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# Some Remarks on Security of Receipt-free E-auction

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## Abstract

Recently, a receipt-free scheme is rising for a secure e-auction. The goal of a receipt-free scheme in an e-auction is to prevent a bid-rigging. If the bid-rigging happens in the e-auction, the winner can get the bidding item with an unreasonably low price. The first receipt-free scheme for the e-auction was proposed by Abe and Suzuki. Chen, Lee and Kim also proposed the extended receipt-free scheme. In this paper, we point out that the proposed receipt-free schemes do not prevent perfectly the bid-rigging attack. Moreover, we indicate that a bid-collision is a possible cause of an e-auction. In the strict sense, the bid-collision is different from the bid-rigging. In this paper, we do not present the scheme which can prevent the bid-collision attack. We compare the bid-rigging attack with the bid-collision attack, and analyze the security of the existed receipt-free schemes in a viewpoint of the bid-rigging attack and the bid-collision attack.

**Keyword:** E-auction, Security, Receipt-freeness, Bid-rigging, Bid-collision, Cryptography,

## 1. Introduction

### 1.1. Background

Recently, a receipt-free scheme is rising in field of e-voting [BT94,SK95,HS00] and e-auction [AS02, CLK03]. The receipt-free scheme of e-voting means that a voter should not prove other parties or people how he voted. It is known that the receipt-free scheme of e-auction is to prevent bid-rigging. Abe and Suzuki [AS02] proposed firstly the receipt-free scheme for an e-auction. They introduced the reason why the receipt-free scheme is required in an e-auction as follows.

*The coercer orders other bidders to bid very low price, he then can win the auction at an unreasonably low price. To make other bidders obey his order, the coercer punishes bidders who do not cast the ordered bidding price, and the buyer rewards for bidders who cast the ordered bidding price.*

The goals of the coercer are that he becomes the winner and wants to buy the auction item with an unreasonably low price. Chen, Lee and Kim [CLK03] pointed out that the receipt-free scheme of Abe and Suzuki does not provide a receipt-free for a winner. Also, they proposed a new receipt-free scheme. Table 1 shows the security of proposed receipt-free schemes.

### 1.2. Our contribution

In this paper, we analyze the security on the existed receipt-free e-auction. Although the coercer is the winner, the bid-rigging can succeed under the existed receipt-free scheme. Then, the receipt-free scheme is meaningless. That is, the known receipt-free schemes do not prevent the bid-rigging perfectly.

Moreover, we present a bid-collision attack in e-auction. The bid-collision means that all the bidders have a prior consultation on a winner and a winning price with an unreasonably low price. Therefore, all the bidders know the estimated winner and winning price. They can check whether their promise is kept or not. If their promise is kept, the winner rewards for other bidders. Otherwise, the winner is punished by other bidders. To prevent the bid-collision attack is the bidder should not prove whether he cast a bid or not. We call *bidding-freeness*. Table 2 shows that although the existed receipt-free scheme can prevent partly the bid-rigging attack, but does not prevent the bid-collision attack at all.

**Table 1. Receipt-freeness of the existed receipt-free e-auctions**

Scheme	Receipt-freeness	
	Winner	Losing Bidders
[AS02]	No	Yes
[CLK03]	Yes	Yes

**Table 2. Security analysis in a viewpoint of bid-rigging and bid-collusion**

	Receipt-freeness		Bidding-freeness	
[AS02]	$W = C$	No	$W = SB$	No
	$W \neq C$	No	$W \neq SB$	No
[CLK03]	$W = C$	Yes	$W = SB$	No
	$W \neq C$	Yes	$W \neq SB$	No

(W means Winner, and C means Coercer. SB is the Special Bidder)

## 2. Bid-rigging vs. Bid-collusion

In this section, we introduce the difference between the bid-rigging and the bid-collusion.

### 2.1 Bid-rigging

#### Winner = Coercer

If other bidders cast the ordered bidding price and the coercer becomes the winner, then the coercer rewards for other bidders. Although some bidders did not obey the order of the coercer, they can require a reward to the coercer, because the coercer is the winner with an unreasonably low price. Then, other bidders do not need to prove his bidding price. That is, it does not need the receipt-free scheme.

#### Winner Coercer

If the coercer is not the winner, he looks for the winner. Then, it needs the receipt-free scheme. And, it can be happen the dispute that the bidders who cast the ordered bidding prices can require a reward to the coercer. To success the bid-rigging, it needs two conditions as follows:

- The coercer should control all the bidders in e-auction.
- The coercer should not perform non-reputation.

### 2.2 Bid-collusion

The bid-collusion means that all the bidders have a prior consultation on the winner and the winning price. Therefore, all the bidders know the estimated winner (special bidder) and winning price.

#### Winner = Special Bidder

If the special bidder is the winner, he should reward the other bidders. Then, the other bidders do not need

to prove their bidding prices. This case is same with 'winner = coercer' of bid-rigging.

#### Winner Special Bidder

All the bidders know the estimated winner and winning price, and know whether it keeps their promise or not. If the special bidder is not the winner, the other bidders punish the winner who broke their promise. To prevent the bid-collusion attack, it is required that a bidder should not prove he cast a bid. We call this method *bidding-freeness*. In table 3, we compare the bid-rigging attack with the bid-collusion attack.

**Table 3. Comparison of Bid-rigging and Bid-collusion**

Attack	Bid-rigging	Bid-collusion
Control	Coercion-control	Self-control
Control contents	Bidding price	Winner and Winning price
Corresponding method	Receipt-freeness	Bidding-freeness

## 3. Review of Abe-Suzuki model and Chen-Lee-Kim Model

In figure 1,2 and 3, we compare Abe-Suzuki model with Chen-Lee-Kim model by each phase.

## 4. Security Analysis in a viewpoint of Bid-rigging

### 4.1. Winner = Coercer

In case of Abe-Suzuki model, the winner and the winning price are published by auctioneers. If the coercer becomes the winner, he rewards for other bidders who obey his order without proving other bidders' bidding price. Moreover, the coercer can not perform non-repudiation. That is, the receipt-freeness is meaningless in this case. In case of Chen-Lee-Kim model, only the winning price is published. A bidder does not know who the winner is. Therefore, the receipt-freeness is protected unless the seller publishes the winner. Moreover, the coercer which is the winner can perform non-repudiation. It can be happened the argument on the winner.

### 4.2. Winner Coercer

All the bidders know the winner in Abe-Suzuki model. If the coercer is not the winner, the coercer inflicts punishment upon the winner. Also, some bidders who cast the ordered bidding price cry for a reward to the coercer. But, they can not prove his

Abe-Suzuki Model	Chen-Lee-Kim Model
<ul style="list-style-type: none"> <li>- <math>a</math> auctioneers : <math>\{A_i \mid i = 0, \dots, a\}</math></li> <li>- <math>b</math> bidders : <math>\{B_j \mid j = 0, \dots, b\}</math></li> <li>- Price list : <math>P = \{l \mid l = 0, \dots, m\}</math></li> <li>- Large primes : <math>p (= 2q + 1), \quad q</math></li> <li>- A generator <math>g</math> of order <math>q</math> subgroup of <math>Z_q^*</math></li> <li>- Messages <math>M_0, M_1 \in Z_q</math>, that mean “I do not bid”, “I bid” respectively.</li> </ul>	<ul style="list-style-type: none"> <li>- <math>m</math> bidders : <math>\{B_i \mid i = 1, 2, \dots, m\}</math></li> <li>- Seller <math>S</math>, Auctioneer <math>A</math>, Auction Issuer <math>AI</math></li> <li>- Large primes : <math>p, \quad q \mid p - 1</math></li> <li>- A subgroup <math>G_q</math> of order <math>q</math> subgroup of <math>Z_q^*</math></li> <li>- <math>g</math> is a generator of <math>G_q</math></li> <li>- Messages <math>G_1, G_2 \in G_q</math>, which mean “I bid”, “I do not bid” respectively.</li> </ul>

**Fig. 1 Preparation step of the proposed receipt-free models**

Abe-Suzuki Model	Chen-Lee-Kim Model
<ul style="list-style-type: none"> <li>- A Bidder chooses his secret key <math>x_j \in Z_q</math>, public key <math>h_j = g^{x_j}</math>, bidding price <math>p_j \in P</math>, and secret seeds <math>r_{l,j} \in Z_q</math> (<math>l = 1, 2, \dots, m</math>) randomly.</li> <li>- The bidder computes a sequence of chameleon bit-commitments <math display="block">C_{l,j} = \begin{cases} g^{M_1} h^{r_{l,j}} &amp; (l = p_j) \\ g^{M_0} h^{r_{l,j}} &amp; (l \neq p_j) \end{cases}</math> For <math>l = 1, \dots, m</math>.</li> <li>- The bidder proves to each auctioneer that bidder knows the secret key <math>\log_g h_j = x_j</math> and the discrete logs <math>\log_g C_{i,j}</math> by the interactive zero-knowledge proof.</li> <li>- The Bidder makes <math>t</math>-out-of-<math>a</math> secret shares <math>r_{i,j}^i</math> for secret seeds <math>r_{i,j}</math>, and sends <math>i</math>-th shares <math>r_{i,j}^i</math> (<math>i = 1, 2, \dots, m</math>) of secret seeds <math>r_{i,j}^i</math> (<math>i = 1, 2, \dots, m</math>) with his signature to <math>i</math>-th auctioneer through the one-way untappable channel</li> </ul>	<ul style="list-style-type: none"> <li>- A bidder chooses his secret key <math>x_{B_i}</math>, public key <math>h_{B_i} = g^{x_{B_i}}</math>, bidding price <math>p_i \in P</math>.</li> <li>- The bidder computes the encrypted bidding vector <math display="block">C_{l,j} = (x_{i,j}, y_{i,j}) = \begin{cases} (g^{a_{i,j1}}, (h_1 h_2)^{a_{i,j}} G_1), &amp; \text{if } j = p_i \\ (g^{a_{i,j1}}, (h_1 h_2)^{a_{i,j}} G_2), &amp; \text{if } j \neq p_i \end{cases}</math></li> <li>- The seller generates the receipt-free bidding vector <math>C_{i,j}^* = (x_{i,j}^*, y_{i,j}^*) = (x_{i,j} u_j, y_{i,j} v_j)</math>, where <math>u_j = g^{\beta_j}</math> and <math>v_j = (h_1 h_2)^{\beta_j}</math>.</li> <li>- They jointly generate the proof of the validity of the bidding vector.</li> <li>- The bidder <math>B_i</math> sends <math>C_{i,j}^*</math>, <math>P_1</math> and <math>P_2</math> to the corresponding fields of the bulletin board.</li> <li>- <math>P_1</math> and <math>P_2</math> are a kind of proof value. For detail, see [CLK03]</li> </ul>

**Fig. 2 Bidding step of the proposed receipt-free models**

bidding price. It can be happened by the argument on the winner. In case of Chen-Lee-Kim model, the receipt-free is protected unless the seller publishes the winner.

## 5. Security Analysis in a viewpoint of Bid-collusion

We assume that the special bidder is in collusion with other bidders. All the bidders know the estimated winner and winning price. The special bidder can be rotated by an auction item.

### 5.1. Winner = Special Bidder

We assume that the special bidder is the winner. The special bidder rewards for other bidders who cast a bid. Then, other bidders do not need to prove their bidding

prices. Only, he should prove the fact that he made a bid to a special bidder. In case of Abe-Suzuki model, a bidder knows his secret key  $x_j \in Z_q$ , public key

$h_j = g^{x_j}$ , bidding price  $p_j \in P$ , and secret seeds  $r_{l,j} \in Z_q$  ( $l = 1, 2, \dots, m$ ) randomly. Therefore, he can prove his chameleon bit-commitments  $C_{l,j}$  to the special bidder.

In case of Chen-Lee-Kim model, a bidder  $B_i$  sends  $C_{i,j}^*$ ,  $P_1$  and  $P_2$  to the corresponding fields of the bulletin board. After the e-auction system is over, the bidder can prove  $C_{i,j}^*$  to the special bidder because he knows used  $x_{B_i}$ , public key  $h_{B_i} = g^{x_{B_i}}$ , bidding price  $p_i \in P$  and the encrypted bidding vector  $C_{i,j}$ .

Abe-Suzuki Model	Chen-Lee-Kim Model
<ul style="list-style-type: none"> <li>- All auctioneers iterate the following steps for each price <math>l = m, m-1, \dots, 1</math> to determine winning (maximum) bidding price <math>P_{\min} = \max_j \{p_j\}</math> and winning bidders.</li> <li>- Each auctioneer publishes shares <math>r_{i,j}^l</math> (<math>j=1,2,\dots,b</math>) of <math>l</math>-th secret seeds <math>r_{i,j}</math> and check the following equalities <math display="block">C_{i,j} = g^{M_1} h^{r_{i,j}}, (j=1,2,\dots,b)</math> for all bidders <math>B_j</math>.</li> <li>- If there exist <math>j</math>'s for which the above equality holds, auctioneers publish that the winning bidders are these <math>B_j</math>'s and their winning price <math>p_{win}</math> is <math>l</math>, and stop opening.</li> </ul>	<ul style="list-style-type: none"> <li>- <math>AI</math> and <math>A</math> compute the auction result.</li> <li>- Let <math>j = n</math>. <math>AI</math> and <math>A</math> compute separately the final price vector <math display="block">(X_i, Y_i) = (\sum_{i=1}^m x_{i,j}^*, \sum_{i=1}^m y_{i,j}^*)</math> <li>- They then separately publish <math>X^{x_1}_j, X^{x_2}_j</math> and provide a non-interactive zero-knowledge proof of common exponent with their public key <math>h_1, h_2</math>. Let <math display="block">R_j = Y_i / X^{x_1+x_2} = G_1^{l_j} G_2^{m-l_j}</math> where <math>0 \leq l_j \leq m</math>. <li>- If <math>l_j = 0, j = j-1</math>; else terminated.</li> <li>- <math>AI</math> and <math>A</math> determine the first <math>j</math> which satisfies <math>j \neq 0</math>, and winning price is the certain <math>j</math>, denote <math>P_w</math>.</li> <li>- <math>AI</math> and <math>A</math> publish the winning price <math>P_w</math>.</li> </li> </li></ul>

**Fig. 3 Opening step of the proposed receipt-free models**

### 5.2. Winner Special Bidder

We assume that the special bidder does not the winner. This means that the promise of all the bidders is broken. In case of Abe-Suzuki model, the winning price is published and all auctioneers know the estimated winning price. All the bidders can compare the published winning price with the estimated winning price. Other bidders inflict punishment upon the winner who broke their promise. In case of Chen-Lee-Kim model, only the winning price is published at bulletin board. Therefore, Chen-Lee-Kim model does not prevent the bid-collusion attack as that of Abe-Suzuki model.

## 6. Conclusions

In order to prevent the bid-rigging attack, the receipt-free schemes have been proposed. The first receipt-free e-auction was proposed by Abe and Suzuki. Also, Chen-Lee-Kim proposed the extended receipt-free scheme. In this paper, we point out that the existed receipt-free schemes do not prevent the bid-rigging attack perfectly. Moreover, we indicate that the bid-collusion is a possible cause of an e-auction. In this paper, we introduce the difference between the bid-rigging and the bid-collusion. To prevent the bid-collusion, a bidder should not prove he cast a bid. We call this method bidding-freeness. We analyze the

security of the existed receipt-free schemes in a viewpoint of the receipt-freeness and the bidding-freeness. However, we do not give the bidding-free scheme in this paper.

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