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Supervised Image Classification based on AdaBoost with Contextual Weak Classifiers

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Abstract

AdaBoost, one of machine learning techniques, is employed for supervised classification of land-cover categories of geostatistical data. We introduce contextual classifiers based on neighboring pixels. First, posterior probabilities are calculated at all pixels. Then, averages of the posteriors in various neighborhoods are calculated, and the averages are used as contextual classifiers. Weights for the classifiers can be determined by minimizing the empirical risk with multiclass. Finally, a linear combination of classifier is obtained. The proposed method is applied to artificial multispectral images and shows an excellent performance similar to the MRF-based classifier with much less computation time.

1. Introduction

AdaBoost proposed by [0] is one of machine learning techniques and has been progressed for pattern recognition rapidly and widely. AdaBoost combines weak classifiers into a weighted voting machine, and it shows high performance in various fields, see [2–4].

In this paper, we introduce AdaBoost for contextual image classification for geostatistical data. First, we prepare a posterior probability given feature vector at each pixel. The posteriors can be defined by machine learning techniques as well as statistical methods. Then, averages of the posteriors are calculated in various types of neighborhoods, and we positively use them as classifiers. The weights for the classifiers are obtained by minimizing the empirical risk with multiclass. Finally, a linearly combined classifier gives a contextual voting machine.

The proposed method is shown to be a very fast algorithm. It needs only 1/100 of time required by MRF-based classifiers implemented by [?]. The performance of our method keeps equivalent to that of MRF-based classifiers. Also, the proposed method is very flexible since the posteriors can be derived from various techniques: support vector machines (SVM), AdaBoost, and artificial neural networks (ANN), see e.g. [6–8].

In Section II, Real AdaBoost is explained. The determination of the coefficient of

classifiers are discussed in a multiclass case. Section III defines contextual classifiers. Neighborhoods of a pixel and the averages of the posteriors in the neighborhoods are defined, which will be viewed as classifiers. The proposed method is applied to a numerical example in Section IV. It shows an excellent performance similar to MRF-based classifiers. Section V concludes the paper.

2. Real AdaBoost with multiclass

Let $\mathcal{D} = \{1, \dots, n\}$ be a training area consisting of n pixels, and each pixel belongs to one of g possible categories C_1, \dots, C_g . Suppose that an m -dimensional feature vector $\mathbf{x}_i \in \mathbb{R}^m$ is observed at each pixel i . A label of the category covering the pixel i is denoted by $y_i \in \{1, \dots, g\}$. Let $f(\mathbf{x}, y)$ be a discriminant function. We allocate a feature vector $\mathbf{x} \in \mathbb{R}^m$ into a category label:

$$y_f(\mathbf{x}) = \arg \max_{y \in \{1, \dots, g\}} f(\mathbf{x}, y). \quad (1)$$

In the ordinary setting of AdaBoost, the function f is restricted to take only zero or one as follows.

$$f(\mathbf{x}, y) = \begin{cases} 1 & \text{if } y = y_f(\mathbf{x}) \\ 0 & \text{otherwise.} \end{cases} \quad (2)$$

Typical weak classifiers are decision stumps given by the functions $\delta \text{sign}(x^j - t)$ in binary class with label set $\{-1, 1\}$, where $\delta = \pm 1$, $t \in \mathbb{R}$, x^j is the j -th variate of the feature vector \mathbf{x} and $\text{sign}(z)$ is the sign of the argument z .

We also consider the case such that the discriminant function f takes real values. For example, a posterior probability:

$$p(y | \mathbf{x}) = p(\mathbf{x} | y) / \sum_{y'=1}^g p(\mathbf{x} | y') \quad (3)$$

takes positive values, where $p(\cdot | y)$ is a class-conditional probability density of the category C_y .

AdaBoost aims to combine weak classifiers into a strong classifier. Let $\mathcal{F} = \{f(\mathbf{x}, y)\}$ be a set of discriminant functions (weak classifiers). The loss of misclassification due to the function f is assessed by the following exponential loss function:

$$L(\mathbf{x}, y | y_0) = \exp [f(\mathbf{x}, y) - f(\mathbf{x}, y_0)] \quad (4)$$

for $y \neq y_0$, $y = 1, \dots, g$, where y_0 be the true label of the feature vector \mathbf{x} . The loss function (4) is an extension of the exponential loss with binary class. The empirical risk is defined by

$$R_{\text{emp}}(f) = \frac{1}{n} \sum_{i=1}^n \sum_{y=1}^g \exp [f(\mathbf{x}_i, y) - f(\mathbf{x}_i, y_i)], \quad (5)$$

where (\mathbf{x}_i, y_i) are training data on the area \mathcal{D} .

Let f and F be discriminant functions (fixed). Then, the optimal coefficient c

which gives the minimum value of the empirical risk $R_{\text{emp}}(F + cf)$ is denoted by c_* :

$$c_* = \arg \min_{c \in \mathbb{R}} \{R_{\text{emp}}(F + cf)\}.$$

If the function f takes 0-1 values like (2), the optimal coefficient c_* can be expressed in the closed form.

If f takes real values, there is no closed form to the optimal coefficient c_* . We will take an iterative procedure for the estimation. The convergence of the procedure is, however, very fast.

AdaBoost combines several discriminant functions so as to form a strong classifier. Now, we slightly extend Real AdaBoost for combining T functions, where T is a positive integer. Let $\mathcal{F}_t (\subset \mathcal{F})$ be a subset of discriminant functions for $t = 1, 2, \dots, T$. (Possibly, $\mathcal{F}_1 = \mathcal{F}_2 = \dots = \mathcal{F}_T$.) The procedure is as follows.

1. Find a weak discriminant function $f \in \mathcal{F}_1$ and the coefficient c which minimize the empirical risk $R_{\text{emp}}(cf)$ defined by the formula (5), say f_1 and c_1 .
2. Consider the empirical risk $R_{\text{emp}}(c_1 f_1 + cf)$ with given $c_1 f_1$ in the previous step. Then, find the optimal discriminant function $f \in \mathcal{F}_2$ and the coefficient c which minimize the empirical risk, say f_2 and c_2 .
3. This is repeated T -times and obtain the final discriminant function:

$$F_T = c_1 f_1 + \dots + c_T f_T. \quad (6)$$

4. A test vector \mathbf{x} is classified into the label $\arg \max_{y \in \{1, \dots, g\}} \{F_T(\mathbf{x}, y)\}$, where F_T is defined in the above.

We note that AdaBoost is based on a weighted majority vote principle.

3. Neighborhoods and contextual classifiers

As we have seen in Section II, AdaBoost requires multiple discriminant functions defined in the feature space. We will add contextual classifiers to the set of non-contextual classifiers so as to give contextual classification.

Let $d(i, j)$ be a distance between centers of two pixels i and j in the domain \mathcal{D} . Then, define a subset $U_r(i)$ of the area \mathcal{D} with center i and radius r by

$$U_r(i) = \{j \in \mathcal{D} \mid d(i, j) = r\} \text{ for } r = 0, 1, \sqrt{2}, 2, \sqrt{5}, \dots$$

Note that the subset $U_r(i)$ is different from an ordinary neighborhood. See Fig. 1 for the subsets $U_r(i)$ for $r = 0, 1, \sqrt{2}, 2$. It is seen that $U_0(i) = \{i\}$, $U_1(i)$ is the first-order neighborhood of the pixel i , and $U_1(i) \cup U_{\sqrt{2}}(i)$ forms the second-order neighborhood. Suppose that a statistical model is applied to the distribution in the feature space. Then, the posterior probability $p(y | \mathbf{x}_i)$ defined by (3) is a measure of confidence of the current classification. Such a measure is defined by machine learning techniques as well as statistical techniques. See [6–8] for posteriors

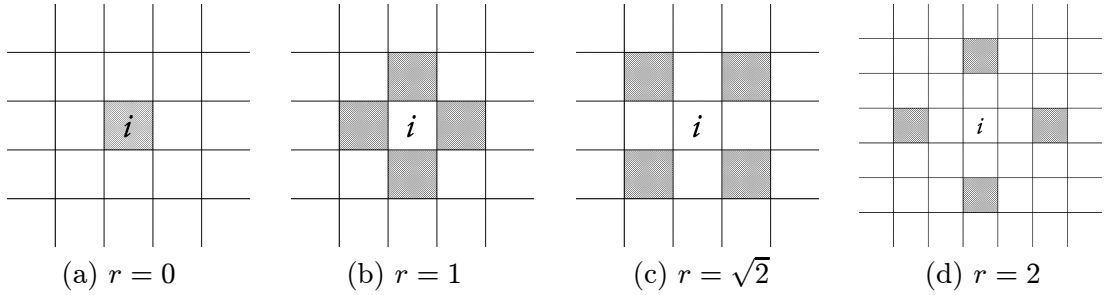


Figure 1. Isotropic subsets $U_r(i)$ with a center pixel i and radius r

introduced in SVM and AdaBoost.

Define the average of posterior probabilities in the subset $U_r(i)$ by

$$\bar{p}_r(y | \mathbf{x}_i) = \begin{cases} \sum_{j \in U_r(i)} p(y | \mathbf{x}_j) / |U_r(i)|, & \text{if } |U_r(i)| > 0 \\ 0, & \text{otherwise} \end{cases} \quad (7)$$

for $r = 0, 1, \sqrt{2}, \dots$, where $|S|$ denotes the cardinality of set S . Obviously, it holds that $\bar{p}_0(y | \mathbf{x}_i) = p(y | \mathbf{x}_i)$. Hence, noncontextual classification is done by the posterior $\bar{p}_0(y | \mathbf{x}_i)$, which is a strong classifier. If the spatial dependency of the categories exists, the averaged posteriors $\bar{p}_1(y | \mathbf{x}_i)$ in the adjacent pixels to the pixel i also have information for classification. If the spatial dependency is strong, $\bar{p}_r(y | \mathbf{x}_i)$ with large r is also useful. Thus, we adopt the average of the posteriors $\bar{p}_r(y | \mathbf{x}_i)$ as a classifier of the center pixel i .

Obviously, the importance of the posteriors for classifying the center pixel i will be in the following order:

$$\bar{p}_0(y | \mathbf{x}_i), \bar{p}_1(y | \mathbf{x}_i), \bar{p}_{\sqrt{2}}(y | \mathbf{x}_i), \dots \quad (8)$$

The coefficients to the averaged posteriors $\bar{p}_r(\cdot | \cdot)$ can be tuned by minimizing the empirical risk (5).

Thus, candidates of contextual classifiers are as follows.

(1a) The averaged posteriors $\bar{p}_r(y | \mathbf{x}_i)$ as (7) in the subset $U_r(i)$.

(1b) Thresholding of the function $\bar{p}_r(y | \mathbf{x}_i)$ by

$$p_r(y | \mathbf{x}_i) = \begin{cases} 1 & \text{if } y = \operatorname{argmax}_{y'} \bar{p}_r(y' | \mathbf{x}_i) \\ 0 & \text{otherwise.} \end{cases} \quad (9)$$

(2a) Proportion of the labeled pixels in $U_r(i)$:

$$\bar{q}_r(y) = |\{j \in U_r(i) | y_j = y\}| / |U_r(i)|. \quad (10)$$

(2b) Majority vote in $U_r(i)$:

$$q_r(y) = \begin{cases} 1 & \text{if } y = \operatorname{argmax}_{y'} \bar{q}_r(y') \\ 0 & \text{otherwise.} \end{cases} \quad (11)$$

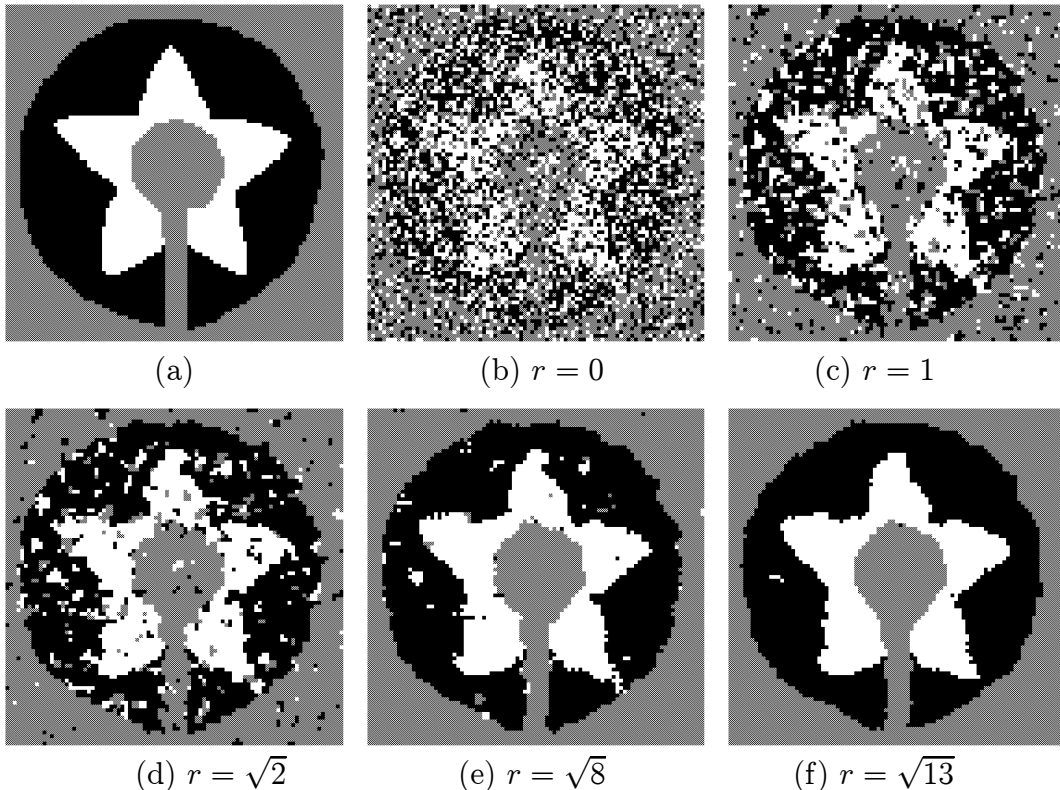


Figure 2. True labels (a) and estimated labels (b): by the linear discriminant function, and (c)~(f): by Spatial AdaBoost based on $c_0\bar{p}_0 + c_1\bar{p}_1 + \dots + c_r\bar{p}_r$

We here note that all the classifiers in the above are well-defined for the training data. However, the classifiers (2a) and (2b) cannot be defined by test data because test labels are unknown. If temporal estimates for test labels are available, the classifiers (2a) and (2b) are utilized. But, the classifiers supply only supplementary information.

Taking the importance of the posteriors, we propose to take T subsets $\mathcal{F}_1, \dots, \mathcal{F}_T$ of discriminant functions in Section 2 as follows.

$$\mathcal{F}_1 = \{\bar{p}_0\}, \mathcal{F}_2 = \{\bar{p}_1\}, \mathcal{F}_3 = \{\bar{p}_{\sqrt{2}}\}, \mathcal{F}_4 = \{\bar{p}_2\}, \mathcal{F}_5 = \{\bar{p}_{\sqrt{5}}\}, \dots \quad (12)$$

Each subset consists of a single averaged posterior, and we get the final discriminant function of the form $c_0\bar{p}_0(y | \mathbf{x}_i) + c_1\bar{p}_1(y | \mathbf{x}_i) + \dots + c_r\bar{p}_r(y | \mathbf{x}_i)$.

4. Numerical experiments

Our method is examined through multispectral images generated over the image (a) of Fig. 2 with three categories ($g = 3$). The labels 1, 2 and 3 correspond to the colors black, white and grey. The numbers of pixels from the categories are respectively given by 3330, 1371 and 3580. We simulate four-dimensional spectral images ($m = 4$) at each pixel of the true image (a) following multivariate normal distributions independently with mean vectors $\boldsymbol{\mu}(1) = (0 \ 0 \ 0 \ 0)^T$, $\boldsymbol{\mu}(2) = (1 \ 1 \ 0 \ 0)^T / \sqrt{2}$, $\boldsymbol{\mu}(3) = (1.0498 \ -0.6379 \ 0 \ 0)^T$ and with common variance-covariance matrix $\sigma^2 E_4$, where E_4 denotes the identity matrix. Test data are similarly generated over the same image (a), and the normal distributions are used for driving the posteriors.

We set the subsets \mathcal{F}_t of discriminant functions by the sequence (12). Hence, we

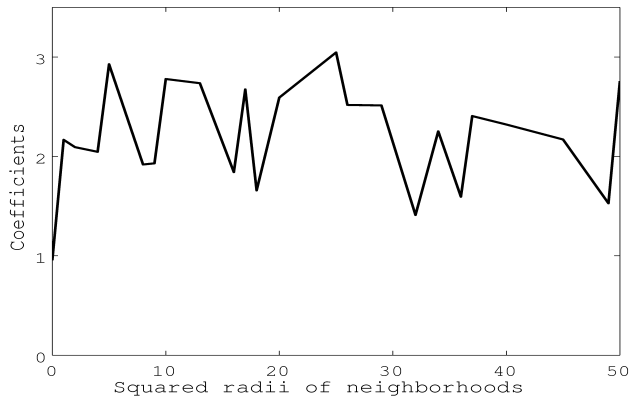


Figure 3. Estimated coefficients for the posteriors

applied the discriminant functions: $c_0\bar{p}_0, c_0\bar{p}_0+c_1\bar{p}_1, \dots, c_0\bar{p}_0+c_1\bar{p}_1+\dots+c_{\sqrt{50}}\bar{p}_{\sqrt{50}}$ to test data, where the coefficient c_r is sequentially tuned by minimizing the empirical risk.

Fig. 3 plots the coefficients $c_0, c_1, \dots, c_{\sqrt{50}}$ against radius r in the case $\sigma^2 = 1$. Magnitude of the coefficients give a reliability of the corresponding classifiers. The coefficient c_0 is not large, and this is ascertained by the fact that the error rate due to \bar{p}_0 (the noncontextual classifier) is 41.75%.

Fig. 4 show training and test error rates due to the classifiers $c_0\bar{p}_0+c_1\bar{p}_1+\dots+c_r\bar{p}_r$ for $r = 0, 1, \dots, \sqrt{50}$ in the case with error variance $\sigma^2 = 1$. The training error (a) shows that the neighborhood information reduces the error rate rapidly, and it is stable even if the radius r is too large. The test error attains the minimum value at $r^2 = 13$.

Fig. 2 (b) is the classified image obtained by the posterior \bar{p}_0 , which is equivalent to the linear discriminant function. The classified images are getting closer to the true label (a) as the radius r is getting larger.

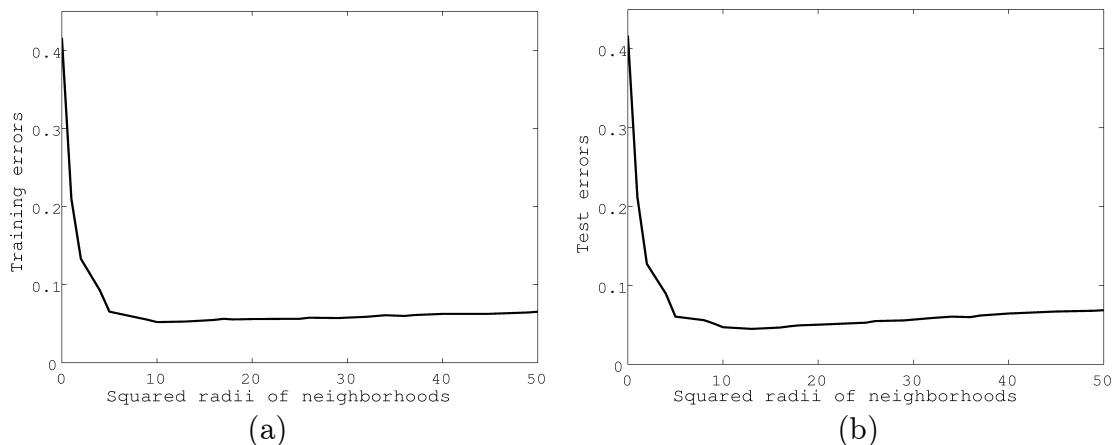


Figure 4. Error rates against squared radius r^2 for training data (a) and test data (b) due to the discriminant functions $c_0\bar{p}_0 + c_1\bar{p}_1 + \dots + c_r\bar{p}_r$

TABLE 1. Error rates (%) of classification results based on Gaussian MRF and Spatial Real AdaBoost

radius r	Distributions of the categories : $N_4(\boldsymbol{\mu}(g), \sigma^2 E)$					
	$\sigma^2 = 1$				$\sigma^2 = 4$	
	GMRF	CPU	AdaBoost	CPU	GMRF	AdaBoost
0	41.75	–	41.75	–	54.56	54.56
1	10.68	210	21.46	1.66	40.55	41.03
$\sqrt{2}$	5.01	409	12.91	1.70	17.14	34.15
2	3.57	617	8.98	1.64	12.04	29.11
$\sqrt{5}$	3.23	852	6.09	2.00	10.04	22.50
$\sqrt{8}$	4.61	1117	5.62	1.83	10.18	20.88
3	5.12	1402	5.17	1.81	10.19	19.26
$\sqrt{10}$	6.10	1716	4.64	2.24	11.05	16.50
$\sqrt{13}$	9.52	2082	4.46	2.20	19.41	14.88
4	11.70	2481	4.64	1.97	18.51	14.31
$\sqrt{17}$	13.56	2904	4.79	2.27	20.66	13.48
$\sqrt{18}$	21.78	3371	4.87	2.13	21.46	13.28
$\sqrt{20}$	30.58	3376	5.00	2.41	22.79	12.33

Table 1 compares error rates due to Gaussian MRF-based (GMRF) and the proposed discriminant functions in two cases: $\sigma^2 = 1, 4$. Each row is corresponding to GMRF with the neighborhood system $U_1(i) \cup U_{\sqrt{2}}(i) \cup \dots \cup U_r(i)$ and the discriminant function $c_0\bar{p}_0 + c_1\bar{p}_1 + \dots + c_r\bar{p}_r$. The third and fifth columns show CPU time (seconds) required to GMRF and the proposed method respectively. GMRF needs much time for tuning the dependency parameter [5], whereas the proposed method determines the coefficient sequentially with several iterations. It is shown that the proposed method is very fast procedure compared with the ordinary MRF-based classifier, and that both the classifiers show similar performance.

5. Conclusion

Real AdaBoost is introduced to provide contextual image classification. Weak classifiers based on posteriors on subsets of neighbors are proposed. The proposed method is flexible in the following two points. One is that various types of posteriors obtained by machine learning techniques as well as statistical models can be implemented. The other is in the definitions of the neighborhoods. In Section II, isotropic neighborhoods of a center pixel are considered (Fig. 1). In nonisotropic image case, directed neighborhoods would be useful, see Fig. 5. This means that the proposed method would be also applicable to image classification with texture.

Features of the proposed method are as follows.

- Various types of posteriors can be implemented.
- Various types of neighborhoods can be implemented.
- The method requires much less computation time and shows similar performance to MRF-based classifiers.

Selection of types of posteriors and neighborhoods is a new problem. Selection of the number of classifiers is also an old and new problem.

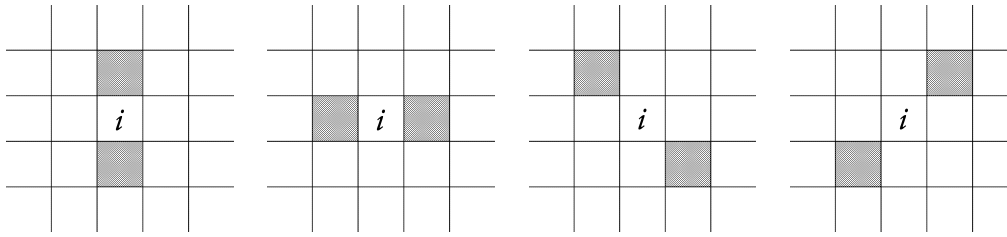


Figure 5. Directed subsets with a center pixel i and radius $r = 1, \sqrt{2}$

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