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Goto, Keisuke Department of Informatics, Kyushu University

Bannai, Hideo Department of Informatics, Kyushu University

Inenaga, Shunsuke Department of Informatics, Kyushu University

Masayuki, Takeda Department of Informatics, Kyushu University

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Fast q-gram Mining on SLP Compressed Strings*

Keisuke Goto, Hideo Bannai, Shunsuke Inenaga, and Masayuki Takeda

Department of Informatics, Kyushu University {keisuke.gotou,bannai,inenaga,takeda}@inf.kyushu-u.ac.jp

Abstract. We present simple and efficient algorithms for calculating q-gram frequencies on strings represented in compressed form, namely, as a straight line program (SLP). Given an SLP of size n that represents string T, we present an O(qn) time and space algorithm that computes the occurrence frequencies of $all\ q$ -grams in T. Computational experiments show that our algorithm and its variation are practical for small q, actually running faster on various real string data, compared to algorithms that work on the uncompressed text. We also discuss applications in data mining and classification of string data, for which our algorithms can be useful.

1 Introduction

A major problem in managing large scale string data is its sheer size. Therefore, such data is normally stored in compressed form. In order to utilize or analyze the data afterwards, the string is usually decompressed, where we must again confront the size of the data. To cope with this problem, algorithms that work directly on compressed representations of strings without explicit decompression have gained attention, especially for the string pattern matching problem [1] where algorithms on compressed text can actually run faster than algorithms on the uncompressed text [23]. There has been growing interest in what problems can be efficiently solved in this kind of setting [17,8].

Since there exist many different text compression schemes, it is not realistic to develop different algorithms for each scheme. Thus, it is common to consider algorithms on texts represented as *straight line programs* (SLPs) [12,17,8]. An SLP is a context free grammar in the Chomsky normal form that derives a single string. Texts compressed by any grammar-based compression algorithms (e.g. [21,15]) can be represented as SLPs, and those compressed by the LZ-family (e.g. [24,25]) can be quickly transformed to SLPs [22]. Recently, even *compressed self-indices* based on SLPs have appeared [6], and SLPs are a promising representation of compressed strings for conducting various operations.

In this paper, we explore a more advanced field of application for compressed string processing: mining and classification on string data given in compressed form. Discovering useful patterns hidden in strings as well as automatic and accurate classification of strings into various groups, are important problems in

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the field of data mining and machine learning with many applications. As a first step toward *compressed* string mining and classification, we consider the problem of finding the occurrence frequencies for all q-grams contained in a given string. q-grams are important features of string data, widely used for this purpose in many fields such as text and natural language processing, and bioinformatics.

In [10], an $O(|\Sigma|^2n^2)$ -time $O(n^2)$ -space algorithm for finding the most frequent 2-gram from an SLP of size n representing text T over alphabet Σ was presented. In [6], it is mentioned that the most frequent 2-gram can be found in $O(|\Sigma|^2n\log n)$ -time and $O(n\log |T|)$ -space, if the SLP is pre-processed and a self-index is built. It is possible to extend these two algorithms to handle q-grams for q>2, but would respectively require $O(|\Sigma|^qqn^2)$ and $O(|\Sigma|^qqn\log n)$ time, since they must essentially enumerate and count the occurrences of all substrings of length q, regardless of whether the q-gram occurs in the string. Note also that any algorithm that works on the uncompressed text T requires exponential time in the worst case, since |T| can be as large as $O(2^n)$.

The main contribution of this paper is an O(qn) time and space algorithm that computes the occurrence frequencies for all q-grams in the text, given an SLP of size n representing the text. Our new algorithm solves the more general problem and greatly improves the computational complexity compared to previous work. We also conduct computational experiments on various real texts, showing that when q is small, our algorithm and its variation actually run faster than algorithms that work on the uncompressed text.

Our algorithms have profound applications in the field of string mining and classification, and several applications and extensions are discussed. For example, our algorithm leads to an $O(q(n_1+n_2))$ time algorithm for computing the q-gram spectrum kernel [16] between SLP compressed texts of size n_1 and n_2 . It also leads to an O(qn) time algorithm for finding the optimal q-gram (or emerging q-gram) that discriminates between two sets of SLP compressed strings, when n is the total size of the SLPs.

Related Work There exist many works on compressed text indices [20], but the main focus there is on fast search for a given pattern. The compressed indices basically replace or simulate operations on uncompressed indices using a smaller data structure. Indices are important for efficient string processing, but note that simply replacing the underlying index used in a mining algorithm will generally increase time complexities of the algorithm due to the extra overhead required to access the compressed index. On the other hand, our approach is a new mining algorithm which exploits characteristics of the compressed representation to achieve faster running times.

Several algorithms for finding characteristic sequences from compressed texts have been proposed, e.g., finding the longest common substring of two strings [19], finding all palindromes [19], finding most frequent substrings [10], and finding the longest repeating substring [10]. However, none of them have reported results of computational experiments, implying that this paper is the first to show the practical usefulness of a compressed text mining algorithm.

Algorithm 1: Calculating $vOcc(X_i)$ for all $1 \le i \le n$.

```
Input: SLP \mathcal{T} = \{X_i\}_{i=1}^n representing string T.

Output: vOcc(X_i) for all 1 \le i \le n

1 vOcc[X_n] \leftarrow 1;

2 for i \leftarrow 1 to n - 1 do vOcc[X_i] \leftarrow 0;

3 for i \leftarrow n to 2 do

4 | if X_i = X_\ell X_r then

5 | vOcc[X_\ell] \leftarrow vOcc[X_\ell] + vOcc[X_i]; vOcc[X_r] \leftarrow vOcc[X_r] + vOcc[X_i];
```

2 Preliminaries

Let Σ be a finite alphabet. An element of Σ^* is called a *string*. For any integer q > 0, an element of Σ^q is called an q-gram. The length of a string T is denoted by |T|. The empty string ε is a string of length 0, namely, $|\varepsilon| = 0$. For a string T = XYZ, X, Y and Z are called a prefix, substring, and suffix of T, respectively. The i-th character of a string T is denoted by T[i] for $1 \le i \le |T|$, and the substring of a string T that begins at position i and ends at position j is denoted by T[i:j] for $1 \le i \le j \le |T|$. For convenience, let $T[i:j] = \varepsilon$ if j < i.

For a string T and integer $q \ge 0$, let pre(T,q) and suf(T,q) represent respectively, the length-q prefix and suffix of T. That is, $pre(T,q) = T[1 : \min(q,|T|)]$ and $suf(T,q) = T[\max(1,|T|-q+1):|T|]$.

For any strings T and P, let Occ(T, P) be the set of occurrences of P in T, i.e., $Occ(T, P) = \{k > 0 \mid T[k : k + |P| - 1] = P\}$. The number of elements |Occ(T, P)| is called the *occurrence frequency* of P in T.

2.1 Straight Line Programs

A straight line program (SLP) \mathcal{T} is a sequence of assignments $X_1 = expr_1, X_2 = expr_2, \ldots, X_n = expr_n$, where each X_i is a variable and each $expr_i$ is an expression, where $expr_i = a \ (a \in \Sigma)$, or $expr_i = X_\ell X_r \ (\ell, r < i)$. Let $val(X_i)$ represent the string derived from X_i . When it is not confusing, we identify a variable X_i with $val(X_i)$. Then, $|X_i|$ denotes the length of the string X_i derives. An SLP \mathcal{T} represents the string $T = val(X_n)$. The size of the program \mathcal{T} is the number n of assignments in \mathcal{T} . (See Fig. 1)

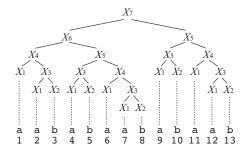


Fig. 1. The derivation tree of SLP $\mathcal{T} = \{X_i\}_{i=1}^7$ with $X_1 = \mathsf{a}, X_2 = \mathsf{b}, X_3 = X_1X_2, X_4 = X_1X_3, X_5 = X_3X_4, X_6 = X_4X_5,$ and $X_7 = X_6X_5$, representing string $T = val(X_7) = \mathsf{aababaababaab}$.

The substring intervals of T that each variable derives can be defined recursively as follows: $itv(X_n) = \{[1:|T|]\}$, and $itv(X_i) = \{[u+|X_\ell|:v] \mid X_k = X_\ell X_i, [u:v] \in itv(X_k)\} \cup \{[u:u+|X_i|-1] \mid X_k = X_i X_r, [u:v] \in itv(X_k)\}$ for

Algorithm 2: A naïve algorithm for computing q-gram frequencies.

```
Input: string T, integer q \ge 1

Report: (P, |Occ(T, P)|) for all P \in \Sigma^q where Occ(T, P) \ne \emptyset.

1 \mathbf{S} \leftarrow \emptyset; // empty associative array

2 for i \leftarrow 1 to |T| - q + 1 do

3 |qgram \leftarrow T[i:i+q-1];

4 if qgram \in \text{keys}(\mathbf{S}) then \mathbf{S}[qgram] \leftarrow \mathbf{S}[qgram] + 1;

5 |qgram| \leftarrow 1; // new q-gram

6 for qgram \in \text{keys}(\mathbf{S}) do Report (qgram, \mathbf{S}[qgram])
```

i < n. For example, $itv(X_5) = \{[4:8], [9:13]\}$ in Fig. 1. Considering the transitive reduction of set inclusion, the intervals $\bigcup_{i=1}^n itv(X_i)$ naturally form a binary tree (the derivation tree). Let $vOcc(X_i) = |itv(X_i)|$ denote the number of times a variable X_i occurs in the derivation of T. $vOcc(X_i)$ for all $1 \le i \le n$ can be computed in O(n) time by a simple iteration on the variables, since $vOcc(X_n) = 1$ and for i < n, $vOcc(X_i) = \sum \{vOcc(X_k) \mid X_k = X_\ell X_i\} + \sum \{vOcc(X_k) \mid X_k = X_i X_r\}$. (See Algorithm 1)

2.2 Suffix Arrays and LCP Arrays

The suffix array SA [18] of any string T is an array of length |T| such that SA[i] = j, where T[j:|T|] is the i-th lexicographically smallest suffix of T. The lcp array of any string T is an array of length |T| such that LCP[i] is the length of the longest common prefix of T[SA[i-1]:|T|] and T[SA[i]:|T|] for $2 \le i \le |T|$, and LCP[1] = 0. The suffix array for any string of length |T| can be constructed in O(|T|) time (e.g. [11]) assuming an integer alphabet. Given the text and suffix array, the lcp array can also be calculated in O(|T|) time [13].

3 Algorithm

3.1 Computing q-gram Frequencies on Uncompressed Strings

We describe two algorithms (Algorithm 2 and Algorithm 3) for computing the q-gram frequencies of a given uncompressed string T.

A naïve algorithm for computing the q-gram frequencies is given in Algorithm 2. The algorithm constructs an associative array, where keys consist of q-grams, and the values correspond to the occurrence frequencies of the q-grams. The time complexity depends on the implementation of the associative array, but requires at least O(q|T|) time since each q-gram is considered explicitly, and the associative array is accessed O(|T|) times: e.g. $O(q|T|\log |\mathcal{L}|)$ time and O(q|T|) space using a simple trie.

The q-gram frequencies of string T can be calculated in O(|T|) time using suffix array SA and lcp array LCP, as shown in Algorithm 3. For each $1 \le i \le |T|$, the suffix SA[i] represents an occurrence of q-gram T[SA[i]:SA[i]+q-1], if the

Algorithm 3: A linear time algorithm for computing q-gram frequencies.

```
Input: string T, integer q \ge 1

Report: (i, |Occ(T, P)|) for all P \in \Sigma^q and some position i \in Occ(T, P).

1 SA \leftarrow SUFFIXARRAY(T); LCP \leftarrow LCPARRAY(T, SA); count \leftarrow 1;

2 for i \leftarrow 2 to |T| + 1 do

3 | if i = |T| + 1 or LCP[i] < q then

4 | _ if count > 0 then Report (SA[i-1], count); count \leftarrow 0;

5 | if i \le |T| and SA[i] \le |T| - q + 1 then count \leftarrow count + 1;
```

suffix is long enough, i.e. $SA[i] \leq |T| - q + 1$. The key is that since the suffixes are lexicographically sorted, intervals on the suffix array where the values in the lcp array are at least q represent occurrences of the same q-gram. The algorithm runs in O(|T|) time, since SA and LCP can be constructed in O(|T|). The rest is a simple O(|T|) loop. A technicality is that we encode the output for a q-gram as one of the positions in the text where the q-gram occurs, rather than the q-gram itself. This is because there can be a total of O(|T|) different q-grams, and if we output them as length-q strings, it would require at least O(q|T|) time.

3.2 Computing q-gram Frequencies on SLP

We now describe the core idea of our algorithms, and explain two variations which utilize variants of the two algorithms for uncompressed strings presented in Section 3.1. For q=1, the 1-gram frequencies are simply the frequencies of the alphabet and the output is $(a, \sum \{vOcc(X_i) \mid X_i = a\})$ for each $a \in \Sigma$, which takes only O(n) time. For $q \geq 2$, we make use of Lemma 1 below. The idea is similar to the mk Lemma [5], but the statement is more specific.

Lemma 1. Let $\mathcal{T} = \{X_i\}_{i=1}^n$ be an SLP that represents string T. For an interval [u:v] $(1 \le u < v \le |T|)$, there exists exactly one variable $X_i = X_\ell X_r$ such that for some $[u':v'] \in itv(X_i)$, the following holds: $[u:v] \subseteq [u':v']$, $u \in [u':u'+|X_\ell|-1] \in itv(X_\ell)$ and $v \in [u'+|X_\ell|:v'] \in itv(X_r)$.

Proof. Consider length 1 intervals [u:u] and [v:v] corresponding to leaves in the derivation tree. X_i corresponds to the lowest common ancestor of these intervals in the derivation tree.

From Lemma 1, each occurrence of a q-gram $(q \geq 2)$ represented by some length-q interval of T, corresponds to a single variable $X_i = X_\ell X_r$, and is split in two by intervals corresponding to X_ℓ and X_r . On the other hand, consider all length-q intervals that correspond to a given variable. Counting the frequencies of the q-grams they represent, and summing them up for all variables give the frequencies of all q-grams of T.

 X_i X_i X_r X_r

Fig. 2. Length-q intervals corresponding to $X_i = X_{\ell}X_r$.

For variable $X_i = X_\ell X_r$, let $t_i = suf(X_\ell, q-1)pre(X_r, q-1)$. Then, all q-grams represented by length q intervals that correspond to X_i are those in t_i . (Fig. 2). If we obtain the frequencies of all q-grams in t_i , and then multiply each frequency by $vOcc(X_i)$, we obtain frequencies for the q-grams occurring in all intervals derived by X_i . It remains to sum up the q-gram frequencies of t_i for all $1 \le i \le n$. We can regard it as obtaining the weighted q-gram frequencies in the set of strings $\{t_1, \ldots, t_n\}$, where each q-gram in t_i is weighted by $vOcc(X_i)$.

We further reduce this problem to a weighted q-gram frequency problem for a single string z as in Algorithm 4. String z is constructed by concatenating t_i such that $q \leq |t_i| \leq 2(q-1)$, and the weights of q-grams starting at each position in z is held in array w. On line 8, 0's instead of $vOcc(X_i)$ are appended to w for the last q-1 values corresponding to t_i . This is to avoid counting unwanted q-grams that are generated by the concatenation of t_i to z on line 6, which are not substrings of each t_i . The weighted q-gram frequency problem for a single string (Line 9) can be solved with a slight modification of Algorithm 2 or 3. The modified algorithms are shown respectively in Algorithms 5 and 6.

Theorem 1. Given an SLP $\mathcal{T} = \{X_i\}_{i=1}^n$ of size n representing a string T, the q-gram frequencies of T can be computed in O(qn) time for any q > 0.

Proof. Consider Algorithm 4. The correctness is straightforward from the above arguments, so we consider the time complexity. Line 1 can be computed in O(n) time. Line 2 can be computed in O(qn) time by a simple dynamic programming. For pre(): If $X_i = a$ for some $a \in \Sigma$, then $pre(X_i, q - 1) = a$. If $X_i = X_\ell X_r$ and $|X_\ell| \ge q - 1$, then $pre(X_i, q - 1) = pre(X_\ell, q - 1)$. If $X_i = X_\ell X_r$ and $|X_\ell| < q - 1$, then $pre(X_i, q - 1) = pre(X_\ell, q - 1)pre(X_r, q - 1 - |X_\ell|)$. The strings suf() can be computed similarly. The computation amounts to copying O(q) characters for each variable, and thus can be done in O(qn) time. For the loop at line 4, since the length of string t_i appended to z, as well as the number of elements appended to w is at most 2(q-1) in each loop, the total time complexity is O(qn). Finally, since the length of z and w is O(qn), line 9 can be calculated in O(qn) time using the weighted version of Algorithm 3 (Algorithm 6).

Note that the time complexity for using the weighted version of Algorithm 2 for line 9 of Algorithm 4 would be at least $O(q^2n)$: e.g. $O(q^2n\log |\Sigma|)$ time and $O(q^2n)$ space using a trie.

4 Applications and Extensions

We showed that for an SLP \mathcal{T} of size n representing string T, q-gram frequency problems on T can be reduced to weighted q-gram frequency problems on a string z of length O(qn), which can be much shorter than T. This idea can further be applied to obtain efficient compressed string processing algorithms for interesting problems which we briefly introduce below.

Algorithm 4: Calculating q-gram frequencies of an SLP for $q \geq 2$

```
Input: SLP T = \{X_i\}_{i=1}^n representing string T, integer q \geq 2.

Report: all q-grams and their frequencies which occur in T.

1 Calculate vOcc(X_i) for all 1 \leq i \leq n;

2 Calculate pre(X_i, q - 1) and suf(X_i, q - 1) for all 1 \leq i \leq n - 1;

3 z \leftarrow \varepsilon; w \leftarrow [];

4 for i \leftarrow 1 to n do

5  | if X_i = X_\ell X_r and |X_i| \geq q then

6  | t_i = suf(X_\ell, q - 1)pre(X_r, q - 1); z.append(t_i);

7  | for j \leftarrow 1 to |t_i| - q + 1 do w.append(vOcc(X_i));

8  | for j \leftarrow 1 to q - 1 do w.append(0);

9 Report q-gram frequencies in z, where each q-gram z[i:i+q-1] is weighted by w[i].
```

Algorithm 5: A variant of Algorithm 2 for weighted q-gram frequencies.

```
Input: string T, array of integers w of length |T|, integer q \ge 1

Report: (P, \sum_{i \in Occ(T,P)} w[i]) for all P \in \Sigma^q where \sum_{i \in Occ(T,P)} w[i] > 0.

1 S \leftarrow \emptyset; // empty associative array

2 for i \leftarrow 1 to |T| - q + 1 do

3 |qgram \leftarrow T[i:i+q-1];

4 if qgram \in \text{keys}(S) then S[qgram] \leftarrow S[qgram] + w[i];

5 |qgram| \in \text{keys}(S) do Report |qgram| \in w[i]; // new |qgram| \in w[i]
```

4.1 q-gram Spectrum Kernel

A string kernel is a function that computes the inner product between two strings which are mapped to some feature space. It is used when classifying string or text data using methods such as Support Vector Machines (SVMs), and is usually the dominating factor in the time complexity of SVM learning and classification. A q-gram spectrum kernel [16] considers the feature space of q-grams. For string T, let $\phi_q(T) = (|Occ(T,p)|)_{p \in \Sigma^q}$. The kernel function is defined as $K_q(T_1,T_2) = \langle \phi_q(T_1), \phi_q(T_2) \rangle = \sum_{p \in \Sigma^q} |Occ(T_1,p)||Occ(T_2,p)|$. The calculation of the kernel function amounts to summing up the product of occurrence frequencies in strings T_1 and T_2 for all q-grams which occur in both T_1 and T_2 . This can be done in $O(|T_1| + |T_2|)$ time using suffix arrays. For two SLPs T_1 and T_2 of size n_1 and n_2 representing strings T_1 and T_2 , respectively, the q-gram spectrum kernel $K_q(T_1,T_2)$ can be computed in $O(q(n_1+n_2))$ time by a slight modification of our algorithm.

4.2 Optimal Substring Patterns of Length q

Given two sets of strings, finding string patterns that are frequent in one set and not in the other, is an important problem in string data mining, with many

Algorithm 6: A variant of Algorithm 3 for weighted q-gram frequencies.

problem formulations and the types of patterns to be considered, e.g.: in Bioinformatics [3], Machine Learning (optimal patterns [2]), and more recently KDD (emerging patterns [4]). A simple optimal q-gram pattern discovery problem can be defined as follows: Let $\mathbf{T_1}$ and $\mathbf{T_2}$ be two multisets of strings. The problem is to find the q-gram p which gives the highest (or lowest) score according to some scoring function that depends only on $|\mathbf{T_1}|$, $|\mathbf{T_2}|$, and the number of strings respectively in $\mathbf{T_1}$ and $\mathbf{T_2}$ for which p is a substring. For uncompressed strings, the problem can be solved in O(N) time, where N is the total length of the strings in both $\mathbf{T_1}$ and $\mathbf{T_2}$, by applying the algorithm of [9] to two sets of strings. For the SLP compressed version of this problem, the input is two multisets of SLPs, each representing strings in $\mathbf{T_1}$ and $\mathbf{T_2}$. If n is the total number of variables used in all of the SLPs, the problem can be solved in O(qn) time.

4.3 Different Lengths

The ideas in this paper can be used to consider all substrings of length not only q, but all lengths up-to q, with some modifications. For the applications discussed above, although the number of such substrings increases to $O(q^2n)$, the O(qn) time complexity can be maintained by using standard techniques of suffix arrays [7, 13]. This is because there exist only O(qn) substring with distinct frequencies (corresponding to nodes of the suffix tree), and the computations of the extra substrings can be summarized with respect to them.

5 Computational Experiments

We implemented 4 algorithms (NMP, NSA, SMP, SSA) that count the frequencies of all q-grams in a given text. NMP (Algorithm 2) and NSA (Algorithm 3) work on the uncompressed text. SMP (Algorithm 4 + Algorithm 5) and SSA (Algorithm 4 + Algorithm 6) work on SLPs. The algorithms were implemented using the C++ language. We used std::map from the Standard Template Library (STL) for the associative array implementation. ¹ For constructing suffix

¹ We also used std::hash_map but omit the results due to lack of space. Choosing the hashing function to use is difficult, and we note that its performance was unstable and sometimes very bad when varying q.

arrays, we used the divsufsort library² developed by Yuta Mori. This implementation is not linear time in the worst case, but has been empirically shown to be one of the fastest implementations on various data.

All computations were conducted on a Mac Xserve (Early 2009) with 2 x 2.93GHz Quad Core Xeon processors and 24GB Memory, only utilizing a single process/thread at once. The program was compiled using the GNU C++ compiler (g++) 4.2.1 with the -fast option for optimization. The running times are measured in seconds, starting from after reading the uncompressed text into memory for NMP and NSA, and after reading the SLP that represents the text into memory for SMP and SSA. Each computation is repeated at least 3 times, and the average is taken.

5.1 Fibonacci Strings

The i th Fibonacci string F_i can be represented by the following SLP: $X_1 = b$, $X_2 = a$, $X_i = X_{i-1}X_{i-2}$ for i > 2, and $F_i = val(X_i)$. Fig. 3 shows the running times on Fibonacci strings $F_{20}, F_{25}, \ldots, F_{95}$, for q = 50. Although this is an extreme case since Fibonacci strings can be exponentially compressed, we can see that SMP and SSA that work on the SLP are clearly faster than NMP and NSA which work on the uncompressed string.

5.2 Pizza & Chili Corpus

We also applied the algorithms on texts XML, DNA, ENGLISH, and PROTEINS, with sizes 50MB, 100MB, and 200MB, obtained from the Pizza & Chili Corpus³. We used RE-PAIR [15] to obtain SLPs for this data.

Table 1 shows the running times for all algorithms and data, where q is varied from 2 to 10. We see that for all corpora, SMP and SSA running on SLPs are actually faster than NMP and NSA running on uncompressed text, when q is small. Furthermore,

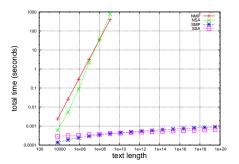


Fig. 3. Running times of NMP, NSA, SMP, SSA on Fibonacci strings for q = 50.

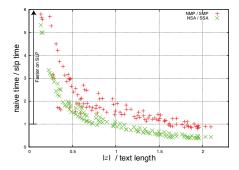


Fig. 4. Time ratios NMP/SMP and NSA/SSA plotted against ratio |z|/|T|.

http://code.google.com/p/libdivsufsort/

³ http://pizzachili.dcc.uchile.cl/texts.html

SMP is faster than SSA when q is smaller. Interestingly for XML, the SLP versions are faster even for q up to 9.

Fig. 4 shows the same results as time ratio: NMP/SMP and NSA/SSA, plotted against ratio: (length of z in Algorithm 4)/(length of uncompressed text). As expected, the SLP versions are basically faster than their uncompressed counterparts, when |z|/(text length) is less than 1, since the SLP versions run the weighted versions of the uncompressed algorithms on a text of length |z|. SLPs generated by other grammar based compression algorithms showed similar tendencies (data not shown).

6 Conclusion

We presented an O(qn) time and space algorithm for calculating all q-gram frequencies in a string, given an SLP of size n representing the string. This solves, much more efficiently, a more general problem than considered in previous work. Computational experiments on various real texts showed that the algorithms run faster than algorithms that work on the uncompressed string, when q is small. Although larger values of q allow us to capture longer character dependencies, the dimensionality of the features increases, making the space of occurring q-grams sparse. Therefore, meaningful values of q for typical applications can be fairly small in practice (e.g. $3 \sim 6$), so our algorithms have practical value.

A future work is extending our algorithms that work on SLPs, to algorithms that work on collage systems [14]. A Collage System is a more general framework for modeling various compression methods. In addition to the simple concatenation operation used in SLPs, it includes operations for repetition and prefix/suffix truncation of variables.

This is the first paper to show the potential of the compressed string processing approach in developing efficient and practical algorithms for problems in the field of string mining and classification. More and more efficient algorithms for various processing of text in compressed representations are becoming available. We believe texts will eventually be stored in compressed form by default, since not only will it save space, but it will also have the added benefit of being able to conduct various computations on it more efficiently later on, when needed.

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Table 1. Running times in seconds for data from the Pizza & Chili Corpus. Bold numbers represent the fastest time for each data and q. Times for SMP and SSA are prefixed with \triangleright , if they become fastest when all algorithms start from the SLP representation, i.e., NMP and NSA require time for decompressing the SLP (denoted by decompression time). The bold horizontal lines show the boundary where |z| in Algorithm 4 exceeds the uncompressed text length.

SURP Size: 2,702,383 decompression time: 0,82 secs 0,82 secs 1,73							XM	L							
	\Box	50MB									200MB				
The compression time: 1.23 Sept. Sept.				2,702,383					5,059,578				9.5	9,541,590	
2 8,106.861 5.9 9.8 1.1 2.0 15,178,446 12.0 2.10 2.1 4.3 28,624.88 24.7 46.9 4.3 8.9 3 13,413,565 13.0 9.8 2.5 3.2 25,160,162 27.8 21.1 4.9 6.8 47,504,478 58.7 46.1 9.8 14.3 4 18,364,951 21.0 9.8 5.7 4.7 34,881,658 47.2 21.3 11.3 9.9 65,496,619 100.3 46.2 22.5 20.0 5 22,873,060 28.7 9.8 10.2 5.9 43,275,004 63.0 21.1 20.4 12.5 82,321,682 139.4 46.2 40.1 25.1 6 27,032,514 35.2 9.8 14.9 7.1 51,354,178 71.1 21.0 20.0 14.8 98,124,580 172.4 46.3 59.4 30.2 7 30,908,898 40.0 9.8 9.4 8.2 88,935,352 87.4 21.1 38.9 16.9 113,084,186 197.7 46.8 78.5 34.9 8 34,555,233 44.3 9.8 26.0 9.3 6.104,075 97.5 21.1 52.5 19.1 127,316,007 218,3 46.3 10.3 93.9 9 37,983,150 49.0 9.8 31.0 10.1 72,859,310 105.3 21.1 60.9 20.9 140,846,749 23.6 46.3 148.8 48.8 S 50MB				0.3	82 secs										
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