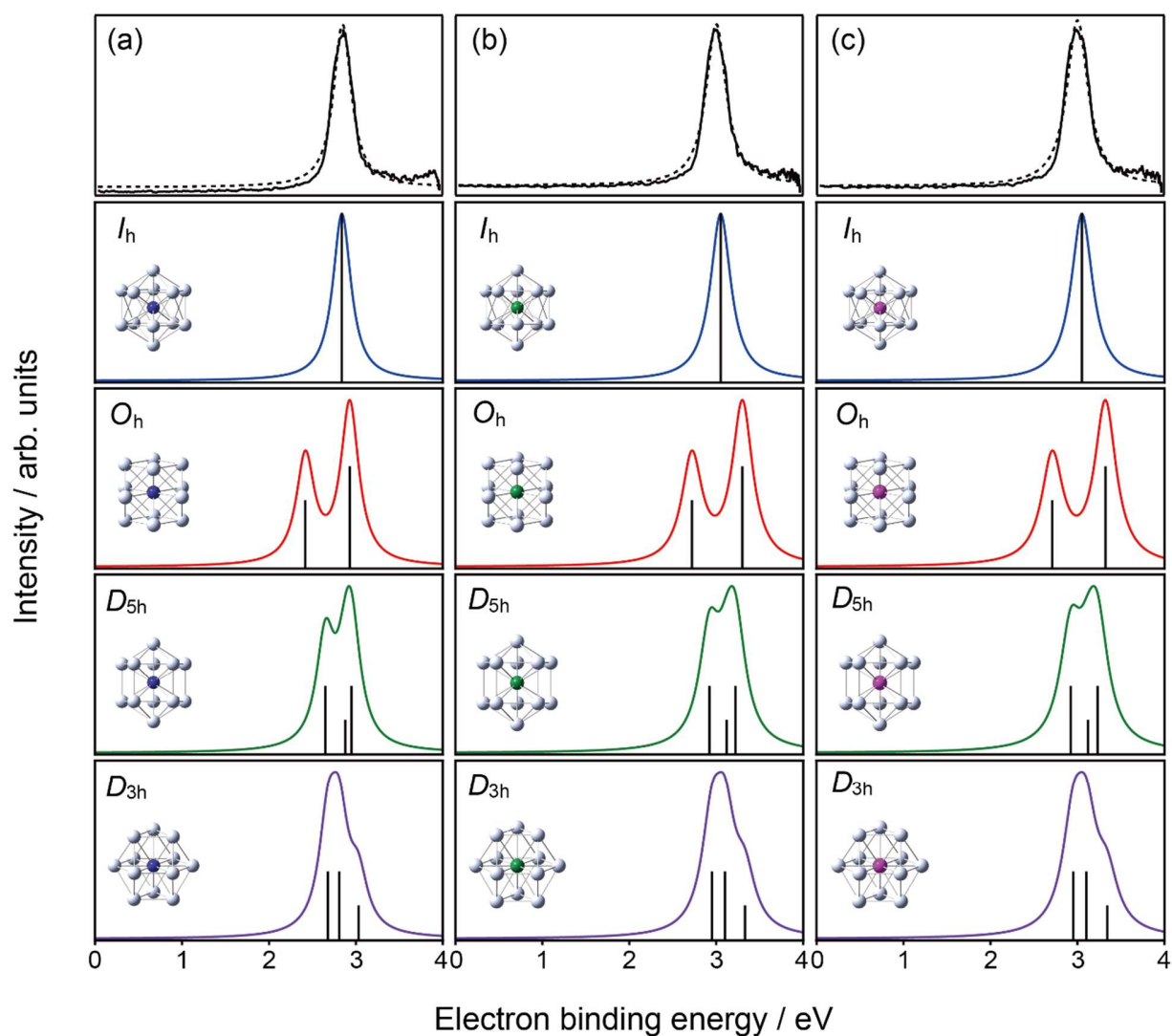


Figure 3. Photodetachment spectra (solid lines in the top panels) obtained for (a) Ag_{12}V^- , (b) $\text{Ag}_{12}\text{Nb}^-$, and (c) $\text{Ag}_{12}\text{Ta}^-$ with a detachment laser at 310 nm (4.00 eV). The best-fit curves using Lorentzian functions are shown with dashed lines. Simulated spectral profiles assuming I_h , D_{5h} , O_h , and D_{3h} structures, which are obtained from discrete spectra shown with vertical sticks, are presented in the lower panels (see the text).

We performed DFT calculations for exploring the most stable geometries of Ag_{12}M^- ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$) starting from 80 initial geometries of endohedrally- or exohedrally-doped structures, the former of which included I_h , D_{5h} , O_h , and D_{3h} structures. By referring to the theoretical

investigation on $\text{Ag}_n\text{V}^{+/0}$ ($4 \leq n \leq 15$) by Medel et al.,¹⁷ the spin multiplicity was restricted to singlet and triplet. The DFT calculations were conducted by the Gaussian 16 package¹⁸ using possible combinations of BP86^{19,20} and PBE/PBE²¹ functionals with SDD^{22,23} and LanL2DZ²⁴ basis sets. We found, for all the combinations of functionals and basis sets examined, that $\text{M}@\text{Ag}_{12}^-$ ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$) with I_h symmetry was the most stable with the spin multiplicity of singlet and that *no* local minima were obtained for D_{5h} , O_h , and D_{3h} structures. We then evaluated their VDEs by calculating the total energy difference between Ag_{12}M^- and the corresponding neutrals, Ag_{12}M , in their ground electronic states that have exactly the same geometries as anionic Ag_{12}M^- . The results obtained using BP86/SDD level are summarized in Table 1 along with the experimental values. The calculated VDEs for $\text{M}@\text{Ag}_{12}^-$ ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$) with I_h symmetry are in excellent agreement with the experimental ones. Although the D_{5h} , O_h , and D_{3h} structures are not in local minima, we calculated VDEs also for these structures in the same manner as mentioned above, which are presented in Table 1 as well; however, the agreement is worse. The VDEs calculated by the other combinations of functionals and basis sets are summarized in Table S1 of Supporting Information.

Table 1. Simulated VDEs for Ag_{12}M^- ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$) with I_h , D_{5h} , O_h , and D_{3h} symmetries at the BP86/SDD level along with the experimental VDEs and their relative total energies (in eV units) shown in the parentheses.

Vertical detachment energy (VDE) / eV					
	Expt.	Calc.			
		I_h	D_{5h}^a	O_h^a	D_{3h}^a
Ag_{12}V^-	2.88 ± 0.02	2.84 (0)	2.65 (0.68)	2.42 (0.69)	2.68 (0.75)
$\text{Ag}_{12}\text{Nb}^-$	3.02 ± 0.02	3.05 (0)	2.92 (0.41)	2.72 (0.45)	2.95 (0.45)
$\text{Ag}_{12}\text{Ta}^-$	3.00 ± 0.04	3.05 (0)	2.92 (0.41)	2.71 (0.47)	2.95 (0.46)

^a Saddle points (no local minima were obtained with these symmetries).

To make our conclusion further convincing, we simulated photoelectron spectra of $\text{M}@\text{Ag}_{12}^-$ with I_h , D_{5h} , O_h , and D_{3h} symmetries, where we utilized generalized Koopmans' theorem²⁵ to evaluate the electron binding energies for photodetachment signals from h_g , $e''_1 + a'_1 + e'_2$, $e_g + t_{2g}$, and $e'' + e' + a'_1$ orbitals. The evaluation yielded stick spectra corresponding to photodetachment energies from each orbital with their relative intensities proportional to the number of electrons occupying the orbital, as shown in Fig. 3. The stick spectra thus obtained were broadened with a Lorentzian function with a full width at half maximum (FWHM) of 0.25, 0.28, and 0.30 eV for $\text{M}@\text{Ag}_{12}^-$ ($\text{M} = \text{V}, \text{Nb}, \text{and Ta}$), respectively, which were obtained from the least-squares fitting analysis mentioned in Fig. 3, to account for the spectral broadening in the experiment; the spectral shape is determined by the instrumental function (see Fig. S1), the Franck–Condon factor in the photodetachment process, and the spin–orbit coupling in the neutral states. The photoelectron spectra thus simulated show that O_h and D_{5h} isomers both exhibit doublet

peaks. The ones simulated for D_{3h} structure are found to be asymmetric owing to the photodetachment signal from the a'_1 orbital. Although further broadening makes their spectral profiles symmetric, such spectra are too broad to reproduce the observed profiles. Thus, it is only the I_h structure that can fully account for the experimental results. Electron binding energies obtained by the other combinations of functionals and basis sets are summarized in Table S2 in Supporting Information. The results are all consistent with the present one obtained by BP86/SDD in terms of the splitting patterns of the 1D orbitals.

In the present study, we have succeeded in isomer-free production of $M@Ag_{12}^-$ ($M = V$, Nb, and Ta) with I_h symmetry, which is contrasted to the cases of gold cages, $M@Au_{12}^-$ ($M = V$, Nb, and Ta) investigated by Zhai et al.¹⁴ The photodetachment spectra observed for the M-doped gold cluster anions showed a main band at around 3.8 eV corresponding to the single band observed for $M@Ag_{12}^-$ ($M = V$, Nb, and Ta) in the present study. While this main band is assignable to icosahedral structures of $M@Au_{12}^-$, additional bands and broad backgrounds superimposed on the main band were noticeable in each spectrum for $M@Au_{12}^-$ ($M = V$, Nb, and Ta). The authors speculated that the spectra would have been contaminated with photodetachment signals from anionic species with close mass-to-charge ratio, such as $Au_xM_yO_z^-$ and $Au_xM_y^-$, and close-lying structural isomers with D_{5h} and O_h symmetries. The co-existence of the D_{5h} and O_h isomers was indeed suggested by their DFT investigations, where these structural isomers were found to be metastable.

Summarizing this work, we have obtained photoelectron spectra of the group 5 metal-doped silver dodecamer anions, $Ag_{12}M^-$ ($M = V$, Nb, and Ta). Each spectrum commonly exhibits only a single and nearly symmetric band, providing unambiguous experimental evidence that the present $Ag_{12}M^-$ clusters have highly symmetric I_h geometries. Our DFT calculations revealed that

the I_h forms were indeed the most stable for all the clusters and that the possible highly-symmetric structures with D_{5h} , O_h , and D_{3h} point groups were not found even in metastable states. The photodetachment spectra simulated for icosahedral $M@Ag_{12}^-$ ($M = V, Nb$, and Ta) were in excellent agreement with the experimental ones, fully supporting the above discovery.

$M@Ag_{12}^-$ ($M = V, Nb$, and Ta) discovered in the present work will offer an excellent opportunity to study photoelectron angular distributions (PADs) from the 1S, 1P, and 1D electronic shells that are the most *ideal* orbitals in the spherical jellium model. As shown in Figs. 1(d) – (f), their PADs all exhibit a weak positive anisotropy to the laser polarization direction with the photoelectron anisotropy parameters, β , of 0.54, 0.38, and 0.33 for $M = V, Nb$, and Ta , respectively. Investigating how the β value varies as a function of the photoelectron kinetic energy, as has been successfully demonstrated for Na_n^- by Bartels et al.,²⁶ will enable us to characterize the fully degenerate 1D electronic shell from the angular-momentum point of view. It is also interesting to measure PADs from ligand-protected icosahedral cores of gold and silver clusters, whose photodetachment spectra have been measured recently.²⁷ The study will address how ligands affect PADs from discrete energy levels formed in gold and silver superatomic cores.

EXPERIMENTAL METHODS

The experiments were conducted using a photoelectron imaging apparatus for metal cluster anions that we have built recently,¹³ which allows for efficient measurements of photoelectron images under space-charge free conditions. While a continuous-wave (CW) laser diode at 404 nm (3.07 eV) was employed as a photodetachment light source in the original setup, we used fs UV pulses at 310 nm (4.00 eV) in the present study, which were generated from an optical parametric

amplifier (ORPHEUS, Light Conversion) pumped by a Yb:KGW (ytterbium-doped potassium gadolinium tungstate) regenerative amplifier (PHAROS PH2-10W, Light Conversion) that delivers 1030 nm, ~210 fs, and 100 μ J pulses at a repetition rate of 100 kHz. The procedures for acquiring photoelectron images of $M@Ag_{12}^-$ ($M = V, Nb, \text{ and } Ta$) are given below.

A continuous beam of mass-selected $M@Ag_{12}^-$ ($M = V, Nb, \text{ and } Ta$) cluster anions was produced using a magnetron-sputtering cluster ion source, which was cooled with liquid nitrogen at ~120 K, followed by a quadrupole mass filter.²⁸ The continuous cluster-anion beam was transformed into ion bunches with a potential switch driven by a high voltage (+600 V) pulser synchronized with the 100-kHz Yb:KGW regenerative amplifier. The bunched anion beam was sent to an assembly of electrodes for extracting photoelectrons, which formed relatively low (10 V/cm) static electric fields²⁹ optimized for a velocity-map imaging (VMI) condition,³⁰ where the anions in the 100-kHz bunched beam were irradiated by linearly-polarized 310-nm fs pulses with the average power of ~50 mW. Photoelectrons ejected from the anionic clusters were accelerated toward a dual microchannel plate (ϕ 40 mm) coupled with a P43 phosphor screen, on which the 2D projection of the 3D photoelectron distribution was captured using a complementary metal-oxide semiconductor camera (CS2100M-USB, 1920×1080 , Thorlabs). Since a part of the bunched anion beam itself created low energy electrons as it impinges on the VMI electrodes, we subtracted a photoelectron image taken without the laser beam (i.e., laser-off image) from the laser-on image to remove such backgrounds originated from the anion beam. The polar-orbital-peeling (POP) method³¹ was used to reconstruct the original 3D distribution of the photoelectrons from the subtracted image. As described in ref.³¹, photodetachment spectra and laboratory-frame photoelectron-angular distributions (PADs) were obtained through the reconstruction procedure.

Photoelectron kinetic energies (PKEs) were calibrated using the vertical detachment energy of Ag_3^- (2.43 eV),³² which was done just after taking the data for M@Ag_{12}^- by maintaining the temperature, T , of the magnetron sputtering source at ~ 120 K to produce also Ag_3^- . To evaluate the energy resolution and instrumental response of our VMI setup at PKEs comparable to those obtained for photoelectrons from M@Ag_{12}^- ($\text{M} = \text{V}$, Nb , and Ta) with the 310-nm pulses, we measured a photoelectron image of Ag^- with a detachment laser tuned at 510 nm (2.43 eV), which was measured at $T \sim 300$ K; the abundance of Ag^- was not sufficient at $T \sim 120$ K. Fig. S1 in Supporting Information presents a photoelectron spectrum for Ag^- obtained from the photoelectron image. The energy resolution is evaluated to be 0.06 eV ($\sim 5\%$) at $\text{PKE} = 1.13$ eV.

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266 **Notes**

267 The authors declare no competing financial interests.

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269 ASSOCIATED CONTENT

270 Supporting Information: The photodetachment spectrum of Ag^- obtained with incident photons at
271 2.43 eV and the results of the additional calculations of VDEs and electron binding energies for
272 Ag_{12}M^- (M = V, Nb, and Ta).

273

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