Introducing Viewpoints of Mechanics into Basic Growth Analysis : (VIII) Applying Basic Growth Mechanics to Ruminants, Forages and Related Problems

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Introducing Viewpoints of Mechanics into Basic Growth Analysis – (VIII) Applying Basic Growth Mechanics to Ruminants, Forages and Related Problems –

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This study was conducted to investigate the way of calculation in the application of basic growth mechanics to the ruminant animal, the forage plant, indigestibility increase with forage growth and net assimilation rate of the forage plant. The results obtained were as follows. (1) The mean value over the given interval for absolute growth rate of weight (AGRw) was described using the product of mean weight (W) and mean growth acceleration of W (GAW). (2) The mean value over the given interval for AGRi (AGR of indigestible matter (I)) was described using the product of mean value of I and that of GAI (GA of I). (3) The indigestibility increase with forage growth, which was given by two different descriptions, was described using mean value over the given interval for I , that for GAI, that for W and that for GAW. (4) The mean value over the given interval for net assimilation rate (NAR) of the forage plant was described using mean leaf area (A), mean W and mean GAW. It was suggested that applying basic growth mechanics gave a unified viewpoint to concepts of analyzing the ruminant animal growth, the forage plant growth, indigestibility increase with forage growth and net assimilation rate of the forage plant.

INTRODUCTION

Shimojo *et al.* (2006, 2007a, 2007b, 2008) introduced viewpoints of mechanics into basic growth analysis of the ruminant animal (Brody, 1945; Shimojo *et al.*, 1997) and the forage plant (Blackman, 1919; Watson, 1952; Radford, 1967; Hunt, 1990). This suggests a differential equation that describes absolute growth rate using the square root of the product of weight and growth acceleration. However, we did not show the way of calculation when applied to the actual data collected from growth experiments of the ruminant and the forage. The growth of ruminant animal depends mainly on intake of digestible materials in the forage plant. It is well known that there is an increase in the weight of indigestible materials with the growth of forage, which causes the decrease in forage digestibility. Therefore, analyzing the process of forage growth and indigestibility increase gives useful information to the development of forage-based ruminant agriculture from the viewpoint of supplying the high quality forage to the ruminant.

The present study was designed to investigate the way of calculation in the application of basic growth mechanics to the ruminant animal, the forage plant, indigestibility increase with forage growth and net assimilation rate of the forage plant.

APPLYING GROWTH MECHANICS TO THE RUMINANT ANIMAL, THE FORAGE PLANT AND RELATED PROBLEMS

(A) Basic growth mechanics

Shimojo *et al.* (2006, 2007a, 2007b, 2008) suggested basic growth mechanics using a series of the following calculations. Thus,

$$(1/W) \cdot (dW/dt) = \text{RGRw}, \quad (1)$$

$$W = W_0 \cdot \exp(\text{RGRw} \cdot t), \quad (2)$$

where W =weight of the ruminant animal or the forage plant at time t , RGRw=relative growth rate of W , W_0 =weight at $t=0$.

Then,

$$\text{AGRw} = dW/dt = \text{RGRw} \cdot W_0 \cdot \exp(\text{RGRw} \cdot t), \quad (3)$$

$$\text{GAW} = d^2W/dt^2 = (\text{RGRw})^2 \cdot W_0 \cdot \exp(\text{RGRw} \cdot t), \quad (4)$$

where AGRw=absolute growth rate of W , GAW=growth acceleration of W .

Relating functions (2)~(4) gives

$$(\text{AGRw}/W) = (\text{GAW}/\text{AGRw}) = \text{RGRw}, \quad (5)$$

$$(\text{AGRw})^2 = W \cdot \text{GAW}. \quad (6)$$

Function (6) shows that AGRw is equal to the product of W and GAW. This relation has an analogy with Newton's equation of motion (Kawabe, 2006), where force (F) is described as the product of mass (m) of an object and

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acceleration (a), namely $F=m \cdot a$. Thus, the left-hand side of function (6) might be regarded as growth force.

The mean value over the interval t_1 to t_2 is calculated for the three terms of function (6) using actual data. The ways of calculation of them are given by,

$$\overline{AGRW} = \frac{W_2 - W_1}{t_2 - t_1}, \quad (7)$$

$$\overline{W} = \frac{W_2 - W_1}{\log_e W_2 - \log_e W_1}, \quad (8)$$

$$\overline{GAW} = \frac{GAW_2 - GAW_1}{\log_e GAW_2 - \log_e GAW_1}, \quad (9)$$

$$= \frac{AGRW_2 - AGRW_1}{t_2 - t_1}. \quad (10)$$

Expression (10) is the definition of $\overline{GAW}$, and it is also given by expression (9) in basic growth mechanics. Thus, combining expressions (6)~(10) gives

$$\overline{AGRW} = \sqrt{\overline{W} \cdot \overline{GAW}}, \quad (11)$$

$$\frac{W_2 - W_1}{t_2 - t_1} = \sqrt{\frac{W_2 - W_1}{\log_e W_2 - \log_e W_1} \cdot \frac{GAW_2 - GAW_1}{\log_e GAW_2 - \log_e GAW_1}}, \quad (12)$$

$$= \sqrt{\frac{W_2 - W_1}{\log_e W_2 - \log_e W_1} \cdot \frac{AGRW_2 - AGRW_1}{t_2 - t_1}}. \quad (13)$$

Expressions (12) and (13) show that mean AGRw over the interval t_1 to t_2 is evaluated by two components that are mean W and mean GAW . It is, therefore, interesting to investigate relationships between W and GAW , namely how the size of W influences GAW . This has an analogy with the issue of motion: how the mass size of an object affects its acceleration (Kawabe, 2006). When W of the ruminant animal or the forage plant is large, high GAW is required to get high AGRw. GAW is related to many animal or plant factors: feed intake and digestibility, animal breeds and other factors for the ruminant animal, and light receiving ability of leaves, nutrients absorption ability of roots and other factors for the forage plant.

(B) Applying basic growth mechanics to formation of forage indigestible matter

Basic growth mechanics for forage indigestible matter is given by a series of the following calculations. Thus,

$$I = I_0 \cdot \exp(RGRi \cdot t), \quad (14)$$

where I =indigestible matter weight of the forage plant at time t , I_0 =forage indigestible matter weight at $t=0$, $RGRi$ =relative growth rate of I .

Then,

$$AGRi = dI/dt = RGRi \cdot I_0 \cdot \exp(RGRi \cdot t), \quad (15)$$

$$GAi = d^2I/dt^2 = (RGRi)^2 \cdot I_0 \cdot \exp(RGRi \cdot t), \quad (16)$$

where $AGRi$ =absolute growth rate of I , GAi =growth acceleration of I .

Relating functions (14)~(16) gives

$$(AGRi/I) = (GAi/AGRi) = RGRi, \quad (17)$$

$$(AGRi)^2 = I \cdot GAi. \quad (18)$$

The mean value over the interval t_1 to t_2 is calculated for the three terms of function (18) using actual data of the forage plant. The ways of calculation of them are given by,

$$\overline{AGRi} = \frac{I_2 - I_1}{t_2 - t_1}, \quad (19)$$

$$\bar{I} = \frac{I_2 - I_1}{\log_e I_2 - \log_e I_1}, \quad (20)$$

$$\overline{GAi} = \frac{GAi_2 - GAi_1}{\log_e GAi_2 - \log_e GAi_1}, \quad (21)$$

$$= \frac{AGRi_2 - AGRi_1}{t_2 - t_1}. \quad (22)$$

Thus, combining expressions (18)~(22) gives

$$\overline{AGRi} = \sqrt{\bar{I} \cdot \overline{GAi}}, \quad (23)$$

$$\frac{I_2 - I_1}{t_2 - t_1} = \sqrt{\frac{I_2 - I_1}{\log_e I_2 - \log_e I_1} \cdot \frac{GAi_2 - GAi_1}{\log_e GAi_2 - \log_e GAi_1}}, \quad (24)$$

$$= \sqrt{\frac{I_2 - I_1}{\log_e I_2 - \log_e I_1} \cdot \frac{AGRi_2 - AGRi_1}{t_2 - t_1}}. \quad (25)$$

When the forage plant has large I , high $AGRi$ requires high GAi . GAi is related to maturing of the forage plant such as lignification and silicification of plant fiber fractions and high ratio of stem to leaf. However, this reduces forage utilization by ruminants, anti-quality characteristics of the plant.

(C) Applying basic growth mechanics of forage indigestible matter formation to indigestibility increase with forage growth

Investigating indigestibility is recommended to analyze forage digestion characteristics, because there is usually a continuous increase of indigestible matter weight with forage growth compared with digestible matter weight that often shows a decrease when the forage matures. We take up two types of functions that describe indigestibility increase with forage growth: function (26) suggested by Masuda (1985) and function (27) suggested by Shimojo *et al.* (1995). Both func-

tions were compared and related by Shimojo *et al.* (1998). Thus,

$$\frac{I_2}{W_2} - \frac{I_1}{W_1} = \frac{I_1}{W_1} \cdot [\exp((\overline{\text{RGRi}} - \overline{\text{RGRw}}) \cdot (t_2 - t_1)) - 1], \quad (26)$$

$$\frac{I_2}{W_2} - \frac{I_1}{W_1} = \left(1 - \frac{I_1}{W_1}\right) \cdot \left(\frac{\overline{\text{AGRi}}}{\overline{\text{AGRw}}} - \frac{I_1}{W_1}\right). \quad (27)$$

(C-1) Analyzing indigestibility increase using function (26)

RGRw in function (26) is replaced with RGAW according to a series of the following procedures. Thus,

$$(\text{AGRw})^2 = W \cdot \text{GAw}, \quad (6)$$

$$(dW/dt)^2 = W \cdot (d^2W/dt^2), \quad (28)$$

$$(1/W) \cdot (dW/dt) = \sqrt{(1/W) \cdot (d^2W/dt^2)}, \quad (29)$$

$$\text{RGRw} = \sqrt{\text{RGAW}}, \quad (30)$$

where RGRw=relative growth rate of W , RGAW=relative growth acceleration of W .

Likewise, applying these procedures to I gives

$$(1/I) \cdot (dI/dt) = \sqrt{(1/I) \cdot (d^2I/dt^2)}, \quad (31)$$

$$\text{RGRi} = \sqrt{\text{RGAi}}, \quad (32)$$

where RGRi=relative growth rate of I , RGAi=relative growth acceleration of I .

The mean value over the interval t_1 to t_2 for functions (30) and (32) are given by

$$\overline{\text{RGRw}} = \sqrt{\overline{\text{RGAW}}}, \quad \overline{\text{RGRi}} = \sqrt{\overline{\text{RGAi}}}. \quad (33)$$

Therefore,

$$\begin{aligned} \overline{\text{RGRw}} &= \frac{\log_e W_2 - \log_e W_1}{t_2 - t_1} \\ &= \sqrt{\frac{\log_e W_2 - \log_e W_1}{W_2 - W_1} \cdot \frac{\text{GAw}_2 - \text{GAw}_1}{\log_e \text{GAw}_2 - \log_e \text{GAw}_1}}, \end{aligned} \quad (34)$$

$$= \sqrt{\frac{\log_e W_2 - \log_e W_1}{W_2 - W_1} \cdot \frac{\text{AGRw}_2 - \text{AGRw}_1}{t_2 - t_1}}. \quad (35)$$

$$\begin{aligned} \overline{\text{RGRi}} &= \frac{\log_e I_2 - \log_e I_1}{t_2 - t_1} \\ &= \sqrt{\frac{\log_e I_2 - \log_e I_1}{I_2 - I_1} \cdot \frac{\text{GAi}_2 - \text{GAi}_1}{\log_e \text{GAi}_2 - \log_e \text{GAi}_1}}, \end{aligned} \quad (36)$$

$$= \sqrt{\frac{\log_e I_2 - \log_e I_1}{I_2 - I_1} \cdot \frac{\text{AGRi}_2 - \text{AGRi}_1}{t_2 - t_1}}. \quad (37)$$

Using functions (34)~(37), function (26) is rewritten by two ways of description as follows,

$$\begin{aligned} \frac{I_2}{W_2} - \frac{I_1}{W_1} &= \frac{I_1}{W_1} \cdot [\exp((\sqrt{\overline{\text{RGAi}}} - \sqrt{\overline{\text{RGAW}}}) \cdot (t_2 - t_1)) - 1], \\ &= \frac{I_1}{W_1} \cdot \left[\exp\left(\left(\sqrt{\frac{\log_e I_2 - \log_e I_1}{I_2 - I_1} \cdot \frac{\text{GAi}_2 - \text{GAi}_1}{\log_e \text{GAi}_2 - \log_e \text{GAi}_1}} \right. \right. \right. \\ &\quad \left. \left. - \sqrt{\frac{\log_e W_2 - \log_e W_1}{W_2 - W_1} \cdot \frac{\text{GAw}_2 - \text{GAw}_1}{\log_e \text{GAw}_2 - \log_e \text{GAw}_1}} \right) \right. \\ &\quad \left. \cdot (t_2 - t_1) - 1 \right], \end{aligned} \quad (38)$$

$$\begin{aligned} &= \frac{I_1}{W_1} \cdot \left[\exp\left(\left(\sqrt{\frac{\log_e I_2 - \log_e I_1}{I_2 - I_1} \cdot \frac{\text{AGRi}_2 - \text{AGRi}_1}{t_2 - t_1}} \right. \right. \right. \\ &\quad \left. \left. - \sqrt{\frac{\log_e W_2 - \log_e W_1}{W_2 - W_1} \cdot \frac{\text{AGRw}_2 - \text{AGRw}_1}{t_2 - t_1}} \right) \right. \\ &\quad \left. \cdot (t_2 - t_1) - 1 \right]. \end{aligned} \quad (39)$$

(C-2) Analyzing indigestibility increase using function (27)

Likewise, function (27) is rewritten by two ways of description as follows,

$$\begin{aligned} \frac{I_2}{W_2} - \frac{I_1}{W_1} &= \left(1 - \frac{W_1}{W_2}\right) \cdot \frac{\sqrt{\bar{I}} \cdot \overline{\text{GAi}}}{\sqrt{\bar{W}} \cdot \overline{\text{GAw}}} - \frac{I_1}{W_1} \\ &= \left(1 - \frac{W_1}{W_2}\right) \cdot \left(\sqrt{\frac{\log_e I_2 - \log_e I_1}{I_2 - I_1} \cdot \frac{\text{GAi}_2 - \text{GAi}_1}{\log_e \text{GAi}_2 - \log_e \text{GAi}_1}} \right. \\ &\quad \left. \sqrt{\frac{\log_e W_2 - \log_e W_1}{W_2 - W_1} \cdot \frac{\text{GAw}_2 - \text{GAw}_1}{\log_e \text{GAw}_2 - \log_e \text{GAw}_1}} \right. \\ &\quad \left. - \frac{I_1}{W_1} \right), \end{aligned} \quad (40)$$

$$\begin{aligned} &= \left(1 - \frac{W_1}{W_2}\right) \cdot \left(\sqrt{\frac{\log_e I_2 - \log_e I_1}{I_2 - I_1} \cdot \frac{\text{AGRi}_2 - \text{AGRi}_1}{t_2 - t_1}} \right. \\ &\quad \left. \sqrt{\frac{\log_e W_2 - \log_e W_1}{W_2 - W_1} \cdot \frac{\text{AGRw}_2 - \text{AGRw}_1}{t_2 - t_1}} \right. \\ &\quad \left. - \frac{I_1}{W_1} \right). \end{aligned} \quad (41)$$

Functions (38)~(41) show that indigestibility increase with forage growth over the interval t_1 to t_2 is evaluated by four components: mean W , mean I , mean GAw and mean GAI. It is, therefore, interesting to investigate how the size of W influences GAw and how the size of I influences GAI.

(D) Applying basic growth mechanics to net assimilation rate of the forage plant

Since leaf area plays an important role in the plant growth, the simple growth analysis of the forage plant is usually given by

$$(1/W) \cdot (dW/dt) = (1/A) \cdot (dW/dt) \cdot (A/W), \quad (42)$$

where A =leaf area of the forage plant,

$(1/A) \cdot (dW/dt)$ =net assimilation rate (NAR), (A/W) =leaf area ratio (LAR).

Combining differential equations (42) and (29) gives

$$\sqrt{(1/W) \cdot (d^2W/dt^2)} = \left\{ (1/A) \cdot \sqrt{W \cdot (d^2W/dt^2)} \right\} \cdot (A/W), \quad (43)$$

where the expression in braces in the right-hand side gives NAR.

The mean value of NAR over the interval t_1 to t_2 in function (43) is given by

$$\begin{aligned} \overline{\text{NAR}} &= \frac{\log_e A_2 - \log_e A_1}{A_2 - A_1} \\ &\cdot \sqrt{\frac{W_2 - W_1}{\log_e W_2 - \log_e W_1} \cdot \frac{\text{GAW}_2 - \text{GAW}_1}{\log_e \text{GAW}_2 - \log_e \text{GAW}_1}}, \end{aligned} \quad (44)$$

$$\begin{aligned} &= \frac{\log_e A_2 - \log_e A_1}{A_2 - A_1} \\ &\cdot \sqrt{\frac{W_2 - W_1}{\log_e W_2 - \log_e W_1} \cdot \frac{\text{AGRW}_2 - \text{AGRW}_1}{t_2 - t_1}}, \end{aligned} \quad (45)$$

(E) Conclusions

It is suggested from the present study that applying basic growth mechanics gives a unified viewpoint to concepts of analyzing the ruminant animal growth, the forage plant growth, indigestibility increase with forage growth and net assimilation rate of the forage plant.

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