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Problems in Size Expansion Analysis based on Hypothetical Relationships between Scale Factor, Exponential Function and Bondi K-Factor

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Exponential function is used not only for the basic growth analysis of the individual plant or animal in animal agriculture but also for the space expansion analysis in cosmology. This study was designed to investigate the problems in the size expansion analysis of the toy space model based on the hypothetical relationships between scale factor, exponential function and Bondi K-factor. Problems (A) ~ (E) were shown. (A) The toy space model using Bondi K-factor was related to the Minkowski space (flat space-time), which was different from the standard model of cosmic expansion based on the FLRW metric. (B) The toy space model was related to the relativistic Doppler redshift, but not to the cosmological redshift that was used in the standard model. (C) Even if Bondi K-factor was hypothetically and forcedly related to the cosmic scale factor through exponential function, the relativistic Doppler redshift merely gave a very poor approximation to the cosmological redshift. (D) The rapid but decelerated expansion at the early stage of the toy space model was not consistent with the accelerated expansion of the inflationary theory. (E) The toy space model did not give the information on the energy distribution of the universe (baryonic matter, dark matter and dark energy), though this toy model gave a mathematical curve composed of early rapid expansion in decelerated expansion, inflection point and accelerated expansion. In conclusion, this study showed that the toy space model using Bondi K-factor had various problems when compared with the standard model of cosmic expansion.

Key words: Bondi K-factor, cosmological redshift, exponential function, relativistic Doppler redshift, scale factor

INTRODUCTION

Animal agriculture is based on the production of plants and animals. The basic growth analysis of the individual plant (Blackman, 1919) or animal (Brody, 1945) is conducted using exponential function. Exponential function is used also for the description of the accelerated expansion at the early inflationary stage (Starobinsky, 1980; Kazanas, 1980; Sato, 1981; Guth, 1981; Linde, 1982; Albrecht and Steinhardt, 1982) and at the present stage (Riess *et al.*, 1998; Perlmutter *et al.*, 1999) in the cosmic history. Tegmark (2014) describes that the inflation theory says that our baby universe grew much like a human baby. Thus, analyzing the growth of individual animal seems to be mathematically similar to analyzing the cosmic expansion. These are why I am interested in the size expansion analysis using exponential function.

Exponential function is known to be equivalent to Bondi K-factor (for example, Lavenda, 2000), the factor that was proposed by Bondi (1964) as a useful educational tool of the special relativity. Bondi K-factor, through the recession velocity of the moving object, is related to the relativistic Doppler redshift. However, as Weinberg (2008) describes, the standard model of cosmic expansion uses the cosmological redshift that depends on the increase of the cosmic scale factor in the whole

period from the emission to the absorption of light. In recent 15 years, there are many studies on whether or not or how the relativistic Doppler redshift is related to the cosmic history (for example, Bedran, 2002; Macleod, 2004; Chodorowski, 2006; Sitnikov, 2006; Francis *et al.*, 2007; Peacock, 2008; Bunn and Hogg, 2009; Rabounski, 2009; Farley, 2010; Davis, 2010; Ben-Amots, 2011; Rebhan, 2012; Kaiser, 2013; May and Yu, 2013; Wagh, 2013; Kipreos, 2014; Konushko, 2014; Li, 2014; Pierseaux, 2014; MacCallum, 2015; Santilli, 2015). Subsequent reports (Shimojo, 2014, 2015) suggested a hypothetical interpretation of Bondi K-factor as a toy space model, showing a mathematical curve that is composed of early rapid expansion, decelerated expansion, inflection point, and accelerated expansion. However, the standard theory uses the cosmological redshift for the investigation of cosmic expansion.

The present study was designed to investigate the problems in the size expansion analysis of the toy space model based on the hypothetical relationships between scale factor, exponential function and Bondi K-factor.

PROBLEMS IN A TOY SPACE MODEL USING BONDİ K-FACTOR

The standard model of cosmic expansion

If based on the cosmological principle, then the standard model of cosmic expansion is given by expressions (1) ~ (5),

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$$\left(\frac{1}{a} \cdot \frac{da}{dt}\right)^2 = \frac{8\pi G}{3c^2} \rho - \frac{c^2 K}{a^2} + \frac{c^2 \Lambda}{3}, \quad (1)$$

$$H = \frac{1}{a} \cdot \frac{da}{dt}, \quad (2)$$

$$a \propto \exp(H \cdot t), \quad (3)$$

$$\frac{a(t_2)}{a(t_1)} = \exp\left[\int_{t_1}^{t_2} H dt\right], \quad (4)$$

$$Z_c = \frac{a(t_2)}{a(t_1)} - 1 = \frac{\lambda_2}{\lambda_1} - 1, \quad (5)$$

where t = time, a = scale factor, π = circular constant, G = gravitational constant, c = speed of light in vacuum, ρ = energy density, p = pressure, K = curvature of space, Λ = cosmological constant, H = Hubble parameter (cosmic expansion rate), Z_c = cosmological redshift from t_1 (emmission of light) to t_2 (absorption of light), λ = wavelength.

A toy space model using Bondi K-factor

A toy space model using Bondi K-factor [$B(v)$] is given by expressions (6) ~ (8) that are altered from the previous reports (Shimojo, 2014, 2015),

$$B(v) = \sqrt{\frac{c-v}{c+v}}, \quad (6)$$

$$Z_R = \frac{1}{B(v)} - 1 = \sqrt{\frac{c+v}{c-v}} - 1 = \frac{\lambda_2}{\lambda_1} - 1, \quad (7)$$

$$B(v) \cdot (Z_R + 1) = B(v) \cdot \frac{1}{B(v)} = 1, \quad (8)$$

where $B(v)$ = space size ratio (toy space model), c = speed of light in vacuum, v = recession speed of moving object, $c \geq v \geq -c$, $0 \leq B(v) < \infty$, Z_R = relativistic Doppler redshift, λ = wavelength.

Equivalence of Bondi K-factor and exponential function

Expressions (9) and (10) give expressions (11) and (12) that show the equivalence of Bondi K-factor and exponential function,

$$\frac{1}{\sqrt{1 - v^2/c^2}} = \frac{\exp(\theta) + \exp(-\theta)}{2}, \quad (9)$$

$$\frac{v/c}{\sqrt{1 - v^2/c^2}} = \frac{\exp(\theta) - \exp(-\theta)}{2}, \quad (10)$$

$$\sqrt{\frac{c \pm v}{c \mp v}} = \exp(\pm\theta), \quad (11)$$

$$\pm \frac{v}{c} = \frac{\exp(\pm 2\theta) - 1}{\exp(\pm 2\theta) + 1}, \quad (12)$$

where double-sign corresponds.

Relativistic Doppler redshift as a very poor approximation to cosmological redshift

Expression (3) shows that the cosmic scale factor is proportional to exponential function with a variable of Hubble parameter. Expression (11) shows that Bondi K-factor is described using exponential function. Since the relativistic Doppler redshift (Z_R) is conceptually different from the cosmological redshift (Z_c), hypothetically and forcedly relating expressions (7) to (5) through exponential function shows that Z_R merely gives a very poor approximation to Z_c [(13) ~ (15)],

$$\sqrt{\frac{c+v}{c-v}} \sim \frac{a(t_2)}{a(t_1)}, \quad (13)$$

$$Z_R \sim Z_c, \quad (14)$$

$$\frac{v}{c} \sim \frac{[a(t_2)/a(t_1)]^2 - 1}{[a(t_2)/a(t_1)]^2 + 1}. \quad (15)$$

There is a hypothesis that Z_c is interpreted as the accumulation of the infinitesimal Z_R (for example, Bunn and Hogg, 2009; Matsubara, 2013). There are some studies that suggest the use of the relativistic Doppler redshift (for example, Bunn and Hogg, 2009; May and Yu, 2013; Pierseaux, 2014). These may give the reason why Bondi K-factor is hypothetically interpreted as a toy space model (Shimojo, 2014, 2015). However, this toy space model is based on the concept that is different from that of the standard model.

Hypothetical phenomena in the size expansion analysis of the toy space model

Despite the serious problems, the toy space model using Bondi K-factor [(6) ~ (7)] seems to suggest mathematical phenomena (i) ~ (iv) about the space expansion. (i) The toy space model (6) shows an early rapid expansion in the context of the decelerated expansion that continues until the inflection point, at which point there turns into the accelerated expansion. (ii) The inflection point of $B(v)$ is the halfway point [$v = c/2$, $B(c/2) = 0.577$, $Z_R = 0.732$] between the birth point [$v = c$, $B(c) = 0$, $Z_R = \infty$] and the present point [$v = 0$, $B(0) = 1$, $Z_R = 0$]. (iii) The relativistic expansion of the toy space model reflects the balance between the attractive force (baryonic matter and dark matter) and the repulsive force (dark energy). (iv) The relativistic Doppler redshift (Z_R) + 1 is related to the energy density of the toy space model.

Perlmutter *et al.* (1999) showed that the crossover between the deceleration and the acceleration occurred when redshift ≈ 0.73 . Perlmutter (2011) showed that the best fit curve was decelerating for about the first seven billion years, and then accelerating for the most recent approximately seven billion years. Choi (2010) reported the decelerating expansion until about 7 billion years, and accelerating expansion from 7 billion years ago. Barrow (2011) described that the deceleration was switched to the acceleration when the universe was expanded to about 57% of the present size.

However, the early decelerated expansion of the toy space model is not consistent with the early accelerated expansion in the cosmic inflation theory proposed by preceding studies (Starobinsky, 1980; Kazanas, 1980; Sato, 1981; Guth, 1981; Linde, 1982; Albrecht and Steinhardt, 1982). In addition, the toy space model does not give the information on the energy distribution of the universe that was reported by preceding studies (Riess *et al.*, 1998; Perlmutter *et al.*, 1999; Komatsu *et al.*, 2009).

The universe is considered almost flat (Guth, 1981; Linde, 1982). Bondi K-factor (relativistic Doppler redshift) is related to the Minkowski space that is flat space-time. However, the standard model of cosmic expansion is based on the FLRW metric (the cosmological redshift).

Hypothetical relationships between some natural phenomena

The natural logarithm of expression (8) gives expression (16),

$$B(v) \cdot \frac{1}{B(v)} = \sqrt{\frac{c-v}{c+v}} \cdot \sqrt{\frac{c+v}{c-v}} = 1, \quad (8)$$

$$\ln\left(\sqrt{\frac{c-v}{c+v}} \cdot \sqrt{\frac{c+v}{c-v}}\right) = \ln(1). \quad (16)$$

Thus,

$$\ln\left(\sqrt{\frac{c-v}{c+v}}\right) + \ln\left(\sqrt{\frac{c+v}{c-v}}\right) = 2n\pi i, \quad (17)$$

$$= 2n\pi \cdot \frac{\psi(x, t) - \psi^*(x, t)}{2A \sin(x, t)}, \quad (18)$$

$$= 2n\pi \cdot \left(\frac{xp - px}{h/2\pi}\right), \quad (19)$$

$$= 2n\pi \cdot \lim_{v \rightarrow \infty} \sqrt{\frac{c \pm v}{c \mp v}}, \quad (20)$$

$$= 2n\pi \cdot \sqrt{\frac{m^2 c^4}{p^2 c^2 - E^2}}, \quad (21)$$

$$= 2n\pi \cdot \sqrt{\frac{(ct)^2}{s^2 - (x^2 + y^2 + z^2)}}, \quad (22)$$

$$= 2n\pi \cdot \sqrt{\frac{\Lambda g_{\mu\nu}}{G_{\mu\nu} - kT_{\mu\nu}}}, \quad (23)$$

where n = integers, π = circular constant, i = imaginary unit, x = position, p = momentum, $\psi(x, t)$ = wave function, $\psi^*(x, t)$ = conjugate complex of $\psi(x, t)$, $\sin(x, t)$ = sine function, A = amplitude, $g_{\mu\nu}$ = metric tensor, $G_{\mu\nu}$ = Einstein tensor, $T_{\mu\nu}$ = energy-momentum tensor, κ = Einstein's constant of gravitation, Λ = cosmological constant, double-sign corresponds.

Expressions (17) ~ (19) seem to suggest a hypothetical relationship between the relativistic expansion of the toy space model and the quantum phenomenon. Expressions (17) ~ (23) seem to suggest a hypothesis that the toy space model using Bondi K-factor relates some natural phenomena through the imaginary unit.

The imaginary unit is given by the mathematical application of the infinite velocity to Bondi K-factor (20). The velocity is defined by dividing distance traveled by time elapsed. Since it is impossible to define the infinite distance, the infinite velocity is hypothetically and forcedly defined by dividing the given distance traveled by no time elapsed. Thus, the infinite velocity seems to be hypothetically interpreted as the simultaneous existence of different states (superposition), which seems to be something like oneness, wholeness, or ubiquity. However, the infinite velocity breaks the Lorentz invariance.

John Bell answered in the interview with him (Davies and Brown, 1986), "Behind the apparent Lorentz invariance of the phenomena, there is a deeper level which is not Lorentz invariant. The reason I want to go back to the idea of an aether here is because in these EPR experiments there is the suggestion that behind the scenes something is going faster than light. It is as if there is some kind of conspiracy, that something is going on behind the scenes which is not allowed to appear on the scenes. And that's very ironic, because it is precisely his own theory of relativity which creates difficulties for this interpretation of the quantum theory (which is in the spirit of Einstein's unconventional view of quantum mechanics)." Alain Aspect answered in the interview with him (Davies and Brown, 1986), "However, if you mean that in some picture of the world that you want to construct, you can include some kind of faster than light mathematical object, then perhaps, yes, it could be a possibility. But you cannot use this mathematical construction for practical faster-than-light signalling. However, all that they demolish is the possibility of having hidden variable theory based on Einstein's ideas such as separability."

Needless to say, the quantum phenomenon is considered basic to molecular biology in animal agriculture. Expressions (17) ~ (23) seem to suggest a hypothesis that the quantum phenomena squared leads to the phe-

nomena observed actually.

Hypothetical phenomena in the birth point of the toy space model

If substituting c for v in expression (8), then the birth point of the toy space model seems to be hypothetically given by expression (24),

$$\begin{aligned} B(c) \cdot \frac{1}{B(c)} &= \sqrt{\frac{c-c}{c+c}} \cdot \sqrt{\frac{c+c}{c-c}} \\ &= \sqrt{\frac{0}{2c}} \cdot \sqrt{\frac{2c}{0}} \\ &= 0 \cdot \infty = 1. \end{aligned} \quad (24)$$

Expression (24) seems to suggest a massless state ($v = c$) when the size of the toy space model is zero [$B(c) = 0$] at the birth point. Does the state of ∞ in (24) seem to suggest a hypothesis that the energy density is ∞ at the birth point of the toy space model? Does '1' in (24) seem to suggest a hypothesis that the singularity at the birth point is under the control of the invariant?

The natural logarithm of expression (24) gives expressions (25) ~ (26) and (18) ~ (19),

$$\ln(0 \cdot \infty) = \ln(1), \quad (25)$$

$$-\infty + \infty = 2n\pi i, \quad (26)$$

$$= 2n\pi \cdot \frac{\psi(x, t) - \psi^*(x, t)}{2A \sin(x, t)}, \quad (18)$$

$$= 2n\pi \cdot \left(\frac{xp - px}{h/2\pi} \right). \quad (19)$$

Expressions (24) ~ (26) and (18) ~ (19) seem to suggest a hypothesis that the toy space model was born from the quantum phenomenon (or from the seeming zero) [(18) ~ (19)] through something like a renormalization of infinities (26). However, this hypothetical phenomenon suggested by the toy space model is not consistent with preceding studies on the cosmic birth (Vilenkin, 1982; Hartle and Hawking, 1983).

Conclusions

This study shows that the toy space model using Bondi K-factor has various problems when compared with the standard model of cosmic expansion.

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