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The Analysis and Verification of Tree Volume Equations of *Pinus elliottii* in the State Forest of Águas de Santa Bárbara, São Paulo †

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The state forests in São Paulo are mostly covered by eucalyptus and pine stands. Pine was introduced into Brazil and planted on a large scale, during the period from 1958 until the beginning of 1965. The cutting cycle for these pine stands was planned to be 25 or 30 years, so that the cutting time will come soon. However, the volume and yield tables which are the necessary tools for the cutting planning, has not been prepared yet. The local volume table and the volume table made on the basis of variety has never been prepared at all. In relation to this, the analysis on tree volume equation, which is an aspect of the study on volume table compilation method, has been conducted for the pine stands of state forest in Águas de Santa Barbara. São Paulo state is located in subtropical region, where the season is distinguished into rainy and dry seasons. In connection to this condition, the bark of pine trees is extremely thick. Therefore, the volume equations are classified into the equations for volume with bark and for volume without bark. Further, these are classified into the equations for total volume, for commercial volume and for real commercial volume. The commercial volume consists of the timber until the smallest diameter of 5 cm, while the real commercial volume is timber volume where the bed of truck of 2.4 m is taken into consideration (the timber until the length as smallest as 1.2 m or half of the truck bed is counted). The analysis on these mentioned 6 different counted-based volumes was conducted and the corresponding 6 different volume equations were obtained.

INTRODUCTION

São Paulo state is covering area of 247,898 km² in which 5,035,070 ha are the forest area (in 1973). This forest area corresponds to 20.3 % of total area. The artificial forests cover 641,420 ha, which correspond to 12.7 % of forest area or 2.6 % of total area. Firther, the artificial forests consist of eucalyptus stands 490,560 ha, pine plantations 142,070 ha and the residual of 8,790 ha is covered by other species. These are corresponding to 76.5 %, 22.1 % and 1.4 % of total artificial forests, respectively. The eucalyptus stand is overwhelming majority in area. However, in the recent period,

[†] A part of this study which is entitled of "Preparation of Tree Volume Table" has been published in Synthetic Report of the Japanese Technical Cooperation Project for the Forestry Research in São Paulo, Brazil, JICA, FDD • JR86-30, 1986.

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pine plantation is being gradually increased.

In São Paulo state, from 1958 to 1965, tropical or subtropical pine trees of North or Middle America were introduced to encourage artificial plantation. Since the history is so short as about 20 years or so, tree volume tables have not been made for each district. Hence, the study of the preparation of tree volume table, taking up *Pinus elliottii* in state forest of Águas de Santa Barbara which is one of state forests, as the subject. At the same time some examination was attempted on this topic.

MATERIALS AND METHODS

1. Collection of materials

The whole area of the state forest of Águas de Santa Barbara were regarded as the subject for the area of sample trees, which would be basic material for tree volume table. Their diameter (DAP) and height (H) were intentionally selected so that they could be almost equally taken out from maximum to minimum. As the result, 100 sample trees of Pinus elliottii in total were collected as in Table 1.

2. Calculation of volume of sample trees

Six cases of the volumes are used in São Paulo state, i. e. A: the whole tree volume, B: the commercial volume of end diameter without bark of up 5 cm, C: the real commercial volume of end diameter without bark of up to 5 cm which was lumbered into the length of 2.4 m, equal to the truck bed length (there are also some cases marking use of as short as the half length, 1.2 m), and with bark and without bark for each of above 3 cases, all of which make 6 cases. These 6 volumes as below are being used for each purpose.

- 1 Total tree volume with bark
- (2) Total tree volume without bark
- (3) Commercial volume with bark
- 4 Commercial volume without bark
- (5) Real commercial volume with bark
- (6) Real commercial volume without bark

Therefore, cutting of sample trees, measurement in case of clean cutting, and volume calculation thereafter, were planned to furnish materials for each case. The measurement at cutting down and clean cut, volume calculation, etc. was carried out by simplified analysis method as shown in Table 2, based on the method of stem analysis. Table 3 is a list of values on sample trees, as above obtained. Various calculations were carried out by computer, as in the flow in Fig. 1. Table 4 indicated one example of sample tree No. 12, and Table 5 show a list of the results of various volume calculations of all sample trees (100 trees).

3. Examination on the volume equation

In the past, various volume equations have been proposed. Properly speaking, it is appropriate to examine each formula separately and select the most adaptable formula. However, in this study, the examination was made on the following five formulae which had been relatively often used.

Table 1. Distribution of sample trees by the grades of diameter at breast height with bark (DAP, Com casca) and tree height.

H										İ	DAP	(Com	casc	a / cr	n)									Tota
(m)	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	Total
7	1	_	1	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_		_		_	2
8	1		_	1	_			_	_	1	_		_	_	_	_	_	_		_	_	_	_	3
9	1	1	1	_	1	_	1	_	1	_		_	_	_	_		-	_	_	-	_	-		6
10	1	_	1	_	1	_	1	-	1	-	_	_	_	_	_	_	_	_	_	_		_	_	5
11	1		2	_	_		1	_	_	_	2	_	_		1	_	-	_		_	_	_	_	7
12	_	_	1	_	2	_	_		1	_	1		1	_	-	_	_	_	_	_	-	_	_	6
13	_		1		1	_	3	1	1	_	1				_		_	_		_	_	_	_	8
14	-	_		_		_	2	_	1	1	2	_	2	_	2	_	1	_		_		_		11
15	_	_	1	_	1	_	1	_	1	_	1	_	1	-	_	1	1	_	1	_	_	_	_	9
16	_	_	_	_	2	_	_		1	1	_	_	1	_	2	_	_	_	_	_	-	_		7
17	_	_	_	_	_	_	1	_		1	1	_	_	_	1		_	_	_	-	1	_	1	6
18	_	_	_	_		_	_	_	2	_	1		2	1		_	2	_	1	_	-	_	_	9
19	_	_	_	_	_		1	_	-	1	1	_	2	1	_	_	_	_		_	_	_	_	6
20	_	_	_	_	-	_	_	_	_	1	-	_	_	_	2	_	_	1	_	_	1		1	6
21	_	_	_	_	_	_	_	_		_	_	_	1		_	-	1	_	1	_	_	_	_	3
22	_	_	_	_		_	_	_	_	_	1	_	_	_	_	_			1		_	-	_	2
23	_	-	_	_	_	_		-	_	_	_	_		-	1	_	1	_	_	_	1	_	1	4
Γotal	5	1	8	1	8		11	1	9	6	11		10	2	9	1	6	1	4		3	_	3	100

Table 2. Field book for simplified stem analysis for the purpose of measurement of sample trees. —— Ficha para o Cálculo do Volume --

				1 101	ia para c	Calculo						
No.	. Árvore:	s : <u>1</u>	2		Espécie	e : <u>P</u>	elliotti	i		Idade	: 18	
	Data d	a Mediç	ão : _	3 de jun	ho de 19	82		Local :		as de Sa		
No.	Alt.		Diâm	etro à Ai	ltura do /)	Peito		Área	Basal		Volume (v)	
190.	Att.	Com	ı casca (C/c)	Sem	casca (S/c)	C/c	S/c	C/c	S/c	Porc.
		Máx.	Min.	Med.	Máx.	Min.	Med.	(G _b)	(G_i)	(V_b)	(V_i)	1 01 0.
0	m 1.3	cm	cm	cm 28.5	cm	cm	cm 24.1	m²	m²	m ³	m ³	%
1	1.1			29.3			24.1	0.0674	0.0456	0.1348	0.0912	67.66
2	3.1			25.7			22.5	. 0519	. 0398	.1038	. 0796	77.69
3	5.1			25.0			22.2	. 0491	.0387	.0982	. 0774	78.82
4	7.1			24.5			21.7	.0471	.0370	.0942	.0740	78.56
5	9.1			24.0	l .	l .	21.2	. 0452	. 0353	. 0904	.0706	78.10 ¹
6	11.1			21.7			19.8	.0370	. 0308	.0740	.0616	83.24
7	13.1			21.7			19.3	. 0370	. 0293	.0740	. 0586	79.19
8	15.1			16.4			15.0	.0211	.0177	. 0422	. 0354	83.89
9	17.1			13.0			12.0	. 0133	.0113	.0266	.0226	84.96
10	19.1			7.2			6.8	.0041	. 0036	.0082	.0072	87.80
11	21.1			4.5			3.8	.0016	.0011	.0032	.0022	68.75
12	22.1			2.1			1.9	.0003	.0003	.0001	.0001	100.00
13												
14												
15												
16												
17												
18												
(19)	19.3			7.5			6.5	.0044	.0033	.0067	.0051	76.12
(20)	20.5			5.9			5.0	.0027	.0020	.0025	.0019	76.00
D A	P		(D)	28.5			cm 24.1					
Altur	ra		(H)	m 22.8			m 22.8					
Comp	o. do Por	iteiro	(l_T)	m - 0.7			m 0.7					
Comp	o. de Aci	ma de 5.	0 cm (<i>l</i> .05)	m 2.3			m 2.3					
Ārea	Basal T	otal	(ΣG_i)		-			m ² 0.3748	m ² 0.2902			
①Vo	1. das Se	ccoes	(ΣV)							m ³ 0.7496	m ³ 0.5804	
②V0	l. do Cor	ne	(V_T)						-	.0001	.0001	
	②Vol. To		(V _A)							.7497	.5805	% 77.43
3V0	l. Acima	de 5.0 c								.0025	.0019	
V_A - $\overline{3}$	Vol. Co	mercial	(V _B)							.7472	.5786	77.44
Porce	entagem		(%)							% 99.67	% 99.67	
			1/9/			/D		ol · Chyo	**			

(Responsável : Chyo, Haga, Aoki, Adauto, Ataide)

Table 3. List of sample trees (A part of 100 trees data).

	Talhā	io Idade -	DA	AP		Altura	Comp. do (Comp. Acima I	Pont Final
No.	No.	Idade -	C/c	S/c	Н	da <i>COPA</i>	Ponteiro	de 5.0 cm	$(l_{\rm F})$
			cm	cm	m	m	m		m
1	4	20	21.0	17.8	19.1	11.5	1.00	2.11	2.20
2	16	//	13.8	12.0	17.1	10.9	1.04	2.69	2.64
3	11	11	25.0	21.0	19.8	10.8	1.74	2.56	2.94
4	10	11	12.5	10.2	15.1	8.5	0.95	2.95	2.95
5	11	"	8.2	6.7	10.5	5.6	0.40	6.64	5.60
6	11	11	7.7	6.2	8.5	1.8	0.35	4.75	3.55
7	15	11	13.6	12.0	13.3	1.9	1.20	3.07	3.60
8	n	11	15.7	14.3	15.7	7.8	1.60	3.04	3.60
9	11	11	17.5	15.3	16.2	7.8	0.10	1.70	1.70
10	35	18	21.2	19.0	17.6	8.7	1.50	2.60	3.10
	n	"	16.8	14.8	20.0	10.0	1.90	2.90	3.10
12	31	"	28.5	24.1	22.8	14.5	0.70	2.30	3.50
13	12	20	21.8	18.8	19.7	12.2	1.60	2.60	2.80
14	n	"	17.3	15.2	19.5	11.9	1.40	2.65	3.80
15	11	"	15.8	12.8	18.0	11.7	1.90	2.74	3.50
16	"	"	12.0	10.1	16.4	11.3	0.30	3.95	4.30
17	123	13	8.1	7.2	11.5	8.1	1.40	4.40	5.40
18	n	"	10.1	8.4	10.8	6.3	0.70	4.70	4.70
19	"	"	12.0	10.7	12.5	8.3	0.40	2.80	2.80
20	11	11	10.0	8.0	11.2	7.8	1.10	5.95	6.30
21	85	17	14.0	11.8	14.0	6.8	1.90	2.70	3.10
22	"	η	14.0	11.2	12.6	7.4	0.50	3.23	4.10
23	11	11	16.0	13.4	14.0	8.2	1.90	2.65	3.10
24	"	11	18.0	15.2	14.5	7.8	0.40	2.40	2.40
25	11	"	20.0	17.0	15.6	7.8	1.50	2.30	2.30
26	11	1)	14.3	12.0	14.8	8.1	0.70	2.90	3.90
27	118	14	23.4	20.0	15.4	8.0	1.30	2.00	2.10
28	11	"	21.8	18.5	14.4	6.0	0.30	2.30	2.30
29	n	וו	17.5	14.8	14.1	7.2	2.00	2.50	3.30
30	n	n	15.2	13.1	13.2	7.0	1.10	3.50	3.50
31	12	20	26.0	22.5	22.4	11.7	0.30	2.40	3.20
32	"	"	20.0	17.0	21.0	14.6	0.90	2.90	3.00
33	"	"	22.0	19.0	22.7	13.7	0.60	3.30	3.50
34	<i>I)</i>	"	30.0	26.8	22.7	14.0	0.60	2.00	2.30
35	<i>I)</i>	"	24.0	20.2	23.0	13.1 15.4	0.90	3.30	3.80
36	"	<i>II</i>	18.0	16.5	22.0		1.90	2.70	2.80
37	<i>]]</i> 109	1) 17	14.2	12.0	18.6	11.6	0.50	2.20	3.00
38 39	103 <i>11</i>	17))	18.0 18.0	15.5 15.2	17.6 17.2	9.5 12.6	1.50 1.10	2.80 2.70	3.20 2.80
~~~~~	·····		~~~~~	~~~~~	~~~~~	~~~~~	^^^		
91	12	20	16.0	13.2	17.8	9.2	1.70	2.80	3.40
92	"	"	18.0	14.8	19.2	13.5	1.10	3.60	3.60
93	"	"	22.0	18.0	19.7	12.0	1.60	3.20	4.10
94	"	"	28.0	24.7	20.5	10.2	0.40	1.90	2.50
95	"	<i>11</i>	30.0	25.0	20.1	9.7	2.00	2.10	2.10
96	<i>II</i>	<i>])</i>	26.0	23.5	21.5	12.8	1.40	2.00	2.30
97	117	13	16.0	14.0	9.1	4.0	1.00	1.90	1.90
98	<i>!!</i>	<i>))</i>	22.0	19.0	15.7	7.8	1.60	2.50	2.50
99	<i>"</i>	"	14.0	11.0	9.1	5.3	1.00	3.90	4.30
100	11	11	22.0	18.5	14.1	7.1	1.90	2.80	3.20

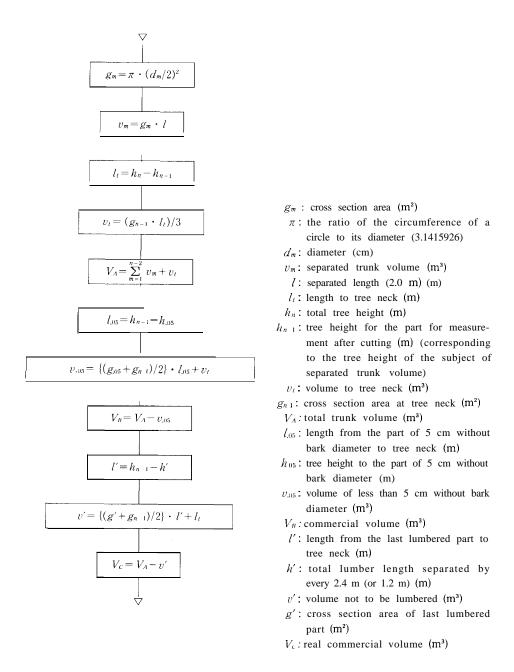


Fig. 1. Flow of volume calculation by computer.

(5)

Table 4. Example of result of volume calculation by computer (sample tree No. 12)

Ficha para o Cálculo do Volume -

N.ARVORES	: 12-(1)		гіспар	arao	Calculo	o do vo	olullie –				
ESPECIE Idade	: P.ELLI : 18	OTTII		_							
DATA LOCAL	: 03/06/	1982 DE SANTA BAR	RARA (31								
LUCAL		DE SANTA DAN	min ()	•							
•	•	. DIAMETRO /				+		BASAL		VOLUME	
• N.		+	++		++	+	+		, +		
+	* +	. MAX. * MIN.								SIC	PORC.
0	1.30	0.0 0.0	28.5	0.0	0.0	24.1		-			
7	1.10										67.66
3	3. 10 5 სე	0.0 0.0 					. 0519 ( <u>ው</u> ያያታሪዮ		0. 1038 09 82 0	0.0796	_ <b>76.69</b> 78,82
4	7.10	0.0 0.0 24	.5 0.0	0.0	21.7 0	.0471	0.0370	0.0942	0. 0	740	78. 56
5 6	9.10	0.0 0.0	21.7	0.0	0.0						
7	13.10	0.0 0.0	21.7	0.0	0.0						
<u>8</u>	15. 10 17. 10	0.0 0.0 -40 JAO 1		0.0	0.0	15.0	0.0211		0. 0422 N. 2. 6	0.0354 0.0226	83. 89 84. 96
10	19.10	0.0 0.0 7.2	2 0.0	0. (0	0.0 60.	0.00	D41 Q.	0036 0.0	280	0. 0072	87. 80
11 12	21.10 22.10	0.0 0.0 0.0 0.0.			.0 0.0 .9			0.0011 3 0.	0. 0032 0001	0. 0022 0. 0001	68. 75 100. 00
								-			
13	19.30 20.50			0.0	0.0	6.5	0.0044	0-0033	0.0067	0.0051	76. 12 7b. 00
		+	++		+	+	·		+		
D. A.	P.	( CM )	28. 50			24. 10	)				
ALTURA	1	( M )	22.80			22. 80	)				
	DO PONTEI	IRO (M)	0. 70			0. 70 2. 30					
AREA I	BASAL TOTA	AL (M**2)	•			۵. 30	0. 3748	0:2902			
	AS SECCO	DES (M**3) (M**3)							0. 7496 0. 0001	0. 5804 0. 0001	
YOL. D		(M**3)						-	0.7497	0. 5805	77. 43
	CIMA DE 5 OMERCIAL	SCM (M**3) (M**3)							0. 0025 0. 7472	0.0019 0.5786	77. 44
PORCEN		( % )							99. 67	99.67	77.44
V =	$a_0 D^{a_1}$										(1)
•											, ,
V =	$a_0 + a_1$	$D^2H$ )									(2)
		·									(0)
V =	$a_0 + (D^2)$	$H)^{a_1}$									(3)
											(4)
V =	$a_0 + D^{a_1}$	$H^{u_2}$									(4)

In order to solve these 5 equations by linear least square method, we apply logarithmic conversion to equation (1), (3) and (4), and the following are obtained.

 $V = a_0 + a_1 D^2 + a_2 H + a_3 (D^2 H)$ 

$$\log \mathbf{V} = \log a_0 + a_1 \log \mathbf{D} \tag{1'}$$

$$\log \mathbf{V} = \log a_0 + a_1 \log (D^2 H) \tag{3'}$$

$$\log V = \log a_0 + a_1 \log \mathbf{D} + a_2 \log \mathbf{H} \tag{4'}$$

When y is substituted for dependent variant,  $x_i$  for an independent variable,  $a_0$  for a regression constant,  $a_i$  for a regression coefficient, these formulae can be expressed in a general formula as below.

 $\textbf{Table} \quad \textbf{5.} \text{List of the calculation results of various volume and ratios on sample trees (A part of 100 trees data).}$ 

N1	D	4P	77	Vol	ume tota	1	Vol.	commerc	ial	Vol.	comme. r	real
No.	c / c	s/c	- <b>H</b>	C/c	s/c	P	C/c	s/c	P	C/c	s/c	P
1 2 3 4 5 6 7 8 9	25.0 12.5 8.2 7.7 13.6 15.7 17.5	cm 17.8 12.0 21.0 10.2 6.7 6.2 12.0 14.3 15.3	19.8 15.1 10.5 8.5 13.3 15.7 16.2	m³ 0.3542 0.1411 0.4758 0.0928 0.0248 0.0200 0.1090 0.1602 0.2450 0.2985	m³ 0.2817 0.1096 0.3776 0.0729 0.0178 0.0140 0.0897 0.1357 0.1998 0.2439	% 79.5 77.7 70.4 78.6 71.8 70.0 82.3 84.7 81.6 81.7	0.1569 0.2429	m³ 0.2803 0.1073 0.3757 0.0705 0.0116 0.0096 0.0874 0.1330 0.1981 0.2418	82.5 84.8 81.6	0.0191 0.0171 0.1039 0.1546 0.2429	0.0119	% 79.6 77.9 79.4 78.7 70.2 69.6 82.4 84.8 81.6 81.8
11 12 13 14 15 16 17 18 19 20	28.5 21.8 17.3 15.8 12.0 8.1 10.1	18.8 15.2 12.8 10.1 7.2 8.4 10.7	22.8 19.7 19.5 18.0 16.4 11.5 10.8	0.2307 0.7497 0.4025 0.2548 0.1859 0.0982 0.0340 0.0389 0.0732 0.0389	0.1886 0.5805 0.3291 0.2035 0.1425 0.0740 0.0283 0.0268 0.0560 0.0255	81.8 79.9 76.7 75.4 83.2 68.9 76.5	0.1829 0.0935 0.0294 0.0324	0.1858 0.5786 0.3271 0.2016 0.1405 0.0703 0.0247 0.0222 0.0531 0.0198	77.4 81.8 79.9 76.8 75.2 84.0 68.5 76.5	0.1804 0.0906 0.0276 0.0324 0.0694	0.2000 0.1387 0.0684 0.0234 0.0222	81.8 77.4 81.8 80.0 76.9 75.5 84.8 68.5 76.5 61.0
21 22 23 24 25 26 27 28 29 30	14.0 16.0 18.0 20.0 14.3 23.4 21.8 17.5	11.8 11.2 13.0 15.2 17.0 12.0 20.0 18.5 14.8	12.6 14.0 14.5 15.6 14.8 15.4 14.4	0.1050 0.0911 0.1514 0.2014 0.2476 0.1195 0.3485 0.2674 0.1656 0.1090	0.0782 0.0664 0.1077 0.1536 0.1973 0.0924 0.2797 0.2048 0.1315 0.0837	76.3 79.7 77.3 80.3 76.6 79.4	0.1489 0.1987 0.2448 0.1161 0.3466 0.2646		72.7 71.1 76.3 79.6 77.5 80.3 76.6 79.5	0.1014 0.0847 0.1475 0.1987 0.2448 0.1127 0.3462 0.2646 0.1608 0.1047	0.0617 0.1049 0.1516 0.1949 0.0876	74.6 72.9 71.1 76.3 79.6 77.7 80.3 76.6 79.5 76.8
31 32 33 34 35 36 37 38	20.0 22.0 30.0 24.0 18.0 14.2	22.5 17.0 19.0 26.8 20.2 16.5 12.0 15.5	21.0 22.7 22.7 23.0 22.0 18.6 17.6	0.6696 0.3188 0.4219 0.8803 0.5134 0.3095 0.1613 0.2281 0.2200	0.5372 0.2627 0.3484 0.7575 0.4324 0.2620 0.1384 0.1906 0.1755	82.4 82.6 86.1 84.2 84.7 85.8 83.6 79.8	0.3064 0.1359 .0.2254 0.2172	0.5350 0.2603 0.3454 0.7557 0.4292 0.2596 0.1185 0.1884 0.1735	82.5 82.6 86.1 84.2 84.7 87.2 83.6 79.9	0.3153 0.4166 0.8773 0.5075 0.3062 0.1331 0.2239 0.2171	0.2594 0.1158 0.1873 0.1734	79.9
91 92 93 94 95 96 97 98 99	18.0 22.0 28.0 30.0 26.0 16.0 22.0 14.0	14.8 18.0 24.7 25.6 23.5 14.0 19.0 11.0	17.8 19.2 19.7 20.5 20.1 21.5 9.1 15.7 9.1	0.1723 0.2325 0.3546 0.6355 0.6868 0.6971	0.1350 0.1812 0.2809 0.5308 0.5590 0.5919 0.0708 0.2189 0.0407 0.1906	78.4 77.9 79.2 83.5 81.4 84.9 78.8 80.8 68.6	0.1695 0.2283 0.3512 0.6333 0.6849 0.6956 0.0878 0.2686 0.0550	0.1327 0.1779 0.2781 0.5291 0.5576 0.5908 0.0694 0.2171 0.0374 0.1884	78.3 77.9 79.2 83.6 81.4 84.9 79.0 80.8 68.0	0.1681 0.2283 0.3479 0.6310 0.6849 0.6948 0.0878 0.2686 0.0529 0.2414	0.1316 0.1779 0.2755 0.5272 0.5576 0.5902 0.0694 0.2171 0.0360 0.1862	78.3 77.9 79.2 83.6 81.4 85.0 79.0 80.8 68.1

$$y = a_0 + \sum_{i=1}^{P} a_i x_i \tag{6}$$

where, P = 1, 2, 3

Here formula (6) is called a linear multiple regression formula. Therefore, in order to determine a volume formula to be adopted, apply each material obtained to five formulae, evaluate their adaptability, and determine the formula furnishing the least value of standard errors for each of residual. Table 6 indicates only the standard errors of residual, out of series of calculation results due to the multiple regression formula programme. In addition, standard error (SE) are acquired by formula (7) (In this formula, n: number of samples, k: number of independent variables, v: real volume,  $\hat{v}$ : estimated volume).

$$SE = \left\{ \frac{1}{n - (k + 1)} \sum_{i=1}^{n} (v - \hat{v})^2 \right\}^{\frac{1}{2}}$$
 (7)

Kin	nd	(1')	(2)	(3')	(4')	(5)
Total tree volume formula	①with bark	0.05828	0.02134	0.02107	0.01990	0.01089
	@without bark	0.05105	0.02129	0.02109	0.02000	0.01986
Commercial volume formula	@with bark	0.05998	0.02135	0.02345	0.02264	0.02020
	@without bark	0.05388	0.02120	0.02566	0.02485	0.01999
Real commercial volume formula	@with bark	0.06011	0.02126	0.02322	0.02219	0.02028
	@without bark	0.05417	0.02143	0.02580	0.02488	0.02008

Table 6. Standard errors of residual

However, standard error determined by the logarithmic formula cannot be simply compared with that by the non-logarithmic formula. For such purpose, when standard errors in (1'), (3') and (4') formula in Table 6 are demanded, calculate by substituting  $\hat{v}$  multiplied by correction factor (c. f.), which is given in formula (8), for  $\hat{v}$  in formula (7). (Where,  $S_{yx_1x_2^2}$ : standard error of residual).

$$c. f. = 10^{\frac{n-1}{n}} Syx_1 x_2^{2 \cdot 1.151293}$$
(8)

As the result of the above calculation, the standard error of residual became minimum in formula (5) for any of volume formula (See Table 6). Hence, we decided to adopt formula (5), which is called Australian formula, for our volume calculation.

Further, in order to examine the effect of independent variable in formula (5) to dependent variable, a significance test in partial regression coefficient in each volume formula was conducted by the formula as below, under a null hypothesis ( $H: a_i = 0$ ), where partial regression coefficient,  $a_i$  is assumed 0,

$$t = \frac{a_i}{\sqrt{S^{ii}V_e}} \ge t \text{ (n-P-1; } \alpha)$$

where,  $S^{ii}$ : reverse matrix in matrix of deviation square sum and product

sum,  $V_e$ : error variance

The result was obtained as in Table 7, showing the second variable ( $x_2 = H$ ) was eliminated in all formulae of volume. Therefore, the formula of volume was determined as formula (9).

$$V = a_0 + a_1 D^2 + a_2 (D^2 H) (9)$$

Next, in order to prevent the effect of abnormal material to the estimated volume, a rejecting zone, when formula (9) was applied, was calculated by formula (10) (where, t: value of t at 99 % level when freedom is n-3,  $s_{yx_1x_2}$ : error variance,  $V(\hat{v})$ : variance of estimated value  $\hat{v}$ ).

$$E_{yx_1x_2} = t \left\{ S_{yx_1x_2} - V(\hat{v})^{\frac{1}{2}} \right\}$$
 (10)

Compare  $E_{yx_1x_2}$  obtained by formula (10) with variance  $v-\hat{v}$  from regression, and reject i-th sample when  $E_{yx_1x_2} < |v_i - \hat{v}_i|$  exists. As the result, material No. 94 was rejected in total volume formulae, and material No. 98 was rejected in formulae with bark.

#### **RESULTS**

In linear regression model, there is a provision that the relation among variable is linear over the whole range of materials. But in this case, since the number of samples are only 100, and the range is narrow, as 8 cm-30 cm in diameter, and 7 m- 23 m in height, one volume formula is taken for the whole diameter grade, as follows. (Application of volume formula is omitted.)

① Total tree volume with bark formula:

$$\hat{V} = 0.00674609 - 0.00012281D^2 + 0.00004552D^2H \qquad (E = 14.96)$$

② Total tree volume without bark formula:

$$\hat{V} = 0.00226291 - 0.00009136D^2 + 0.00003656D^2H \qquad (E = 16.66)$$

(3) Commercial volume with bark formula:

$$\hat{V} = 0.00113217 - 0.00010899D^2 + 0.00004506D^2H \qquad (E = 15.46)$$

(4) Commercial volume without bark formula:

$$\hat{V} = -0.00204230 - 0.00008071D^2 + 0.00003621D^2H \qquad (E = 17.05)$$

⑤ Real commercial volume with bark formula:

$$\hat{V} = 0.00116770 - 0.00011814D^2 + 0.00004539D^2H \qquad (E = 15.61)$$

6 Real commercial volume without bark formula:

$$\hat{V} = -0.00200872 - 0.00008761D^2 + 0.00003644D^2H$$
 (E = 17.20)

The analysis resulted in 6 different volume equations, and based on these equations, 6 different stumpage volume tables for *Pinus elliottii* has been contracted (The

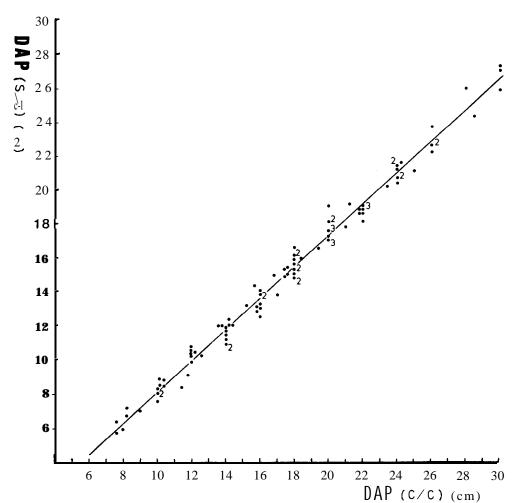
771	,	37 1.1	Partial	95 % confider	nce limit of $a_i$	Standard	Standard partial regression	t-test
Kir	nd	Variable	regression coefficient	Upper limit	Lower limit	error	coefficients	r-test
Total tree	with	$x_1$	-0.00015592	-0.000242	-0.000069	0.0000	-0.1768836	- 3.581**
volume	bark	$x_2$	-0.00044804	-0.002418	0.001522	0.0010	-0.0099104	- 0.451
formula	1	$x_3$	0.00004781	0.000042	0.000052	0.0000	1.1713886	19.412**
	without	$\chi_{_{1}}$	-0.00015530	-0.000241	-0.000069	0.0000	-0.2113804	- 3.573**
	bark	$x_2$	-0.00046669	-0.002433	0.001500	0.0010	-0.0123852	-0.471
	2	<i>x</i> ₃	0.00004095	0.000036	0.000045	0.0000	1.2036333	16.654**
Commercial	with	$x_1$	-0.00014332	-0.000231	-0.000055	0.0000	-0.1619246	- 3.241**
volume	bark	$x_2$	-0.00048609	-0.002486	0.001514	0.0010	-0.0107079	-0.482
formula	3	$x_3$	0.00004744	0.000042	0.000052	0.0000	1.1576738	18.971**
	without	$x_{i}$	-0.00014617	-0.000233	-0.000059	0.0000	-0.1982326	- 3.340**
	bark	$x_2$	-0.00051635	-0.002469	0.001463	0.0010	-0.0136536	-0.518
	4	<i>x</i> ₃	0.00004070	0.000035	0.000045	0.0000	1.1921310	16.442**
Real	with	$x_1$	-0.00015342	-0.000241	-0.000065	0.0000	-0.1736585	- 3.455 <b>**</b>
commercial	bark	$x_2$	-0.00051834	-0.002527	0.001490	0.0010	-0.0114392	-0.512
volume formula	5	$x_3$	0.00004874	0.000042	0.000052	0.0000	1.1693535	19.047**
	without	$x_1$	-0.00015377	-0.000241	-0.000066	0.0000	-0.2088885	- 3.498**
	bark	$x_2$	-0.00053076	-0.002519	0.001458	0.0010	-0.0140581	-0.530
	6	x ₃	0.00004099	0.000036	0.000045	0.0000	1.2024670	16.484**

Table 7. Test of partial regression coefficient.

volume tables are not presented in this paper). Volume tables were made, corresponding to the forest stands, for the range of diameter of 6 cm-34 cm graded by 1 cm, and for the tree height of 5 m-25 m graded by 1 m. The volume tables were indicated in any case in values of diameter with bark, because it was impossible to measure diameter without bark. Therefore, by measuring a diameter with bark, volumes without bark are estimated.

By the way, the relation between diameter with bark (x) and diameter without bark (Y) is as shown in Fig. 2 and the regression formula and the coefficient of correlation are as follows.

$$\mathbf{Y} = 0.962 + 0.909x \qquad (r = 0.989)$$



**Fig. 2.** Relation between with bark diameter at breast height (DAP, C/c) and without bark diameter at breast height (DAP, S/c).

(Y = -0.962 + 0.909x, r = 0.989)

#### DISCUSSION

The six kinds of tree volume equations were made for study of adjustment methods, but hereby some consideration was attempted on the adjusted volume equations.

First, on 98 samples left after 2 extraordinary ones were discarded out of 100 sample trees which were selected and cut in a forest stand, the relation between diameter at breast height (DAP) with bark D and tree height D were as follows.

$$H = 3.759 + 0.790D - 0.008D^2$$
 ( $\gamma = 0.694$ )

When these data are shown on a graph, the distribution indicates scattering to some extent, so the coefficient of correlation cannot be regarded high. But this is the result of that sample trees were intentionally collected so that tree height might distribute in a certain range by each diameter grade. The scattering of this extent is often seen in any forest stand. Viewed from another angle, it means that such scattering as this extent always exists due to the different places or different land positions even in the same state forest of Águas de Santa Barbara.

Next, the relation between bark and volume without bark are as in Table 8.

	Viud of column			Correlation		
	Kind of volume	$a_0$	$a_1$	a2	coefficient	
With	(1)Tatol tree volume	0.08603	-0.01649	0.00127	0.895	
bark	@Commercial volume	0.07084	-0.01591	0.00126	0.897	
	⑤Real commercial volume	0.06875	-0.01567	0.00125	0.895	
Without	@Total tree volume	0.03923	-0.01118	0.00122	0.890	
bark	@Commercial volume	0.03400	-0.01106	0.00123	0.892	
	@Real commercial volume	0.03480	-0.01117	0.00123	0.890	

**Table 8.** List of parameter and correlation coefficients in the regression formula of diameter to volume.

From Table 8, in case of with bark, the regression formula is formed with nearly similar tendency in (1), (3), and (5). The volume was as (1) > (3) > (5), so the values of parameter became a little smaller in order of (1), (3), and (5). In three of (2), (4), and (6), the values of parameter became smaller than those with bark. But the order is not definite as the former three. The coefficients of correlation are generally in a range between (1), (2), and (3), and

The relation between total volume with bark and other volume, between commercial volume with bark and those without bark, and between real volume with bark and that without bark are shown in Table 9.

From Table 9, in all formulae the coefficients of correlation are as high as in a range of 0.997-0.999, showing good correspondence. Regarding individual formula, (b) and (d) show hardly any difference on a graph. On the contrary, in (a),(c), and (e), volume values are much smaller than the total volume with bark. The cases of(f) and (g) show the same tendency. So it is inferable that the main cause for the difference

Table 9. List of parameters and correlation coefficients in regression formulae based on the corresponding volume.

Concerned formula	Parar	meter	Correlation
Concerned formula	au	$a_1$	coefficient
(a) Total volume with bark to total volume without bark	-0.006	0.832	0.998
(b) Total volume with bark to commercial volume with bark	-0.004	1.004	0.999
(c) Total volume with bark to commercial volume without bark	-0.006	0.829	0.999
(d) Total volume with bark to real commercial volume with bark	-0.005	1.002	0.999
(e) Total volume with bark to real commercial volume without bark	-0.010	0.834	0.997
(f) Commercial volume with bark to commercial volume without bark	0.006	0.832	0.998
(g) Real commercial volume with bark to real commercial volume without bark	0.004	0.829	0.998

exists in bark. It is guessed that is probably the reason why São Paulo state measures the volume with bark always together with the volume without bark. By the way, the result of stem analysis carried on *Pinus elliottii* of 21 years age (DAP = 22.0 cm, H = 22.1 m, Talhão No. 15) in the same state forest of Águas de Santa Barbara, indicated total volume without bark 0.3331 m³ against total volume with bark 0.4109 m³, showing bark ratio of 18.93 %.

Here, consideration is mainly limited to the relating formulae corresponding to breast height diameter and various volumes, on basis of 6 different volume formulase. However, the problem is whether the prepared volume value would be adaptable to the actual measurement or not. In this respect, we must wait for the field study result.

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